

NUMERICAL MODELING TECHNIQUES AND APPLICATIONS

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Yong Wei
Vasily Titov*

*NOAA/PMEL
University of Washington*



Tsunamis and Tsunami Warning Systems: Talk Structure

-Tsunamis:

- Generation
- Physical characteristics

-Tsunami Detection:

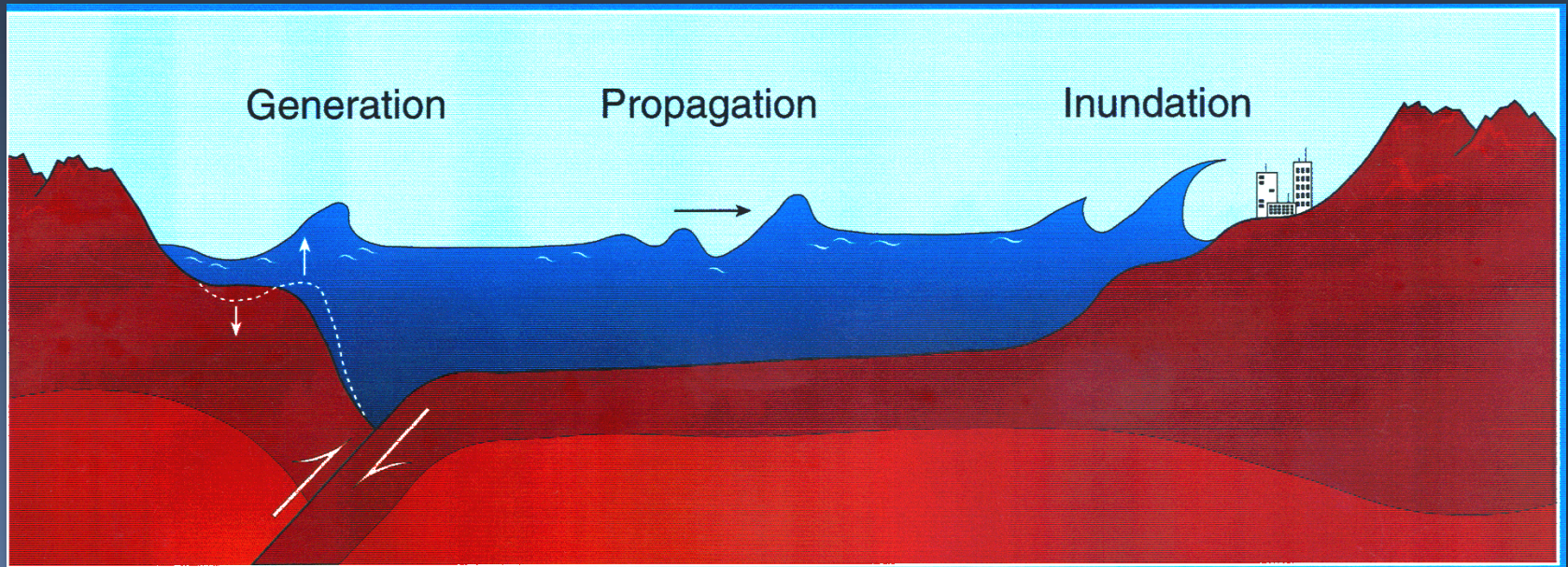
- Earthquake Based
- Tsunami Based

-Tsunami Forecasting:

- Linearity in deep water.
- Inversion of DART data.
- Forecast Model Development.
- Early events.
- Chile, February 2010.

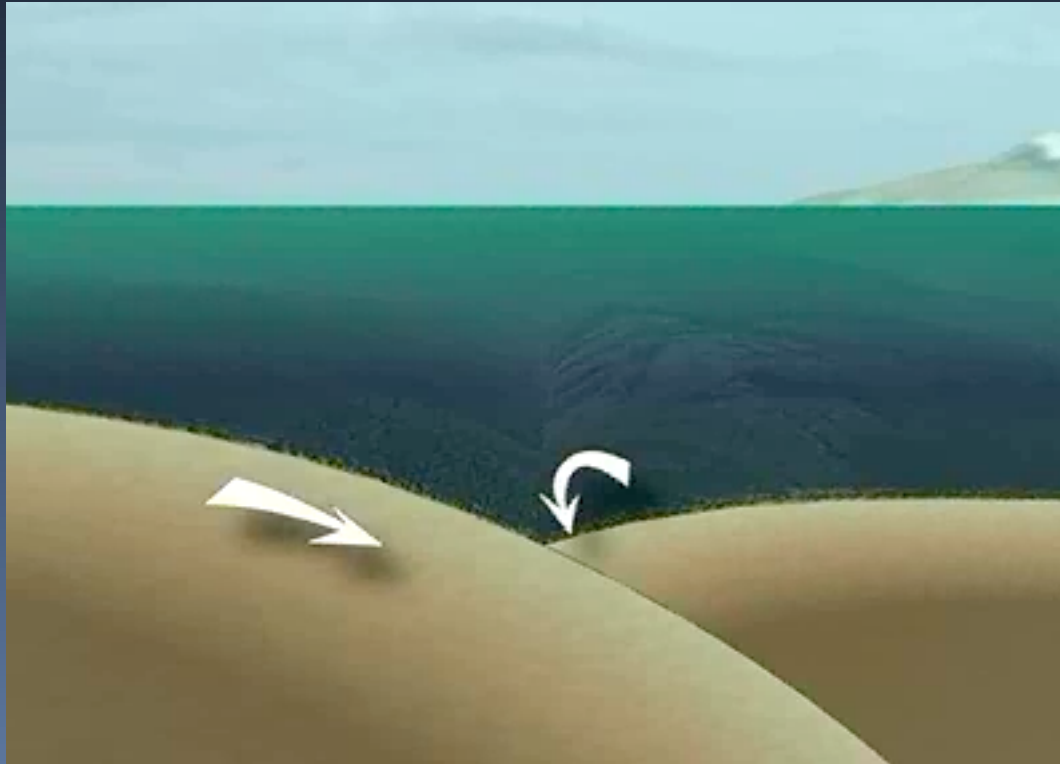
Three phases of tsunamis:

- Generation
- Propagation
- Inundation



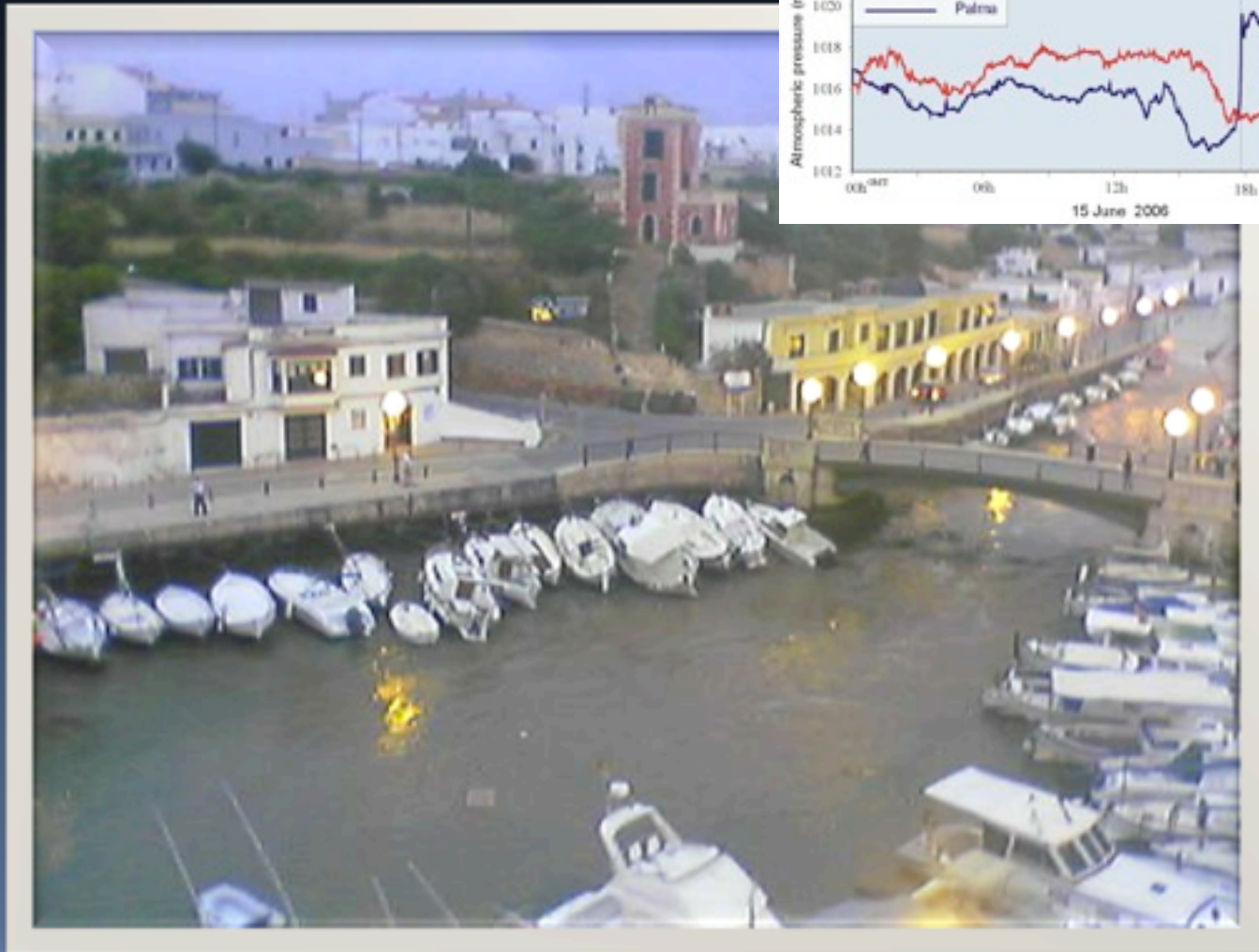
Tsunami Generation

Typical method: earthquake at plate boundary



Tsunamigenic Phenomena

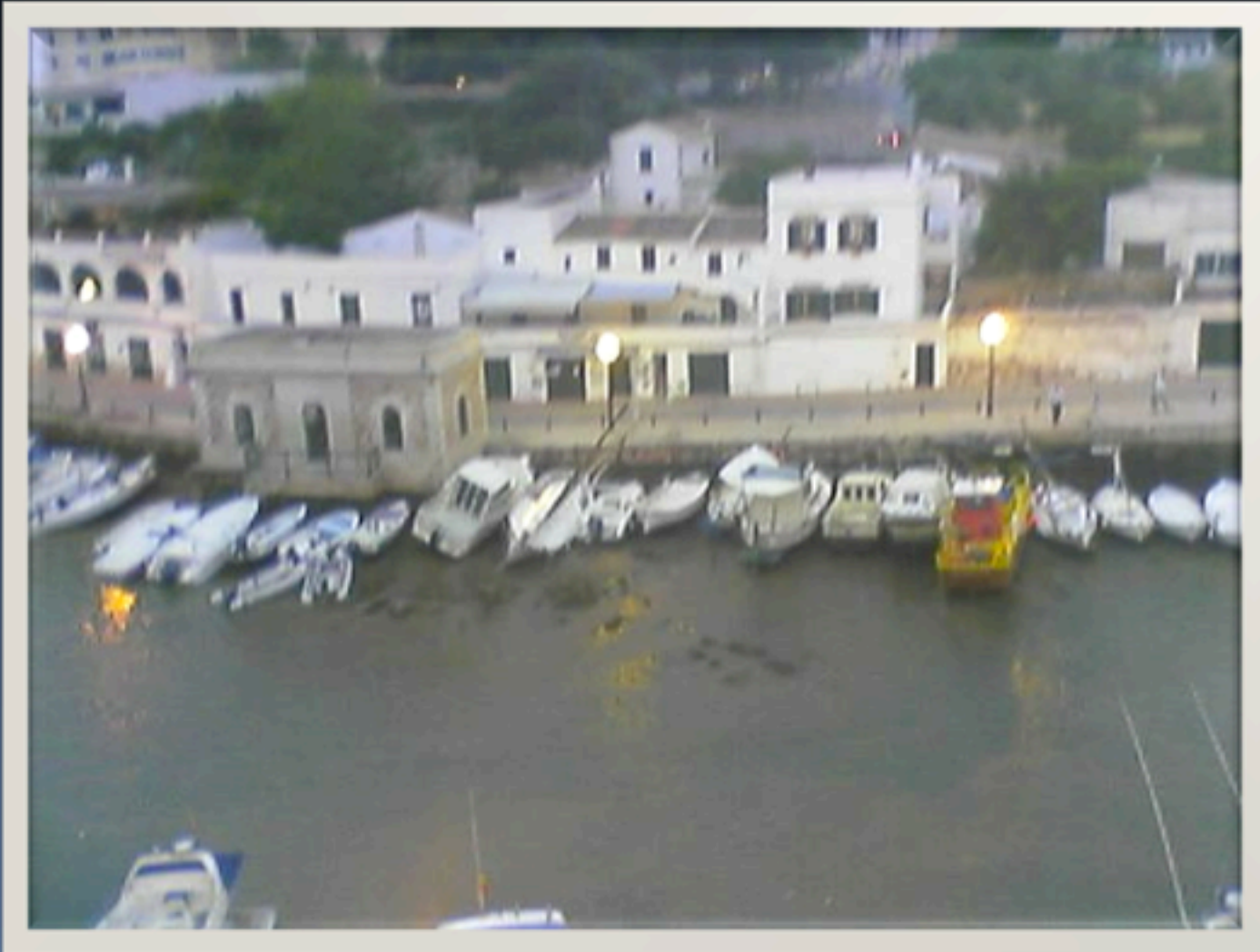
- Meteorological Tsunamis.



Ciudadella, Spain, Tsunami June 15, 2006: Slide1

Tsunamigenic Phenomena

- Meteorological Tsunamis.



Ciudadella, Spain, Tsunami June 15, 2006 : Slide 2

Tsunamigenic Phenomena

- Meteorological Tsunamis.



Ciudadella, Spain, Tsunami June 15, 2006 : Slide 3

Tsunamigenic Phenomena

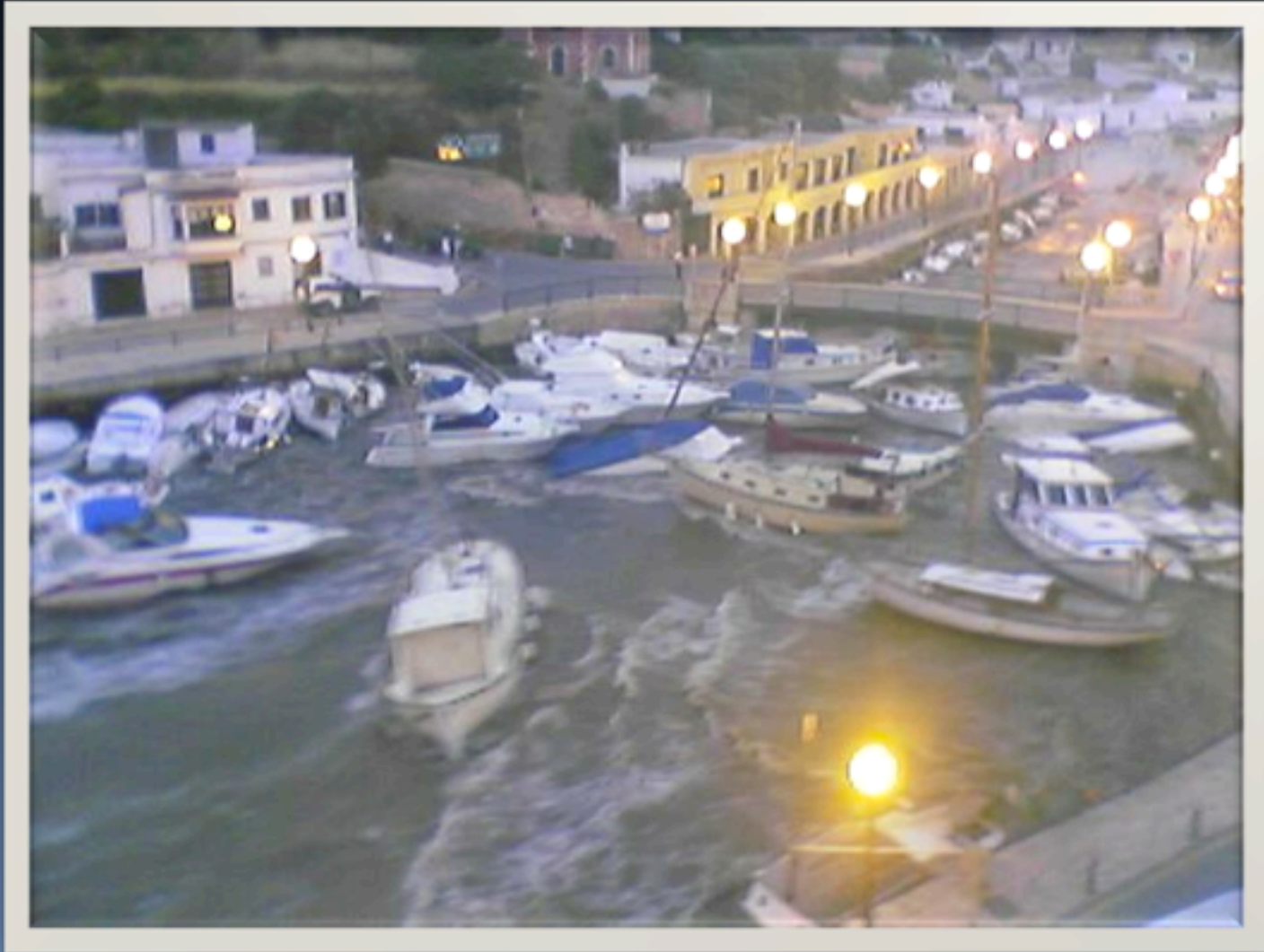
- Meteorological Tsunamis.



Ciudadella, Spain, Tsunami June 15, 2006 : Slide 4

Tsunamigenic Phenomena

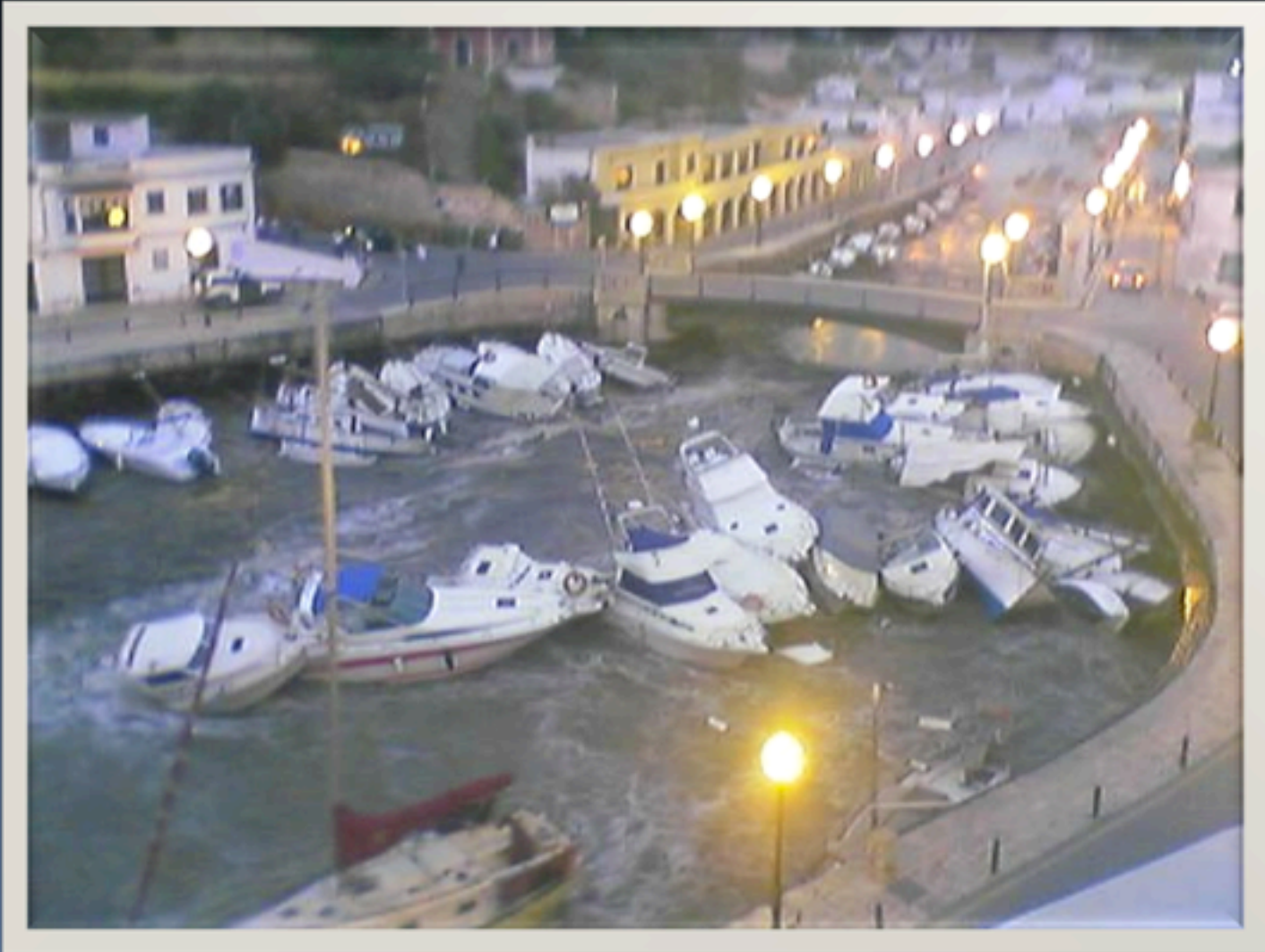
- Meteorological Tsunamis.



Ciudadella, Spain, Tsunami June 15, 2006 : Slide 5

Tsunamigenic Phenomena

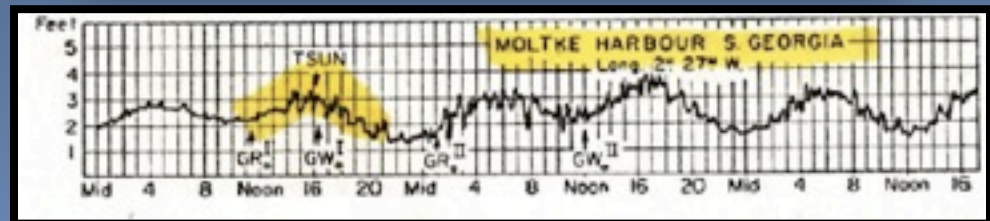
- Meteorological Tsunamis.



Ciudadella, Spain, Tsunami June 15, 2006 : Slide 6

Tsunamigenic Phenomena

- Tsunamis generated by volcanic explosions: Krakatoa, 1883
- They have the potential to generate a meteorological tsunami.



Tsunamigenic Phenomena

- Tsunamis generated by underwater land-slides: Lituya Bay, AK

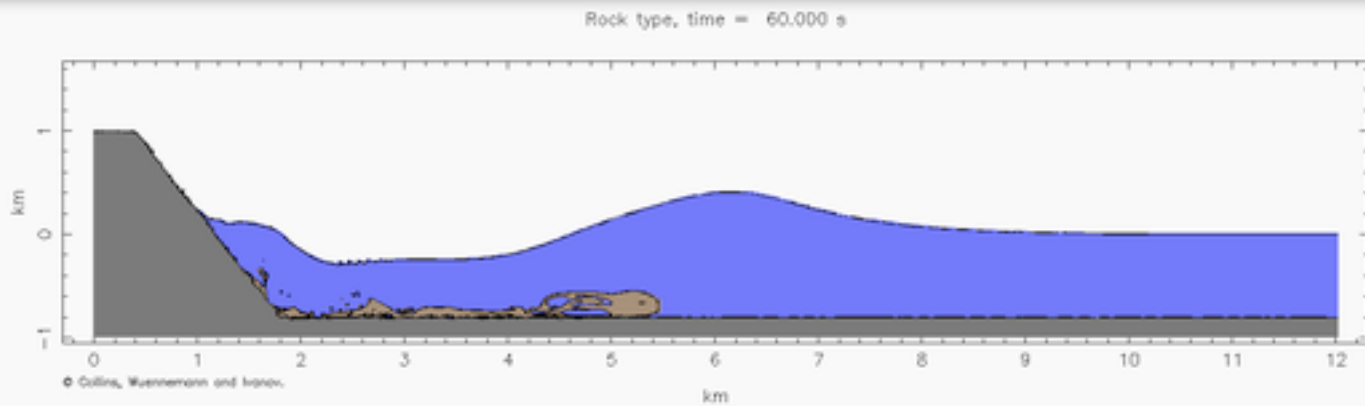
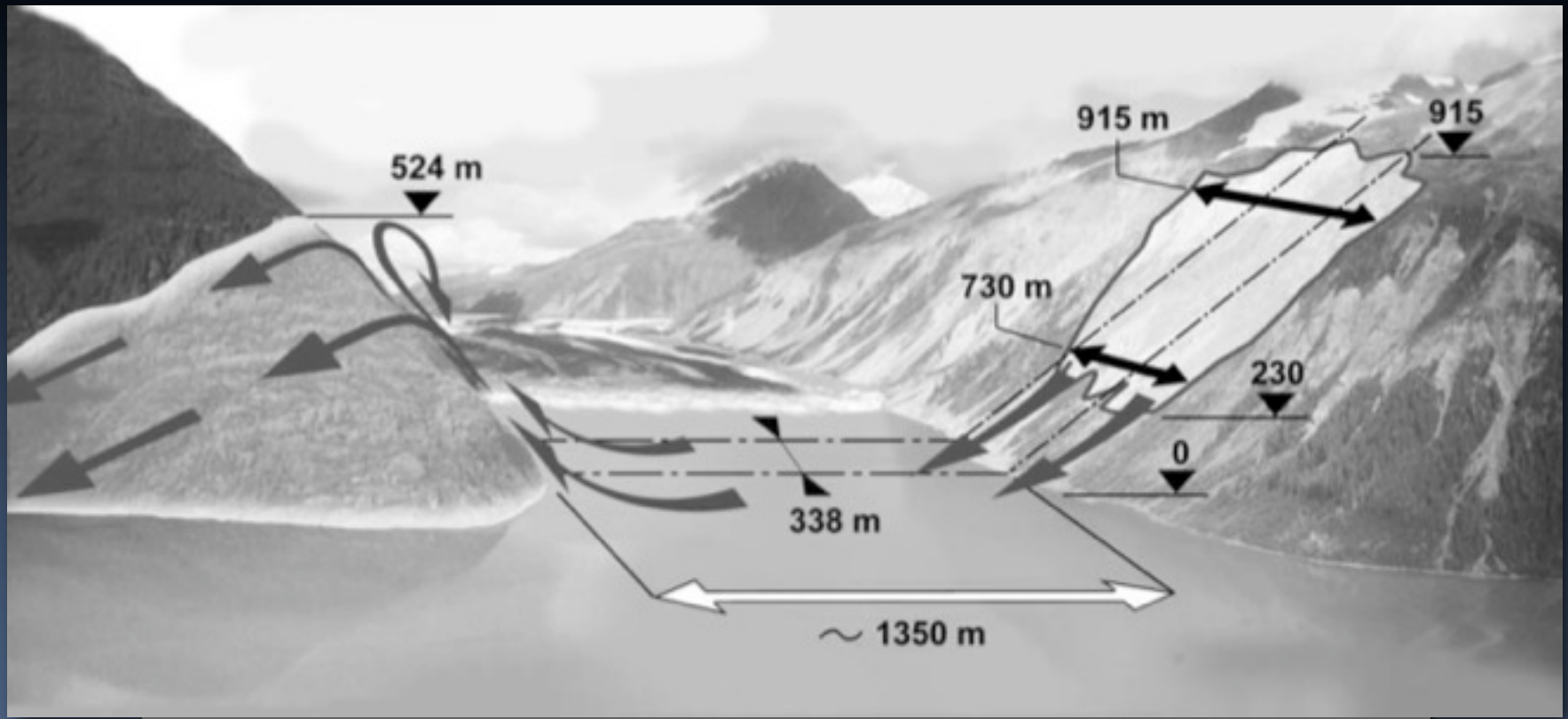


Tsunamigenic Phenomena

- Tsunamis generated by underwater land-slides: Lituya Bay, AK



Tsunamigenic Phenomena



Tsunamigenic Phenomena

- Tsunamis generated by underwater land-slides: Aisén, Chile.
- Slope failure.



Tsunamigenic Phenomena

- Tsunamis generated by underwater land-slides: Aisén, Chile.
- Visible scars.



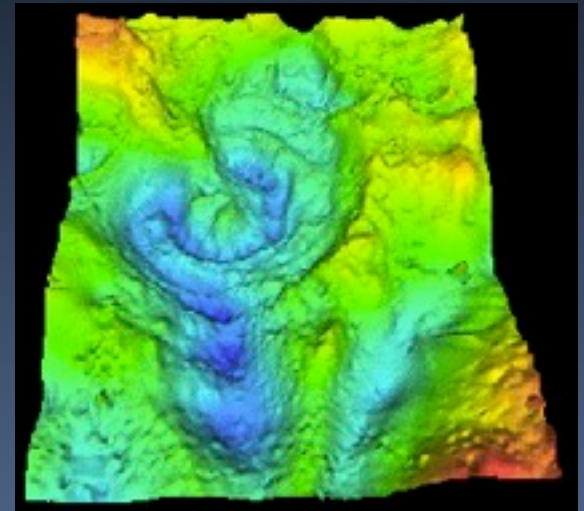
Tsunamigenic Phenomena

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- Inundation.



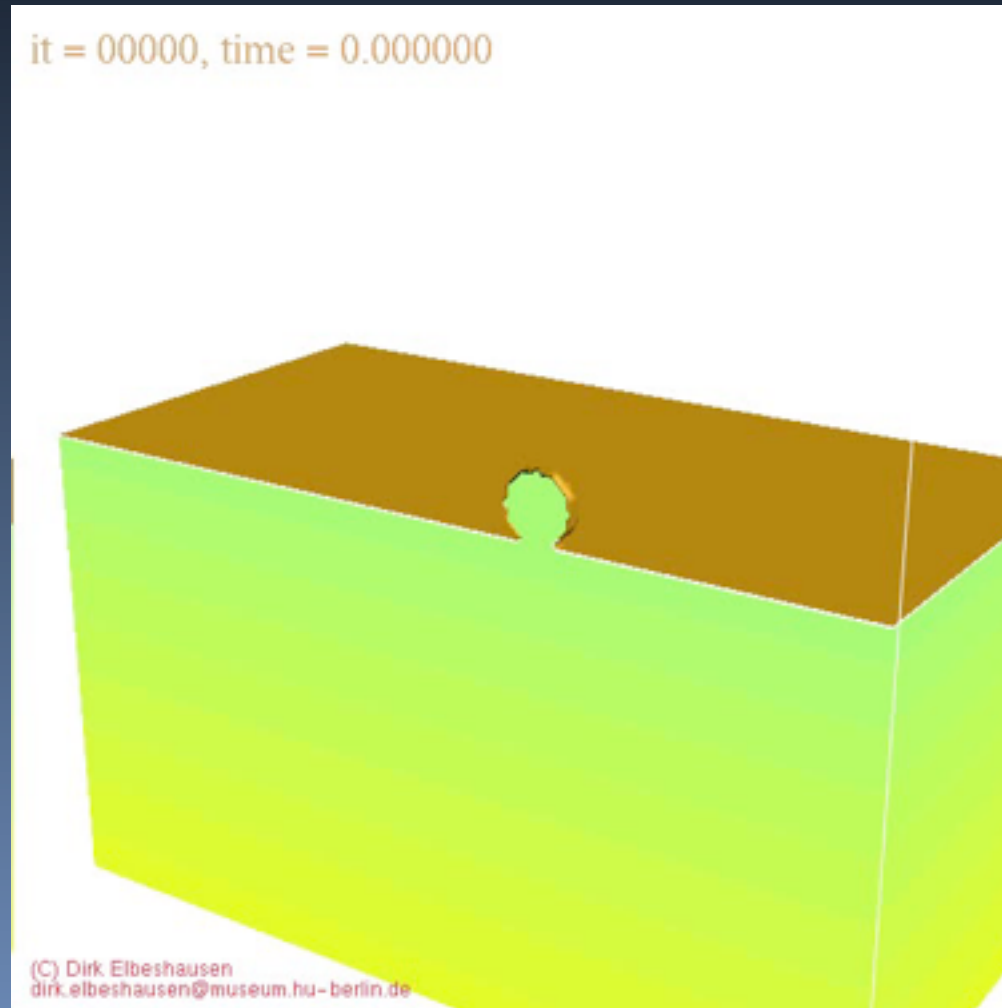
Tsunamigenic Phenomena

- Tsunamis meteorite impacts.



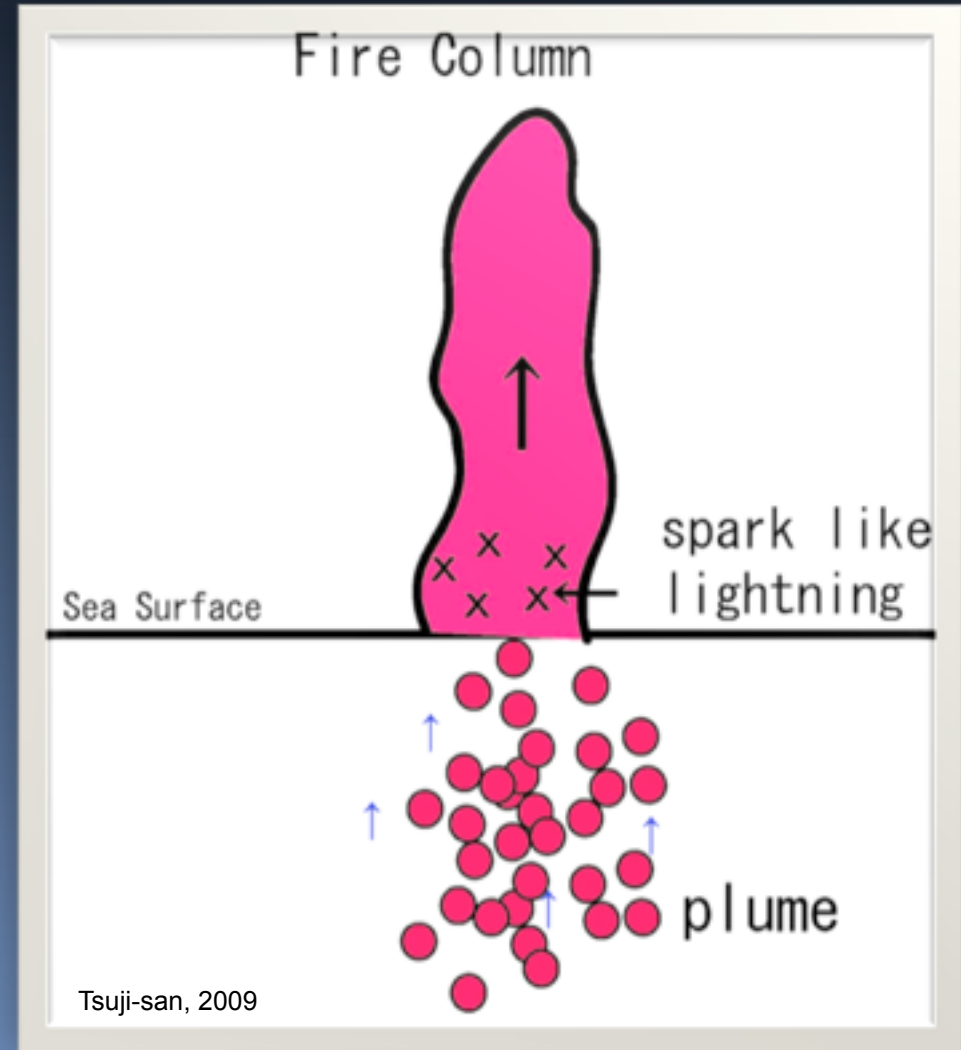
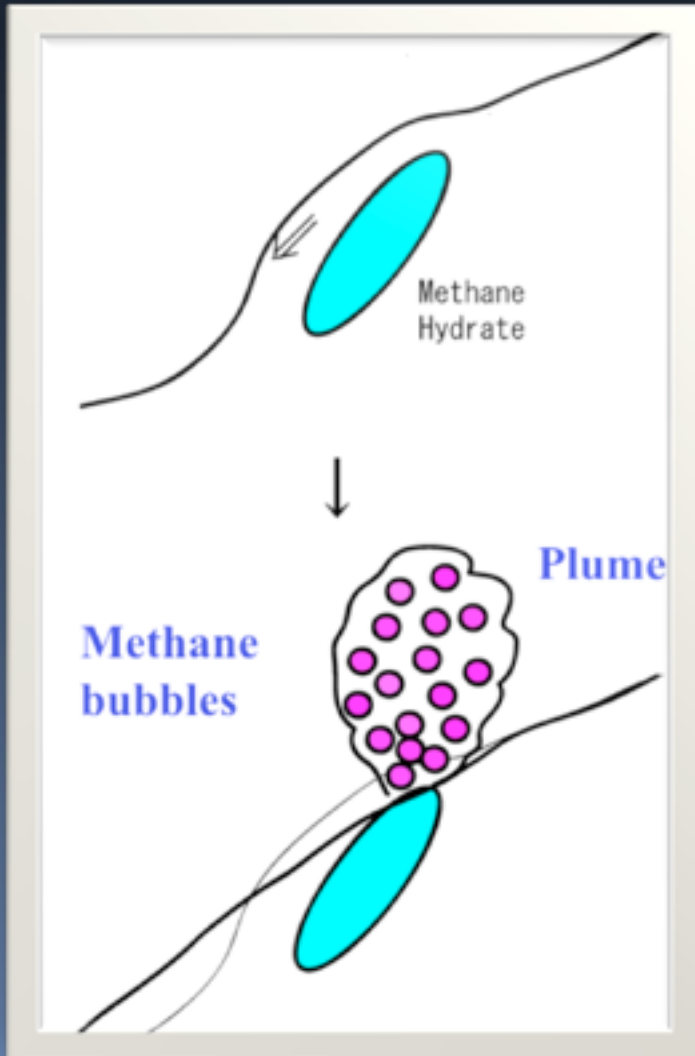
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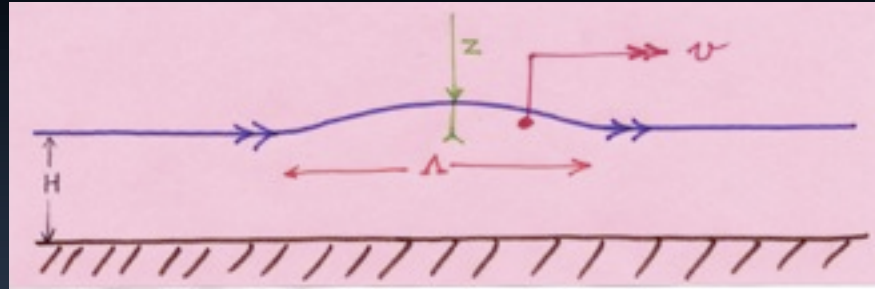


Tsunamigenic Phenomena

- Tsunamis generated by explosion of underwater methane deposits: Deep Water Horizon?



Physical Characteristics of a Tsunami in Deep Water



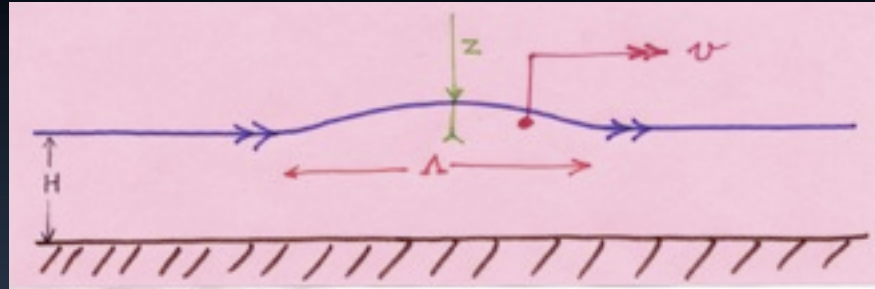
- Propagation Speed: Speed depends on ocean depth, H .

$$v = \sqrt{gH}$$

In practice: $H=5$ Km, $v=220$ m/s (~ 800 Km/h)
(approximate cruise velocity of a commercial airliner)

- Maximum Amplitude, z : from a few centimeters to a half meter.
- Typical Wavelength: $\lambda = 300$ km (period ~ 600 s-3000s)
- A tsunami is always composed of several waves.

Physical Characteristics of a Tsunami in Deep Water



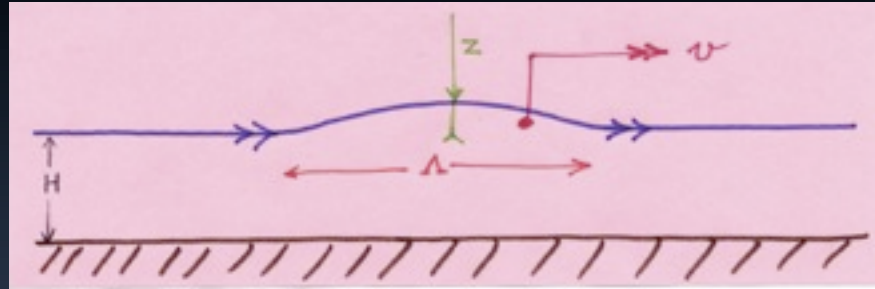
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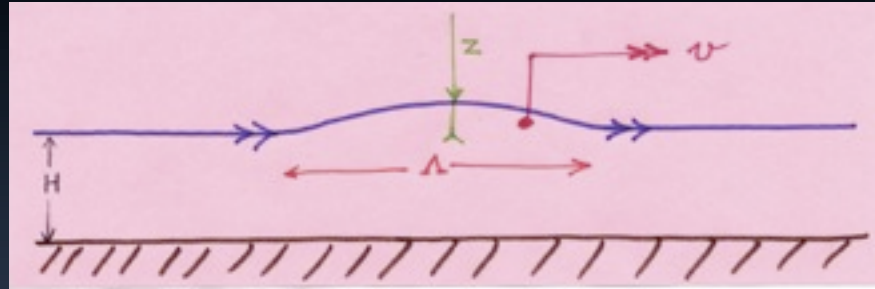
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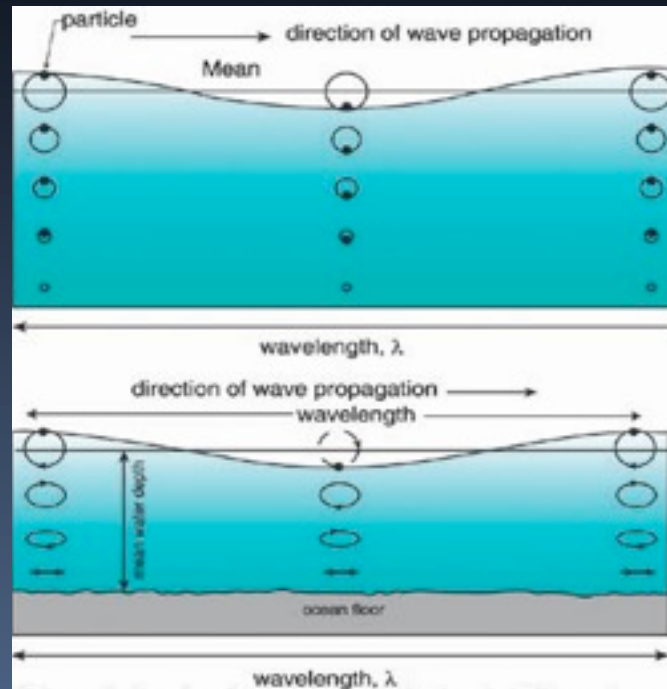
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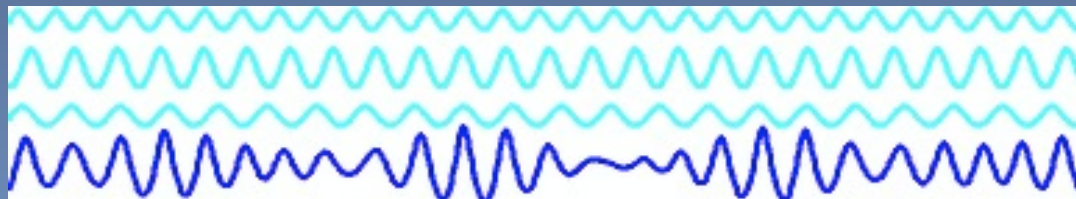
- A tsunami is always a long wave (alt. A wave in shallow water).



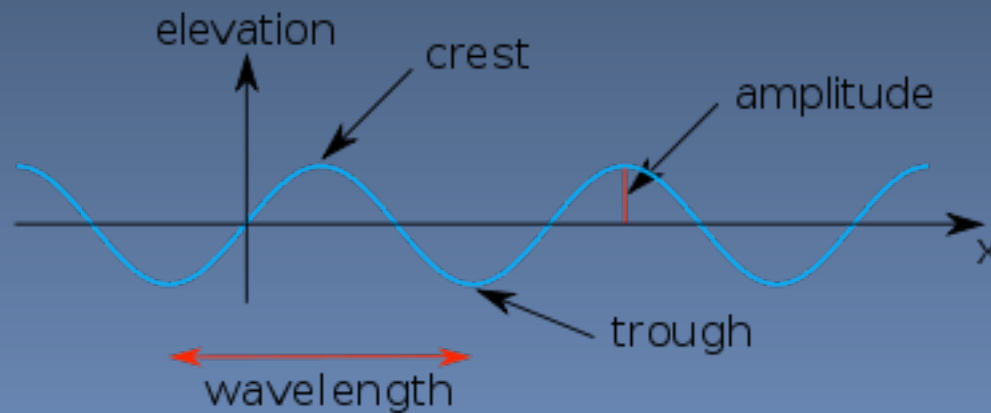
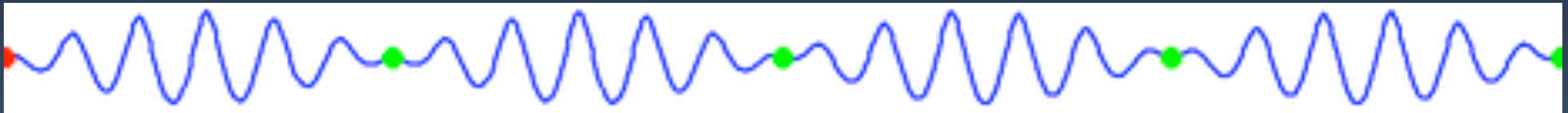
- A tsunami is a non-dispersive wave.

$$c = \frac{\omega}{k} = \sqrt{\frac{g \times \tanh(kH)}{k}}$$

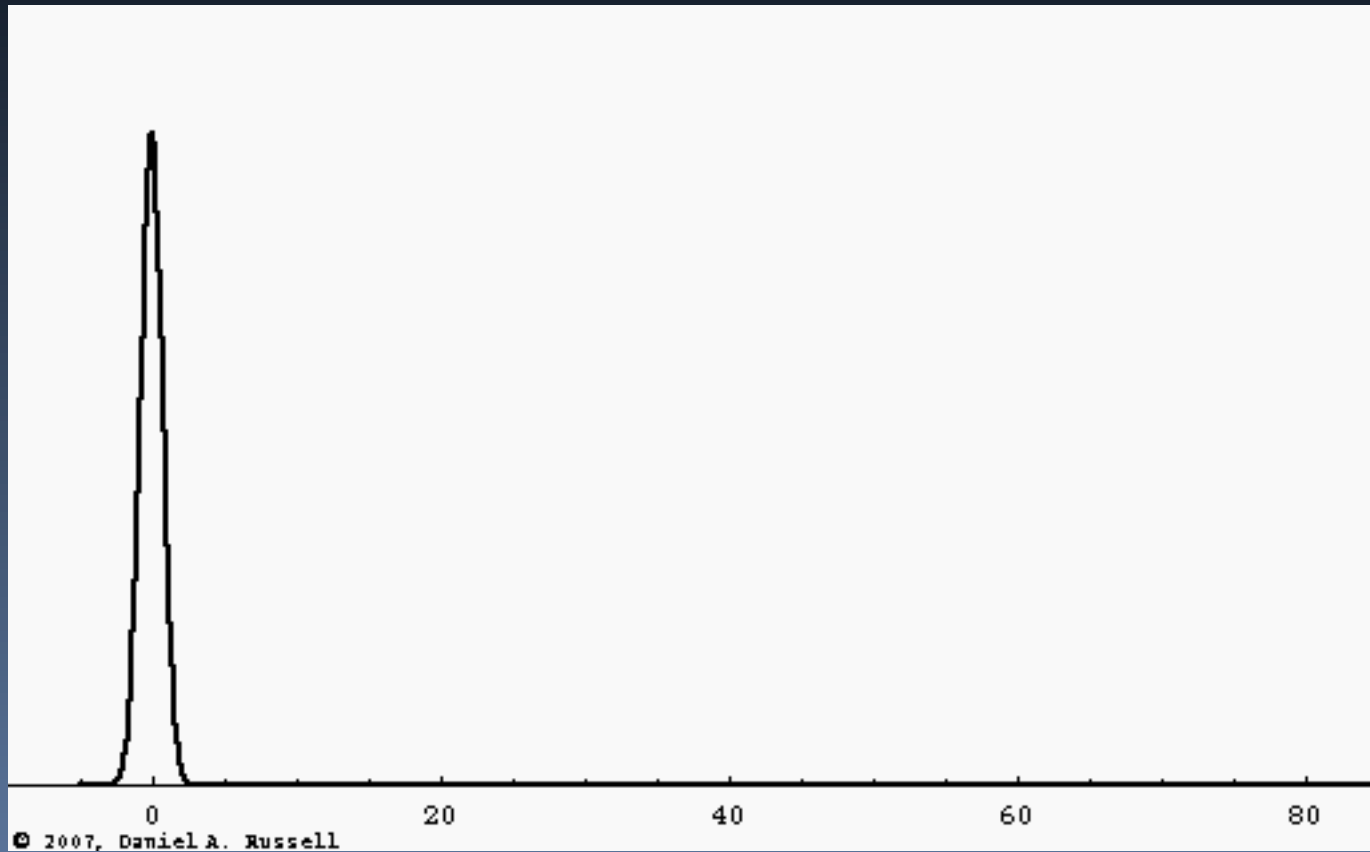
Example of dispersive wave behavior



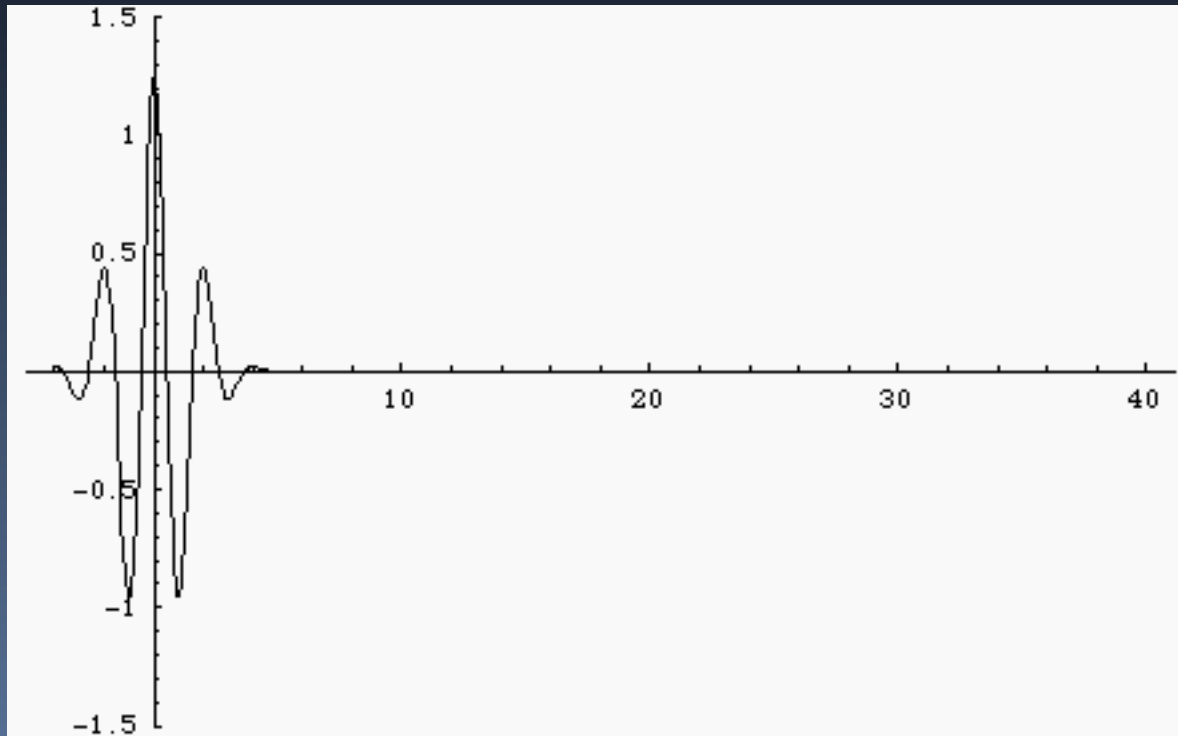
Wave Dispersion, cont'd



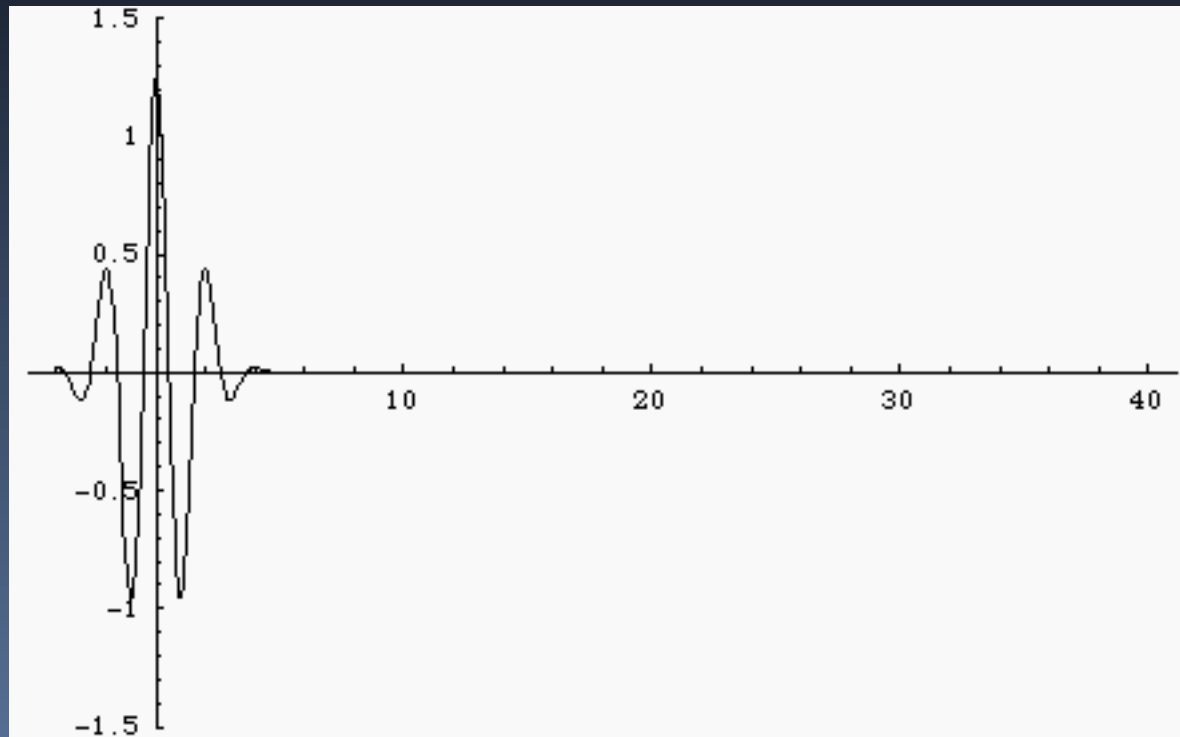
Wave Dispersion, cont'd



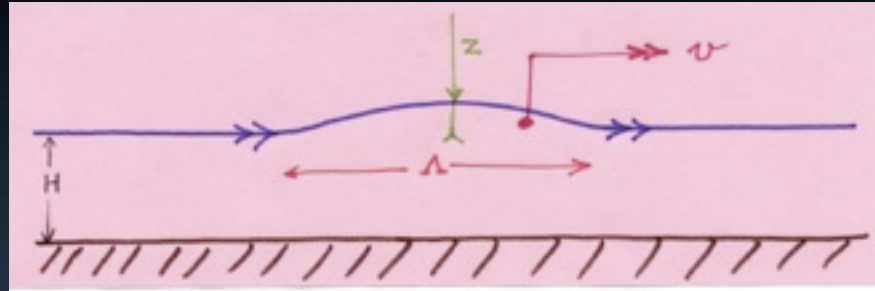
Wave Dispersion, cont'd



Wave Dispersion, cont'd



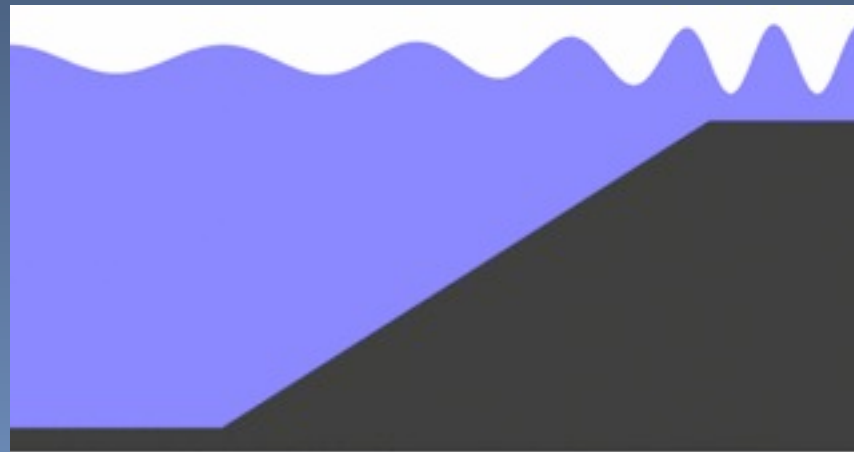
Physical Characteristics of a Tsunami in Shallow Water



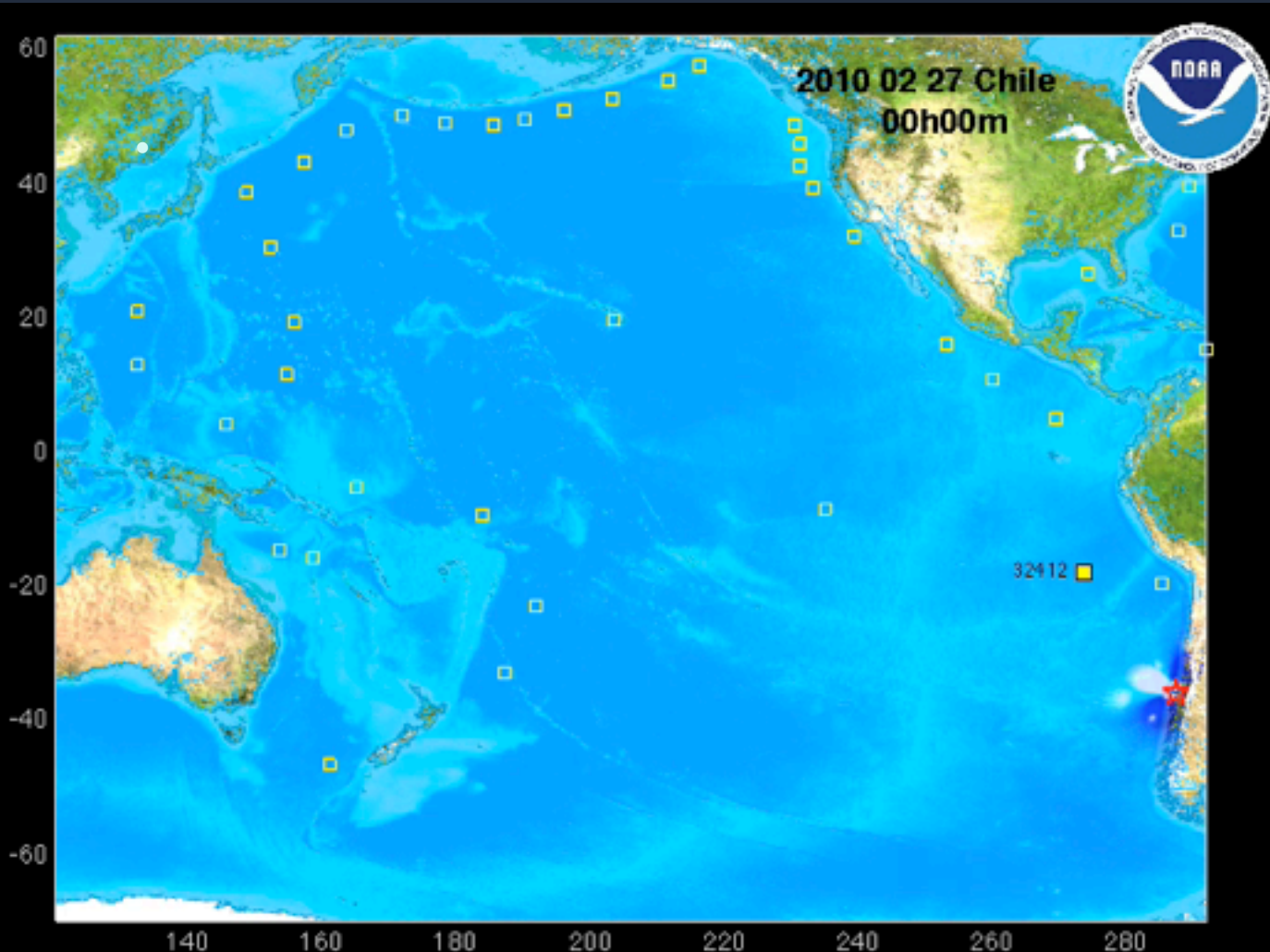
- Propagation Speed: Speed depends on ocean depth, H.

$$v = \sqrt{gH}$$

- The leading part of the wave slows down as it enters shallow waters, the trailing part of the wave is still in deep water and moving faster than the leading part. This causes the wave height to increase and the wavelength to shorten.

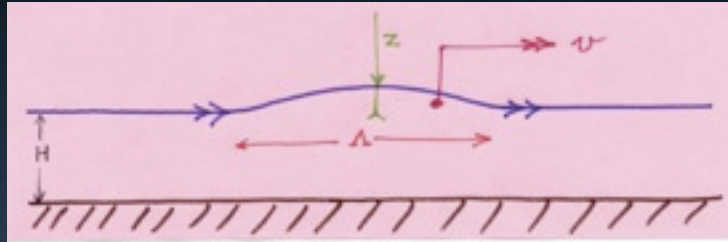


Refraction: waves bend when they go through a slower medium



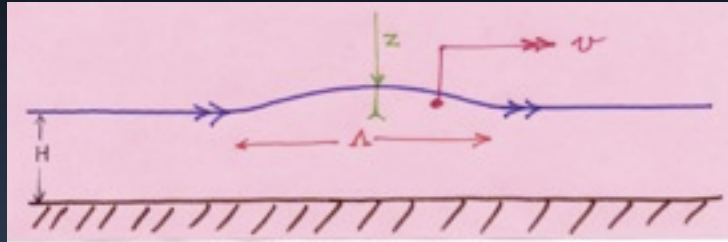
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Physical Characteristics of a Tsunami in Shallow Water.



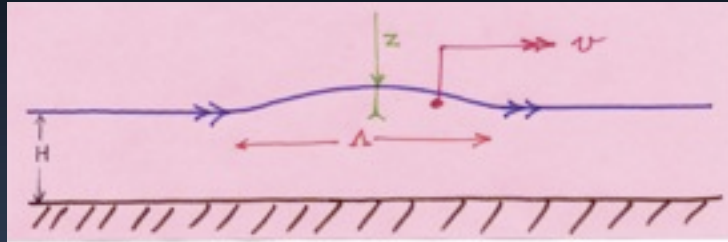
- Tsunami wave heights in shallow water can reach tens of meters.
- Typical wavelengths will range between 10-20 Km.
- The size of the tsunami wavelength makes it much more destructive than storm waves.

Physical Characteristics of a Tsunami in Shallow Water.



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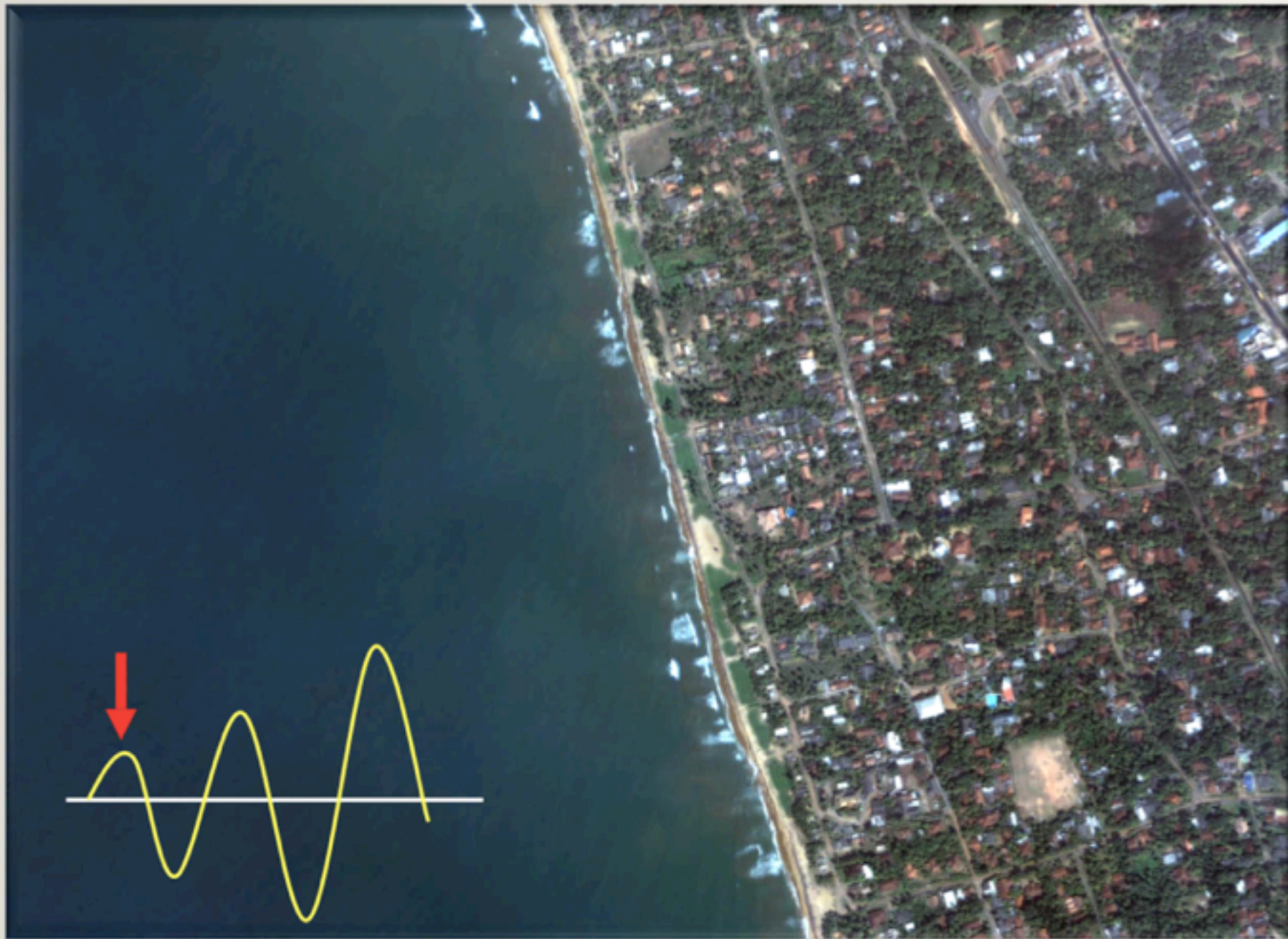


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Kalutara, Sri Lanka, 2004

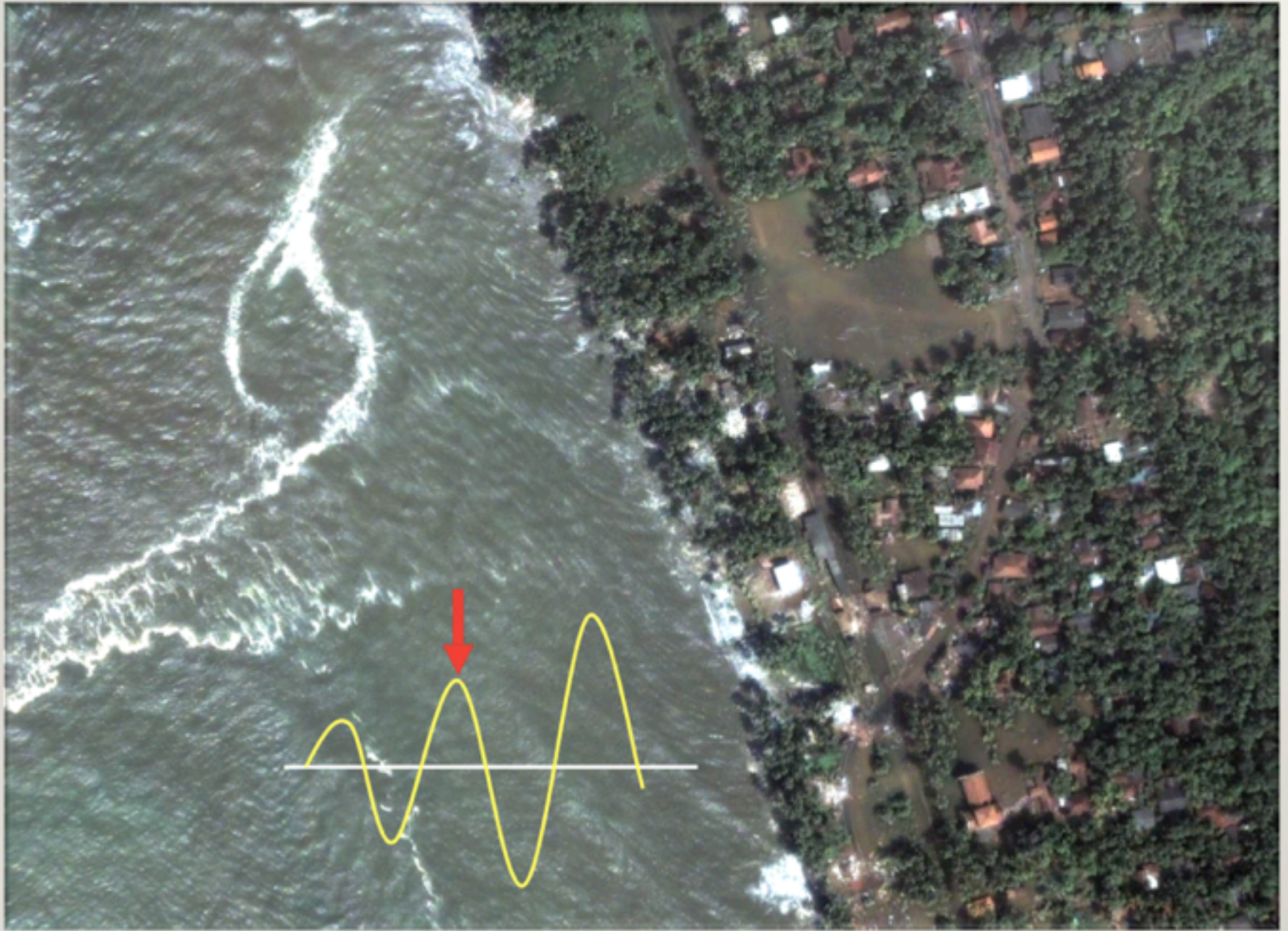
Quickbird satellite







Wednesday, November 28, 2012



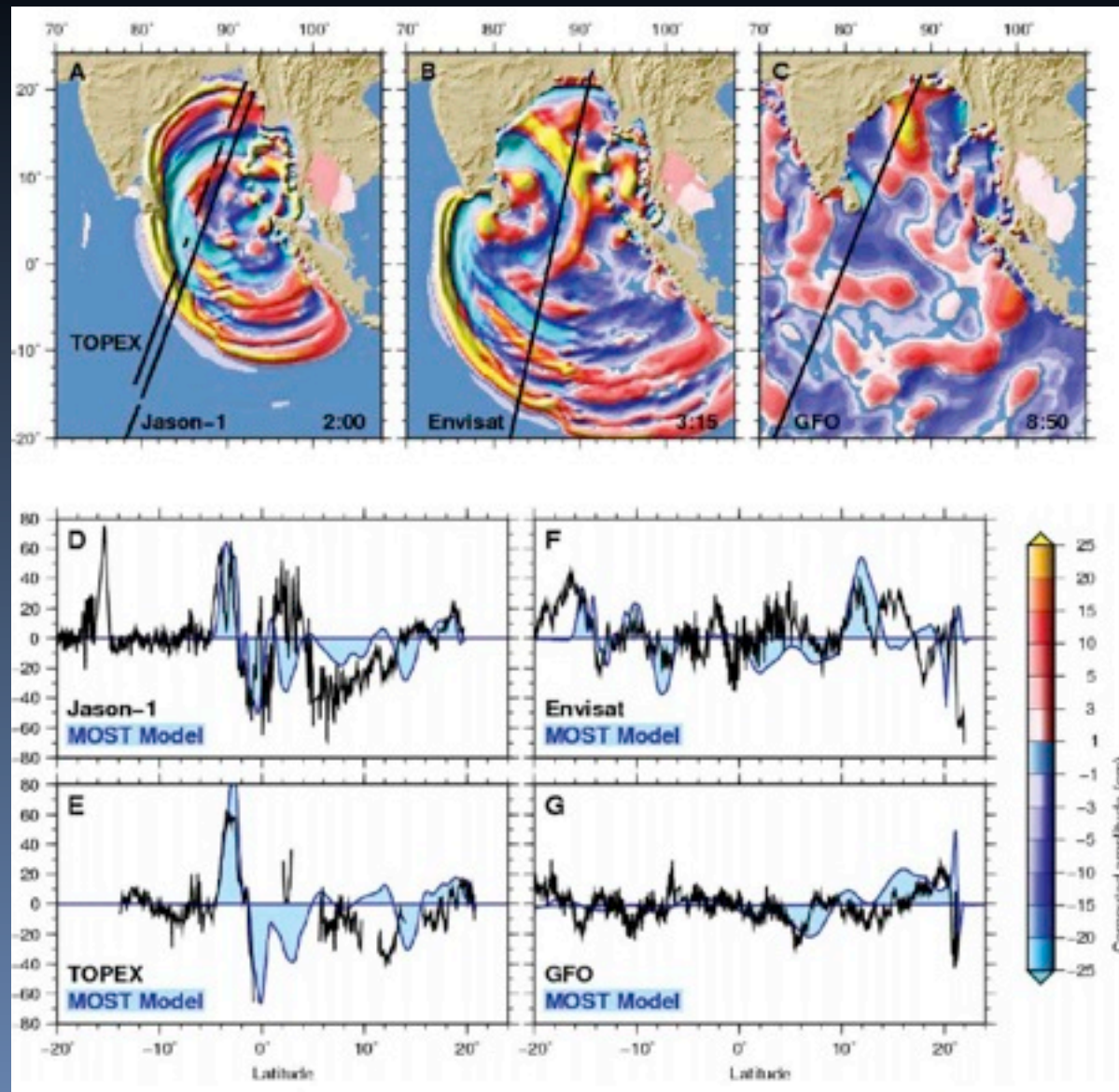




What can we do about forecasting Tsunamis?

- Deploy Detection Hardware.
- Develop algorithms to interpret in-coming data.
- Develop numerical models to forecast/assess tsunami impact on the coast.

Tsunami Inversion based on satellite altimetry . Sumatra 2004 tsunami



Tsunami Warning Systems: DART Systems



D.A.R.T. II

**Deep ocean
Assessment and
Reporting of
Tsunamis**

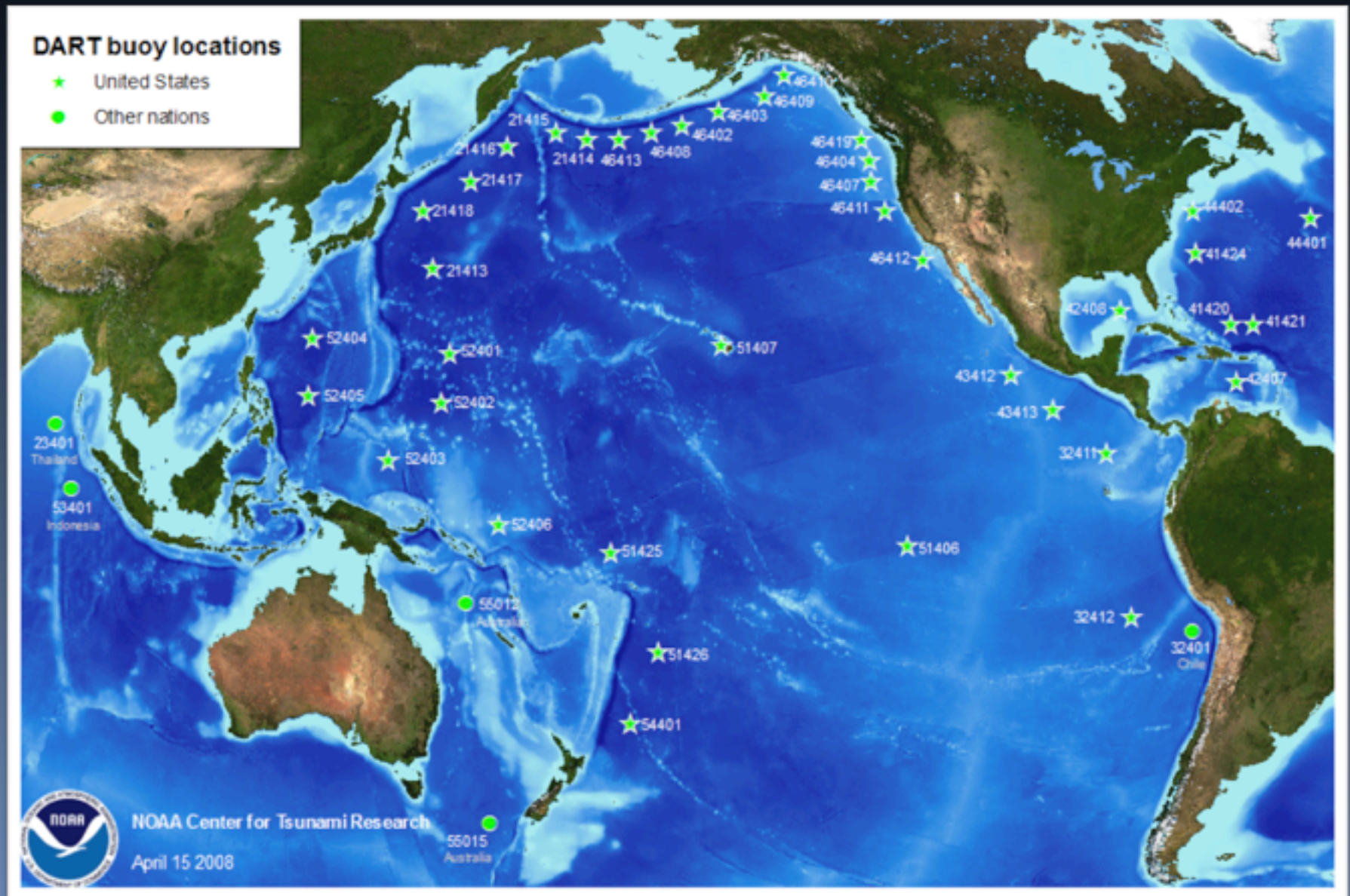
Tsunami Warning Centers



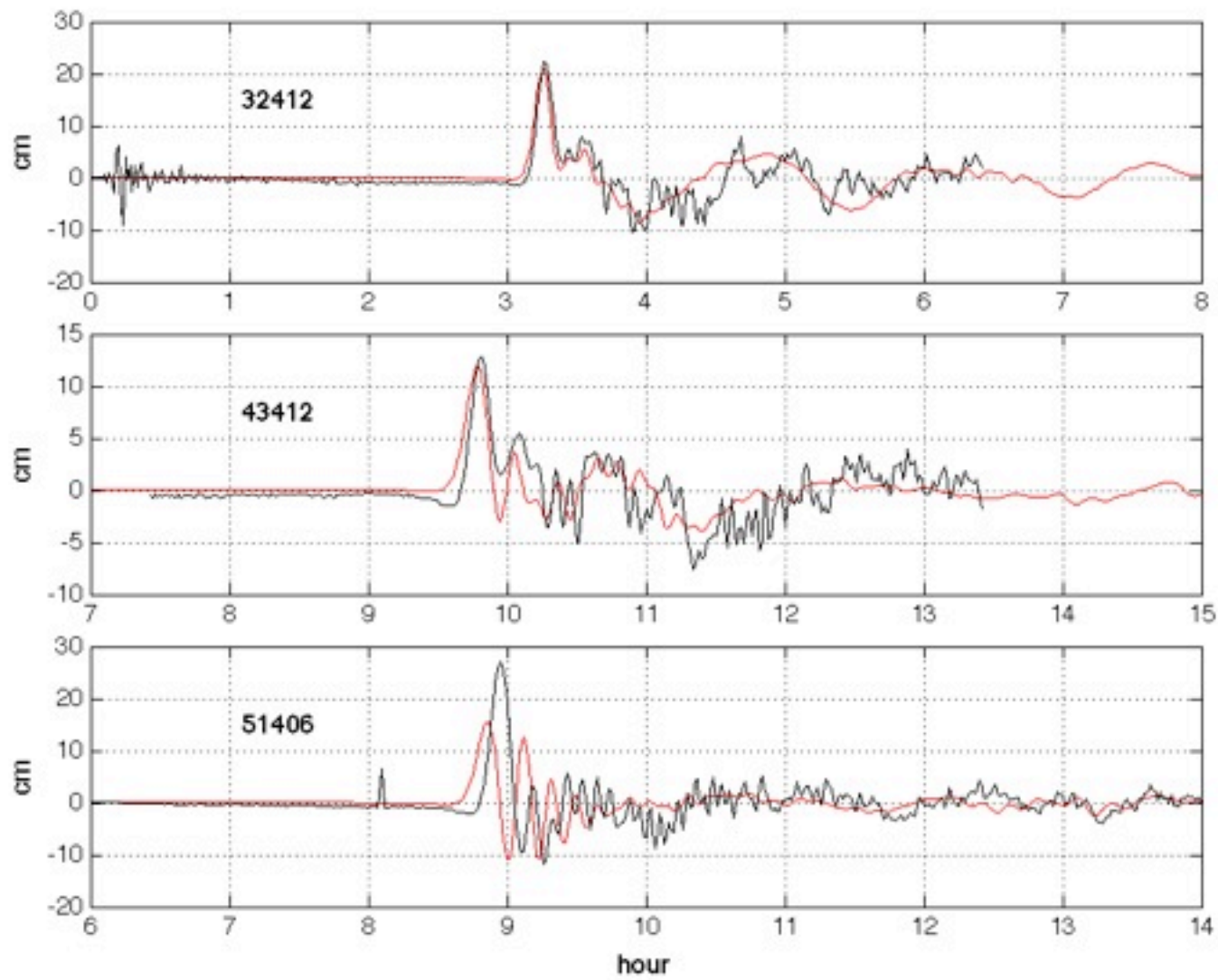
WCATWC (AK)
PMEL (WA)

PTWC (HI)
NDBC (MS)

Dart Stations Position



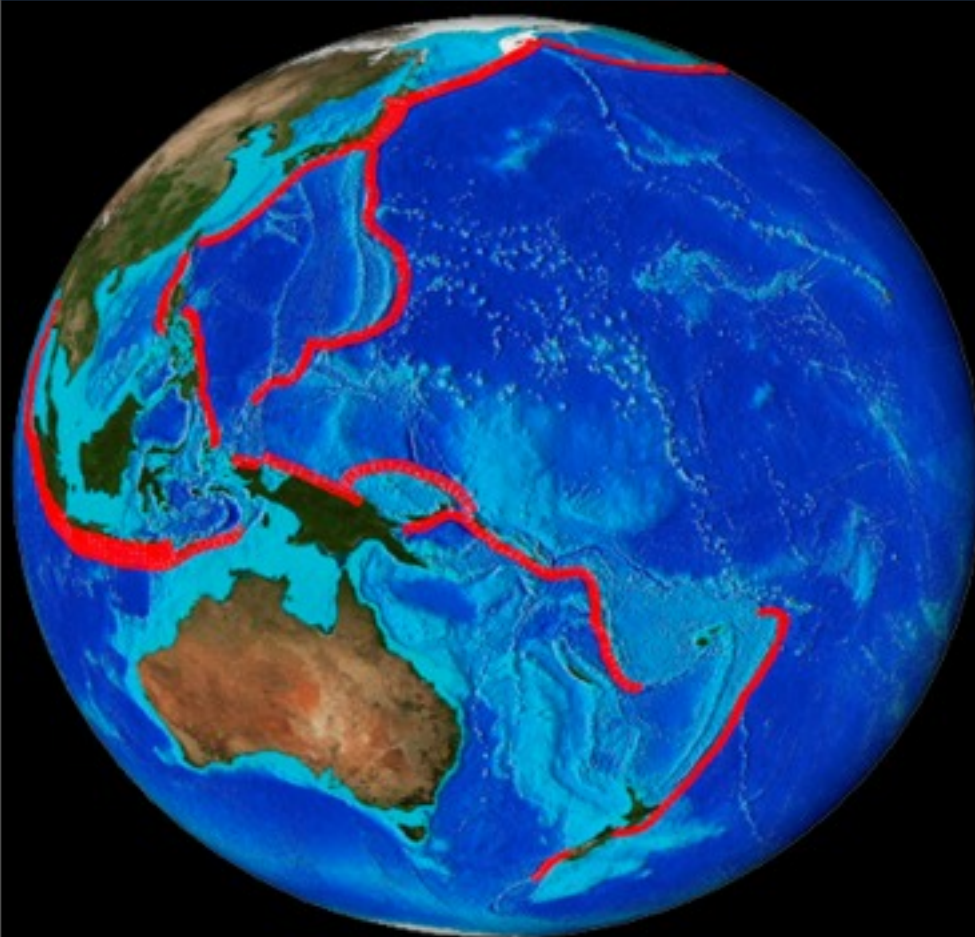
DART time series Chile 2010 tsunami



- What do we constrain with the deep-water DART measurement?

Our deep-water propagation
model run database...

Locations of the unit sources for pre-computed tsunami events.

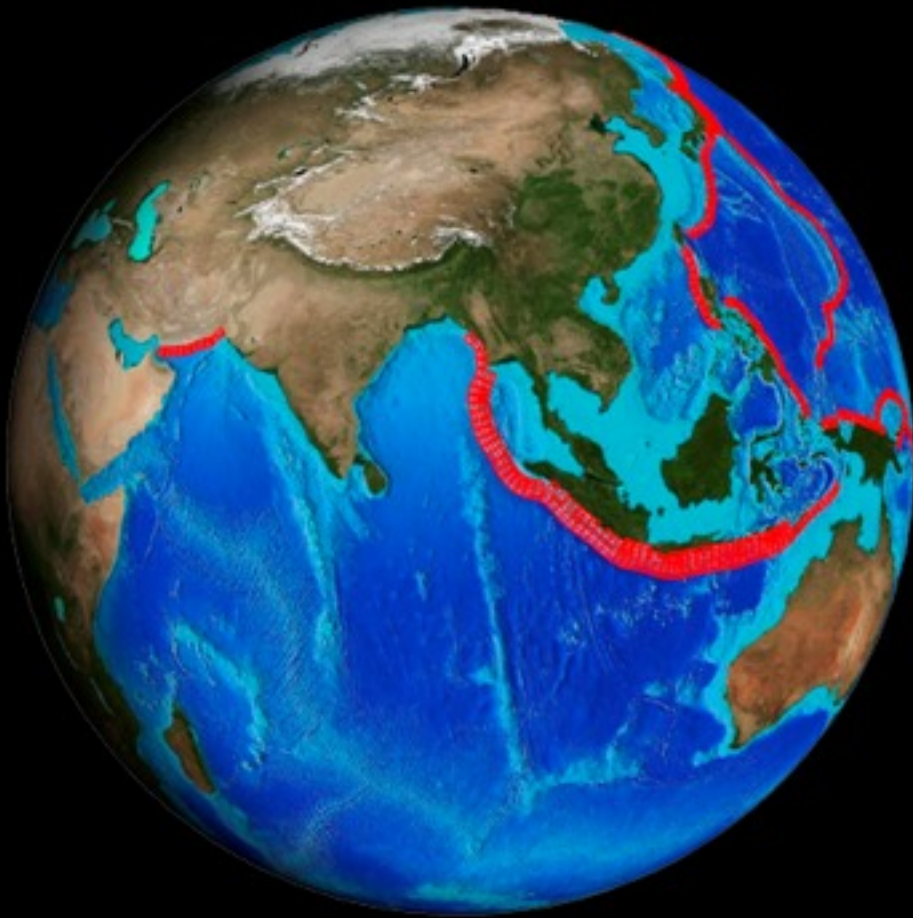


West Pacific



East Pacific

Locations of the unit sources for pre-computed tsunami events.



Indian Ocean



Atlantic Ocean

- Why can we just add arbitrary pre-run models together during a forecast?

Any combination of solutions to the linear equations of motion is also a solution:

Linearity...

Characteristic Form of the Non-linear Shallow Water Equations.

$$\left\{ \begin{array}{l} h_t + (uh)_x = 0 \\ u_t + uu_x + gh_x = gd_x \\ v_t + uv_x = 0 \end{array} \right\} \quad \longrightarrow \quad \left\{ \begin{array}{l} p_1 + \lambda_1 p_x = gd_x \\ q_1 + \lambda_2 q_x = gd_x \\ v'_1 + \lambda_3 v'_x = 0 \end{array} \right.$$

Riemann invariants

$$\left\{ \begin{array}{l} p = u + 2\sqrt{gh} \\ q = u - 2\sqrt{gh} \\ v' = v \end{array} \right.$$

Eigenvalues

$$\left\{ \begin{array}{l} \lambda_1 = u + \sqrt{gd} \\ \lambda_2 = u - \sqrt{gd} \\ \lambda_3 = u \end{array} \right.$$

In deep water the equations are linear!!
We can do propagation database!!

Deep-Water Linearity

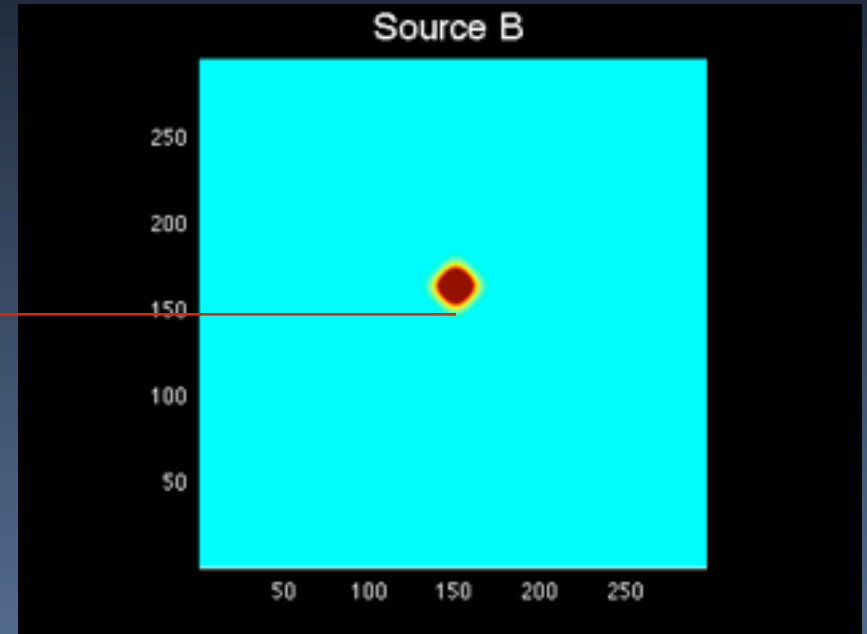
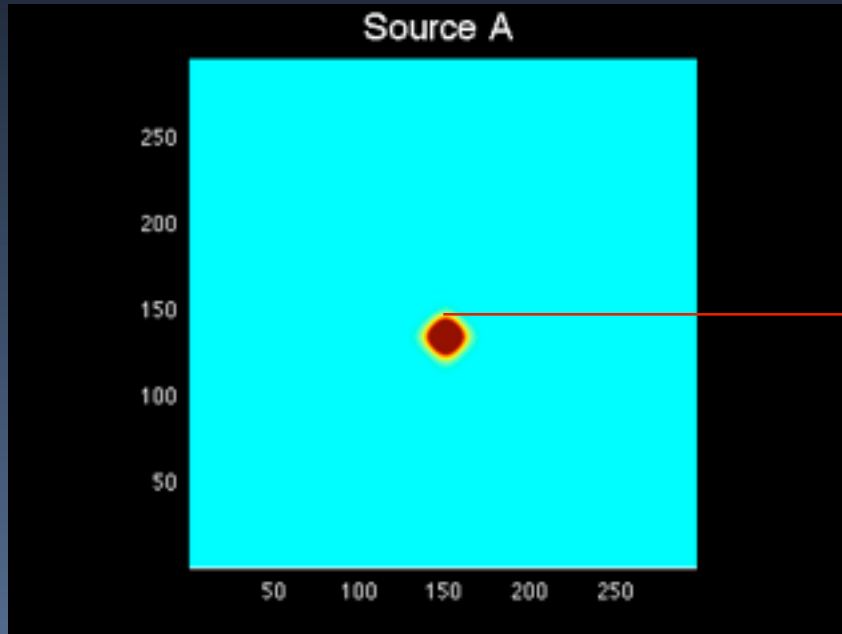


Illustration of Deep Water Linearity

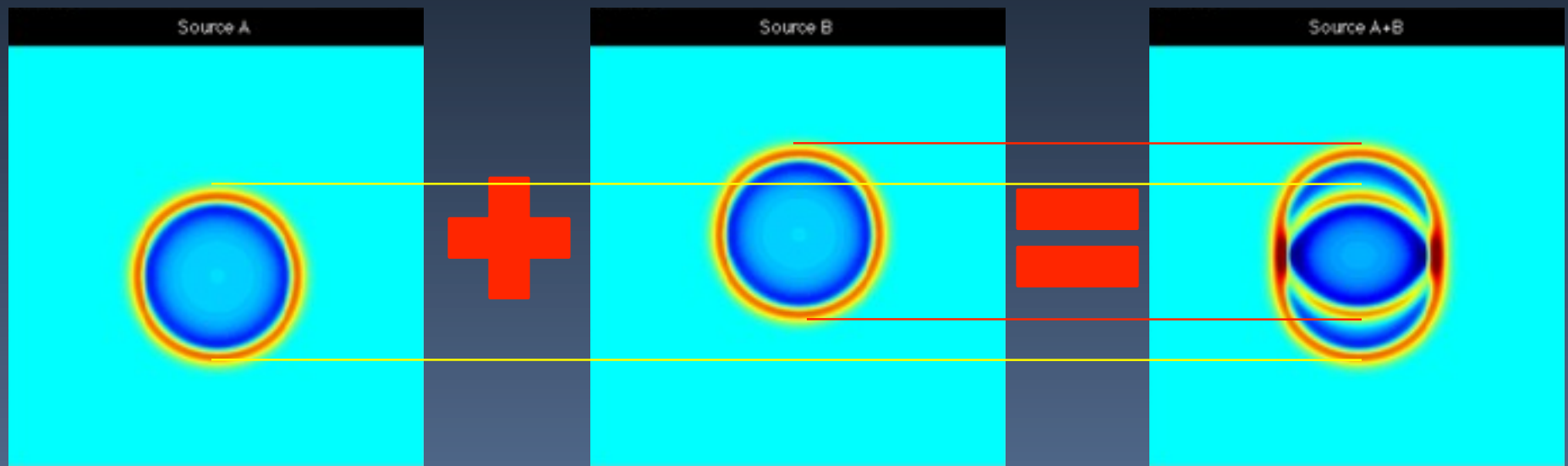
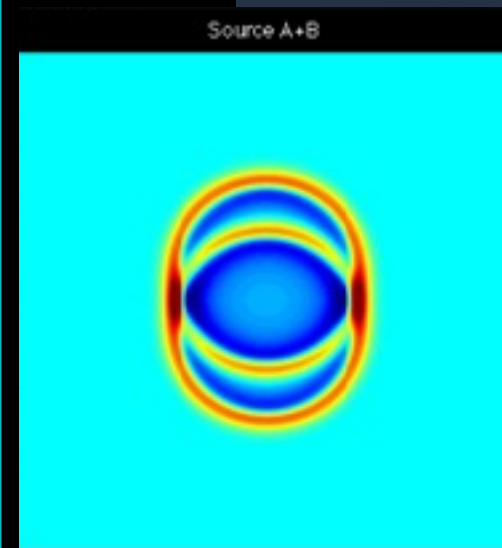
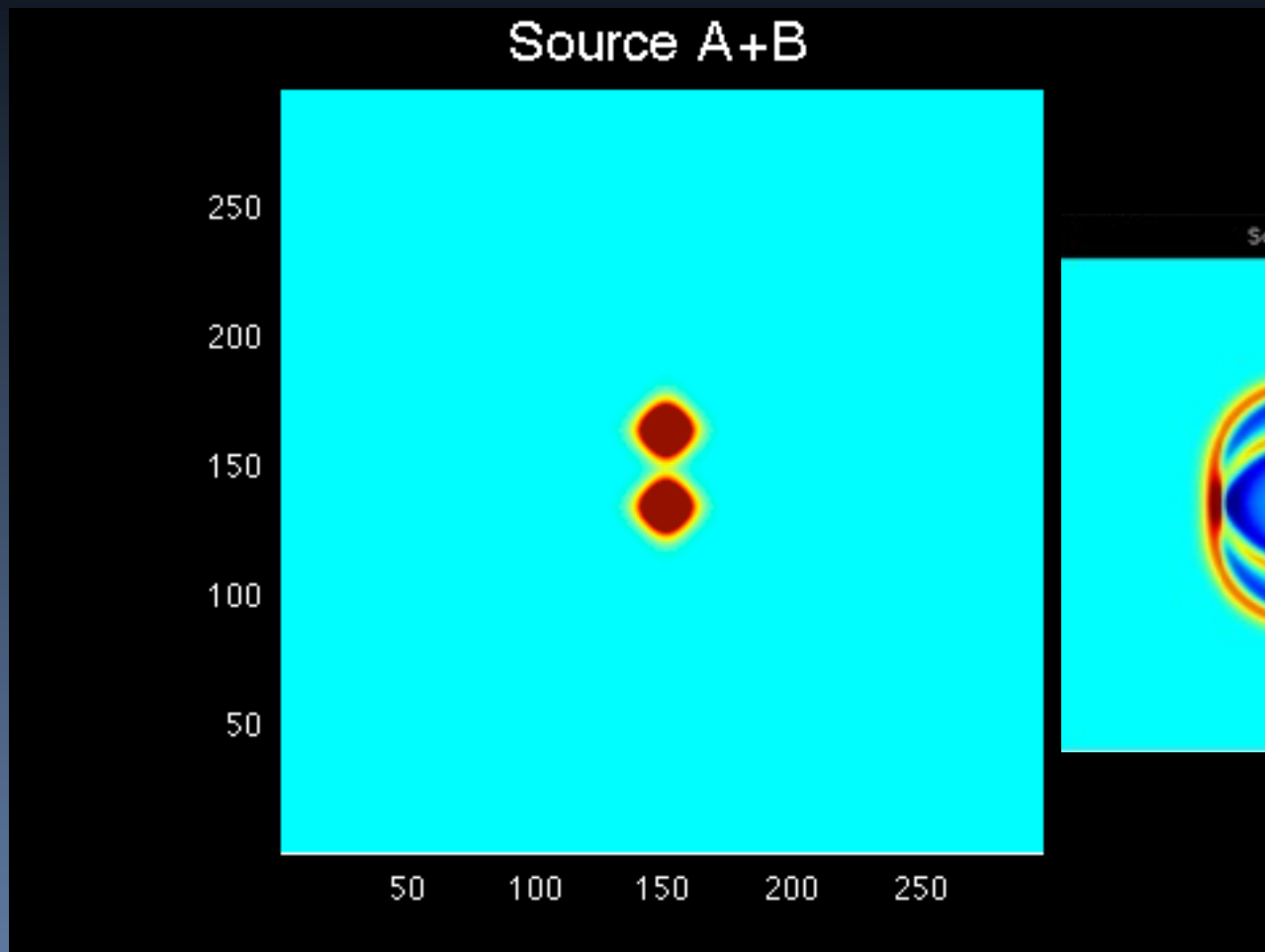
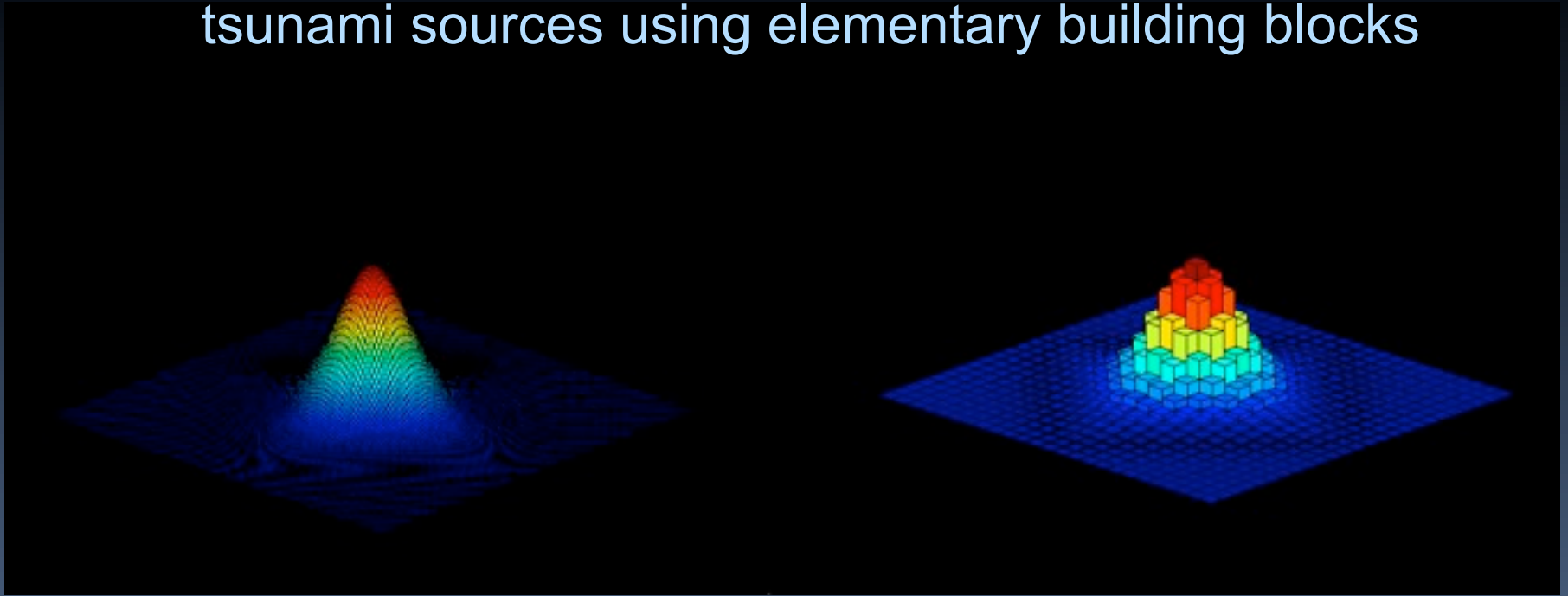


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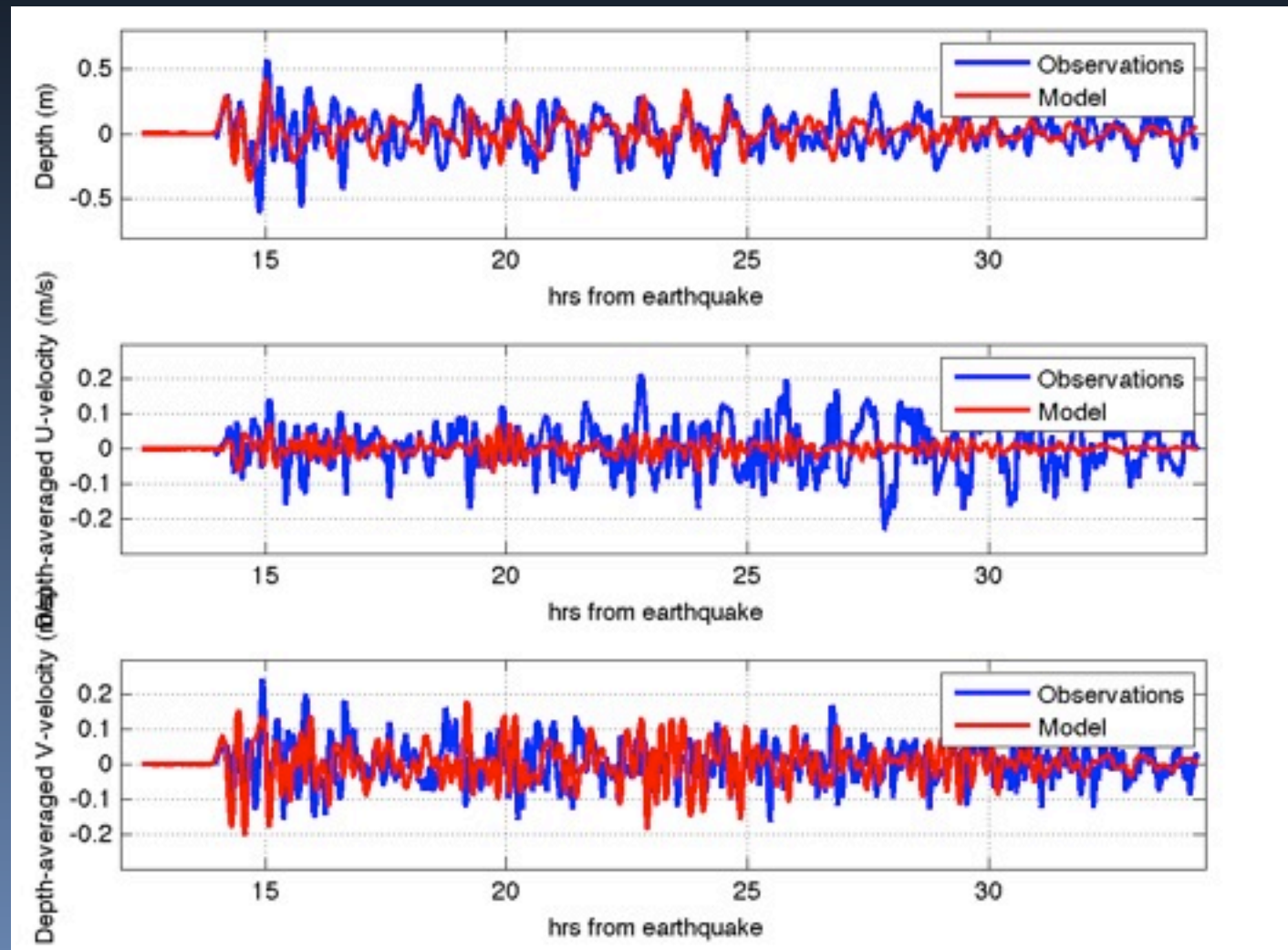


Linearity allows for the reconstruction of an arbitrary tsunami sources using elementary building blocks



For linearity $u \ll gh$

$$\sqrt{0.1^2 + 0.1^2} \ll \sqrt{9.8 \times 10}$$



- We know the deep-water tsunami obeys linear equations of motion
- We have many, many pre-run deep-water model runs in a “Propagation Database”

How do we produce the right combination during an event?

Inversion

- WebSIFT demo
- <http://sift.pmel.noaa.gov/websift>

Break

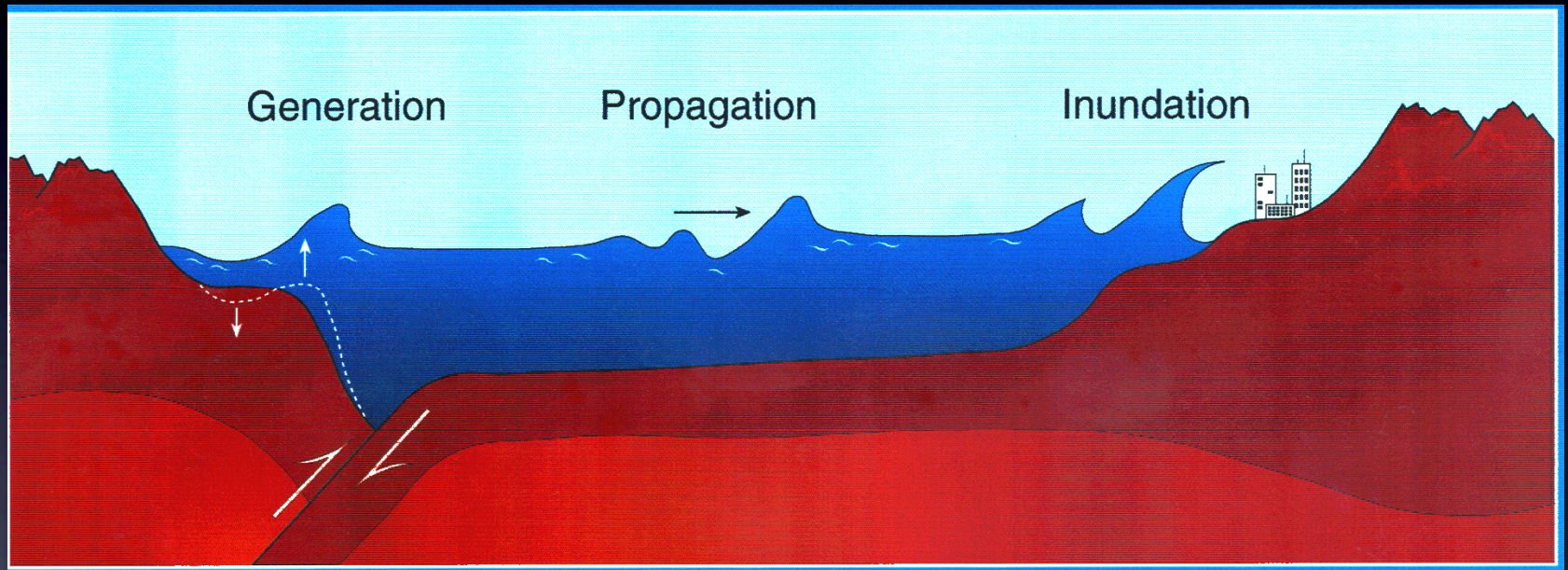
- Now we have the “best-fit” deep-water propagation run...
- How do we get the solution to the harbor?

Inundation...

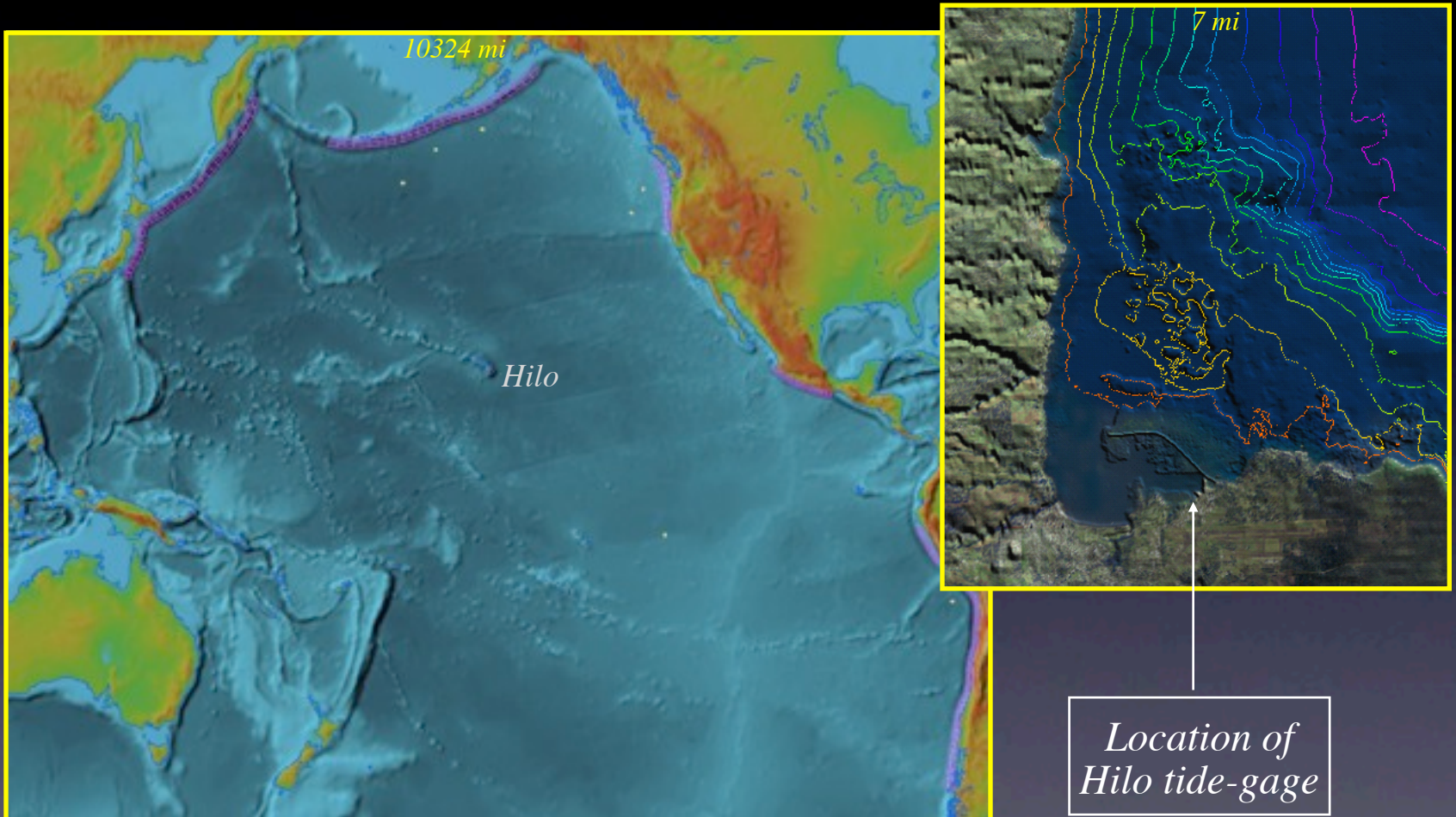
Inundation: 3 telescoping grids

- 3 nested grids used to model the shoaling wave evolution from deep-water to shallow bay, harbor, or coastline
- optimized to run quickly
- takes forcing from linearly-combined, pre-run Propagation model output

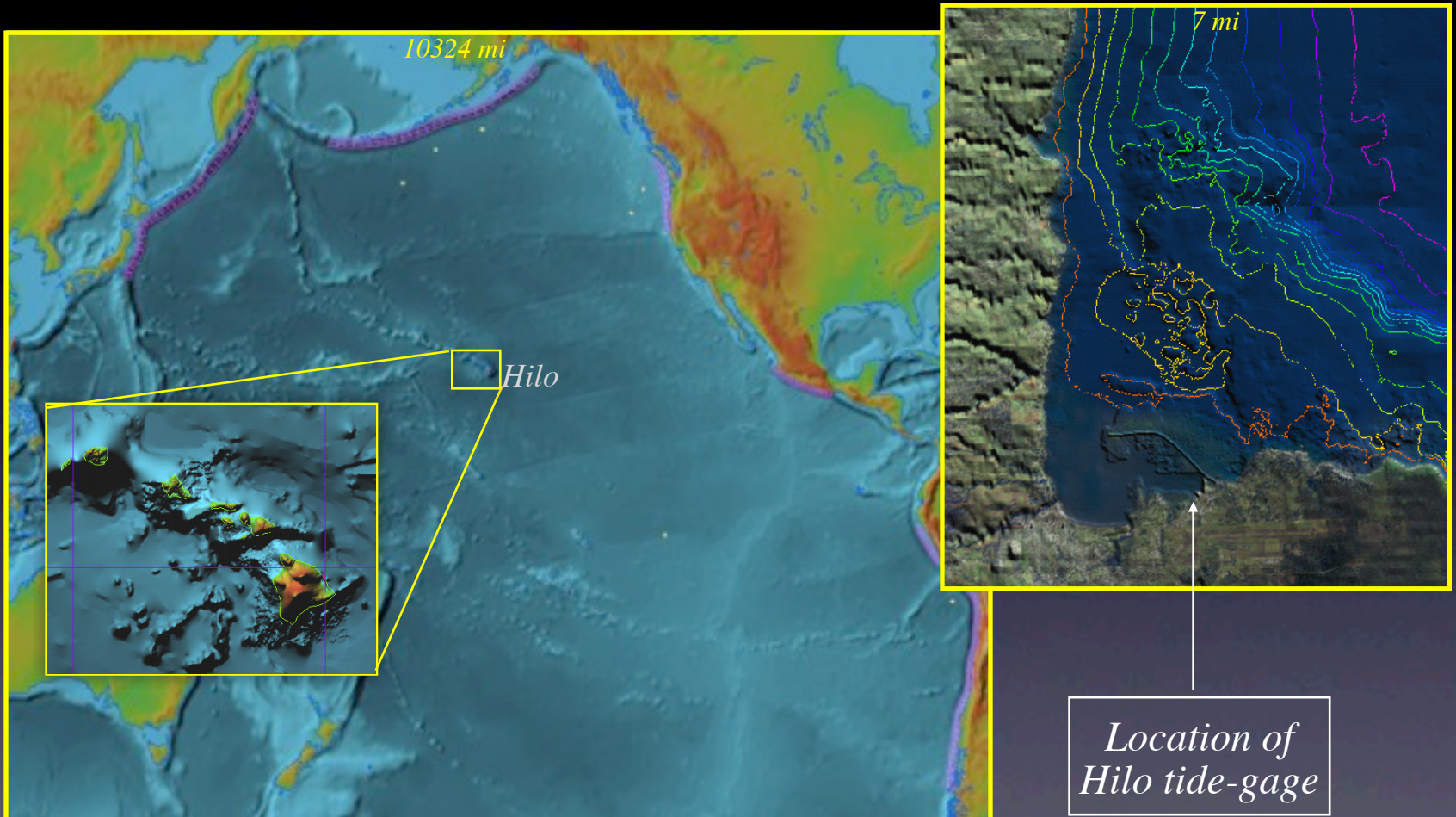
Why model separately?



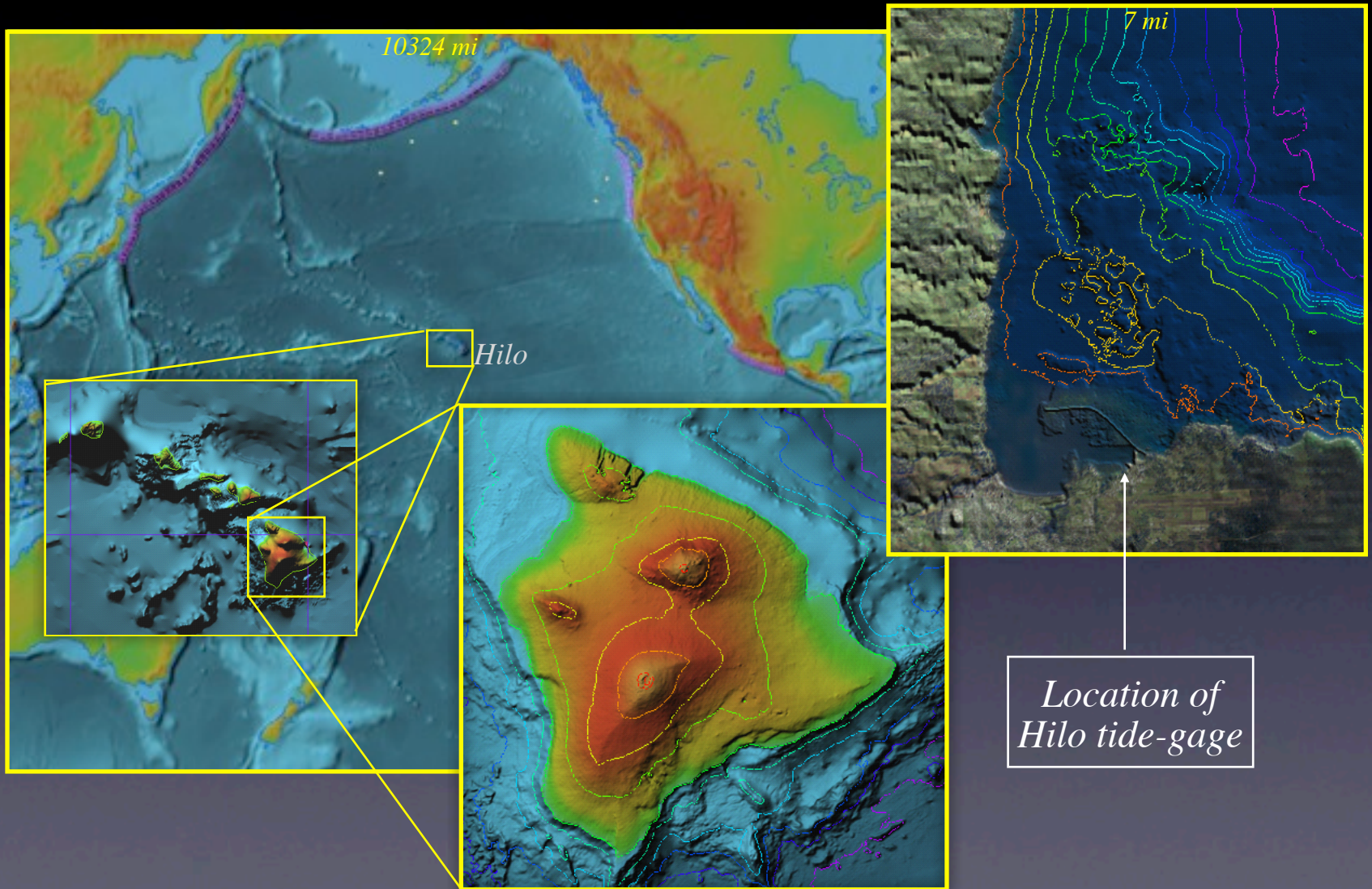
Reason I : Different scales



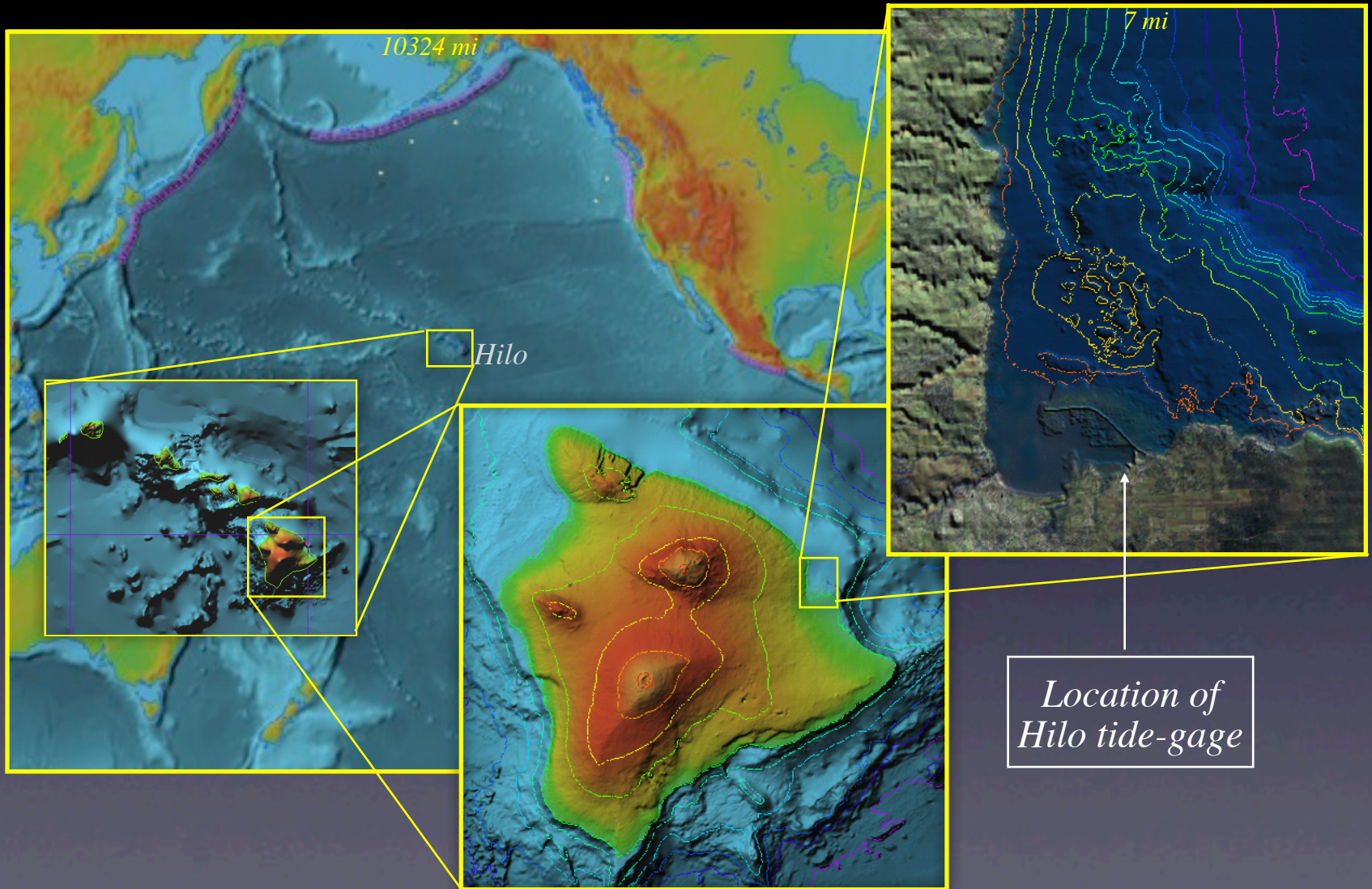
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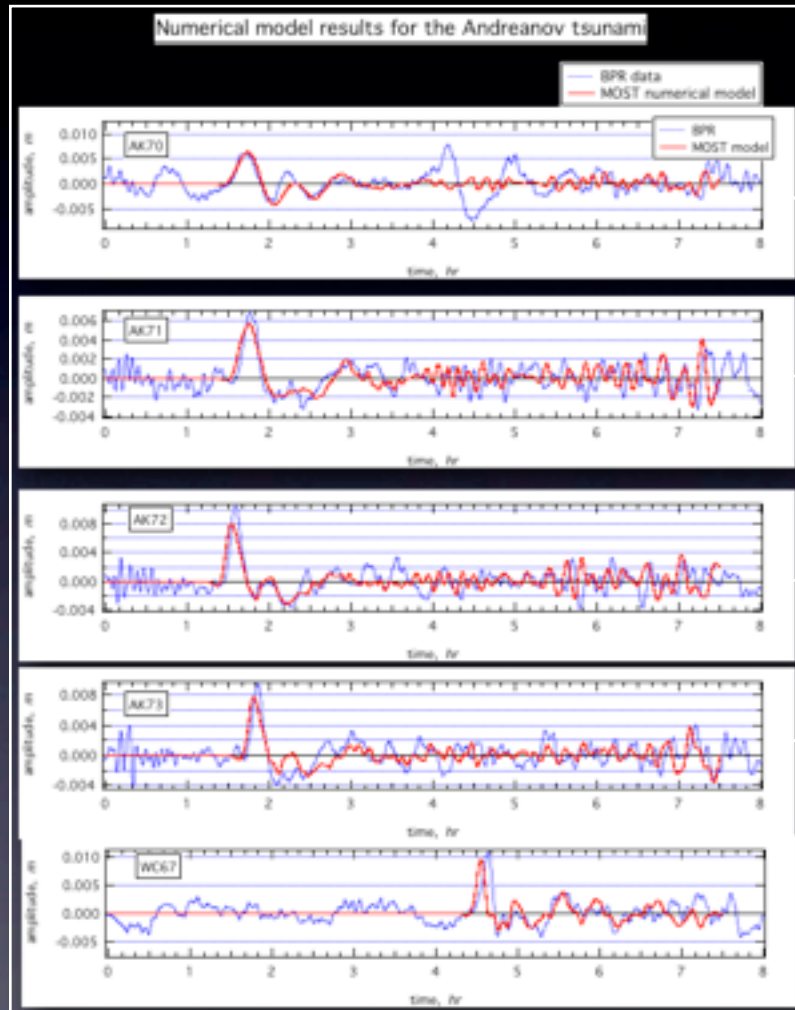
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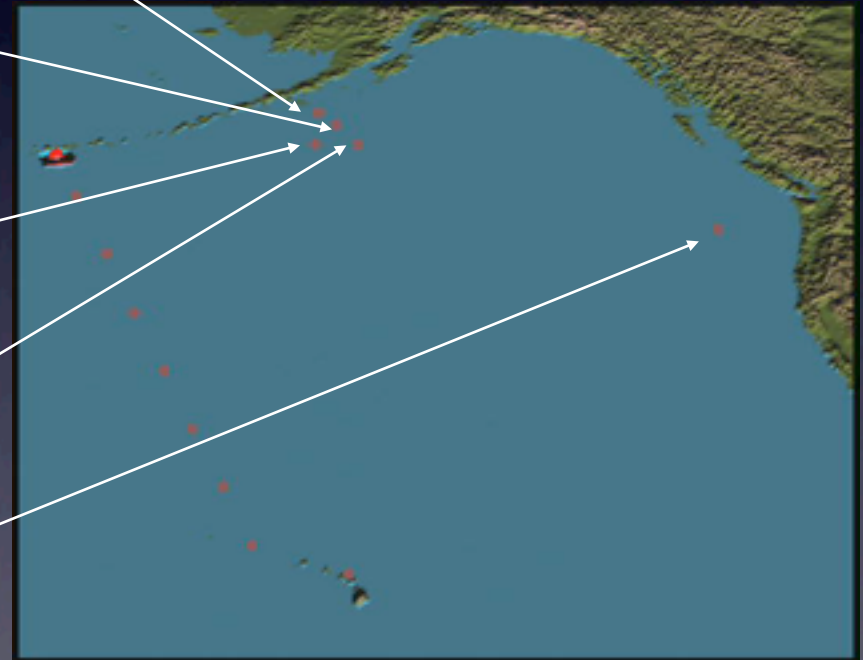
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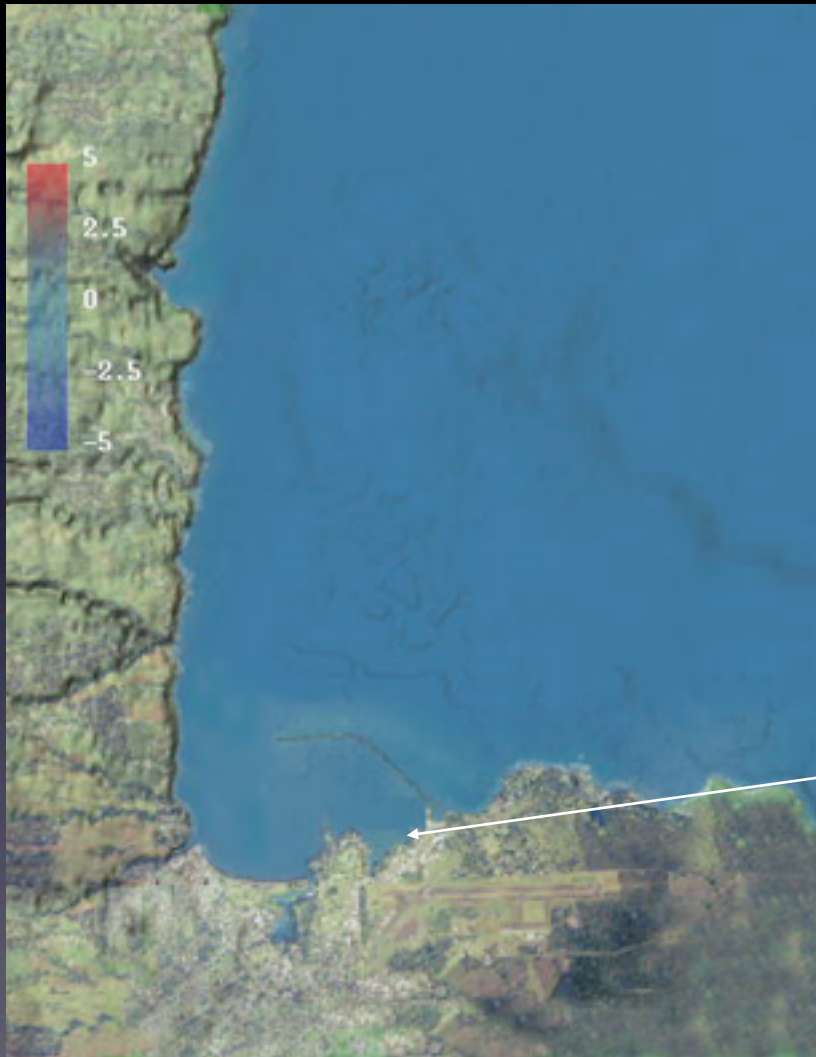
Propagation scale



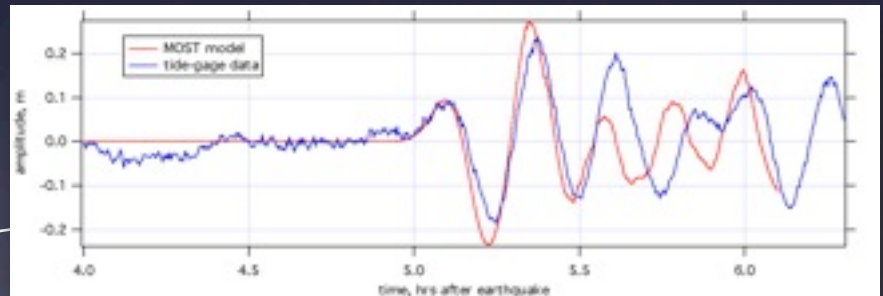
*June 10, 1996 Andreanov tsunami
(Titov & Gonzalez, 1997)*



Inundation model scale



*Andreanov tsunami
“inundation” model
comparison with tide-gage
data*



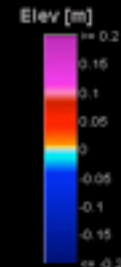
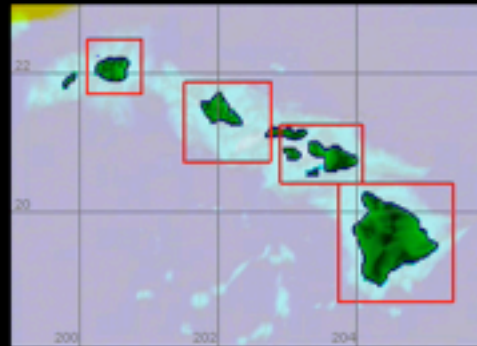
Scale comparison

Cen. Kuri Tsunami Mw = 8.1

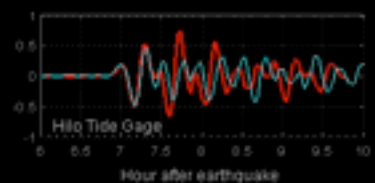
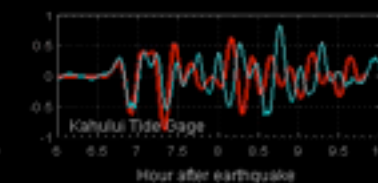
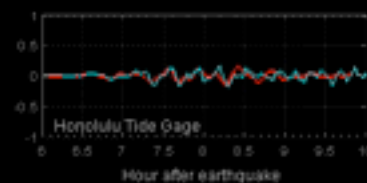
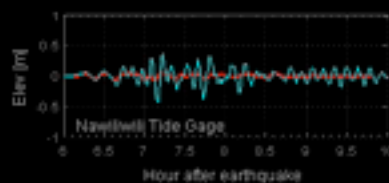
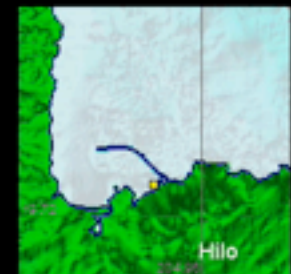
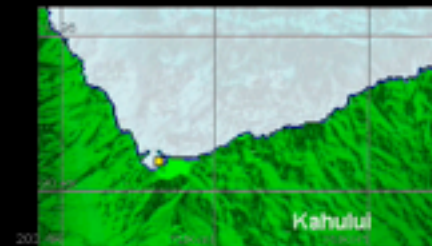
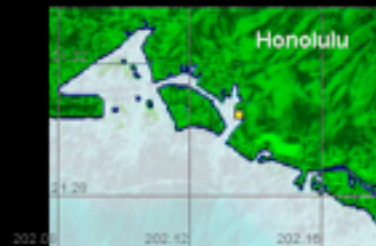
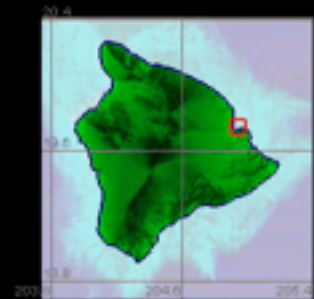
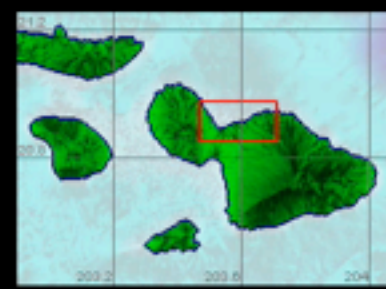
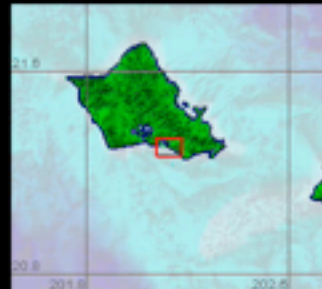
2006.11.15 11:14:16 UTC

05h50m01s

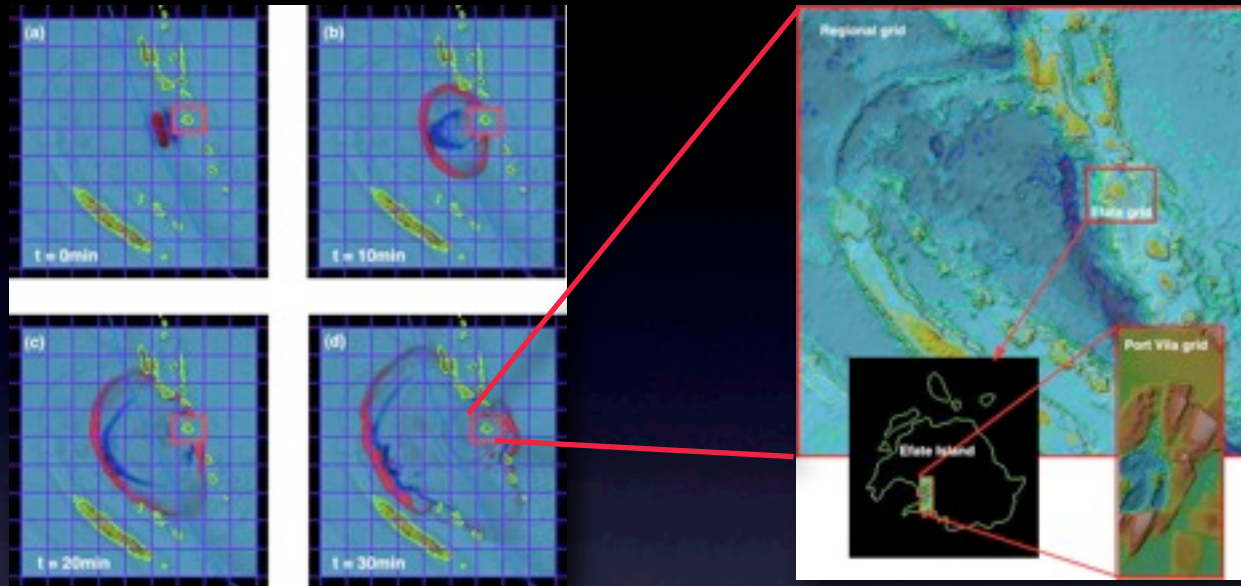
NOAA/PMEL/NCTR



— SIM
— observation



Small scale inundation effects



Port Vila, Vanuatu. Hypothetical Mw8.1 tsunami



Reason 2: Inundation dynamics

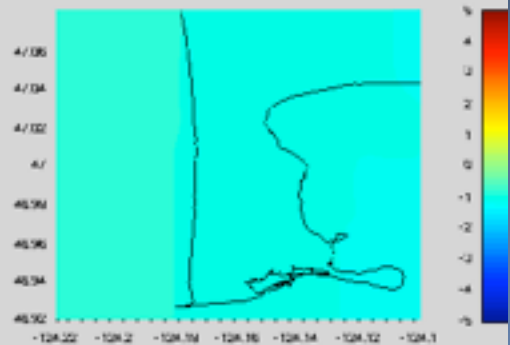
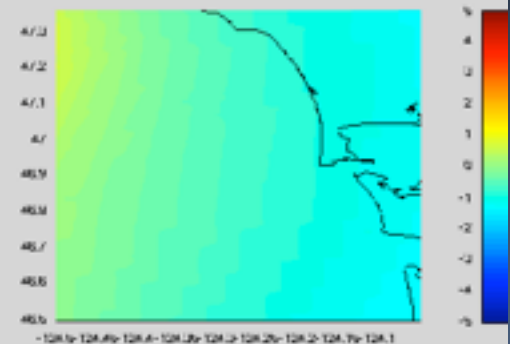
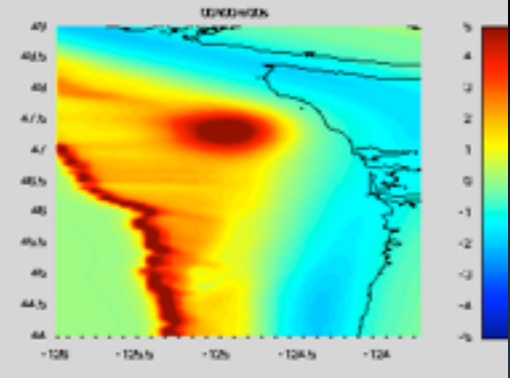
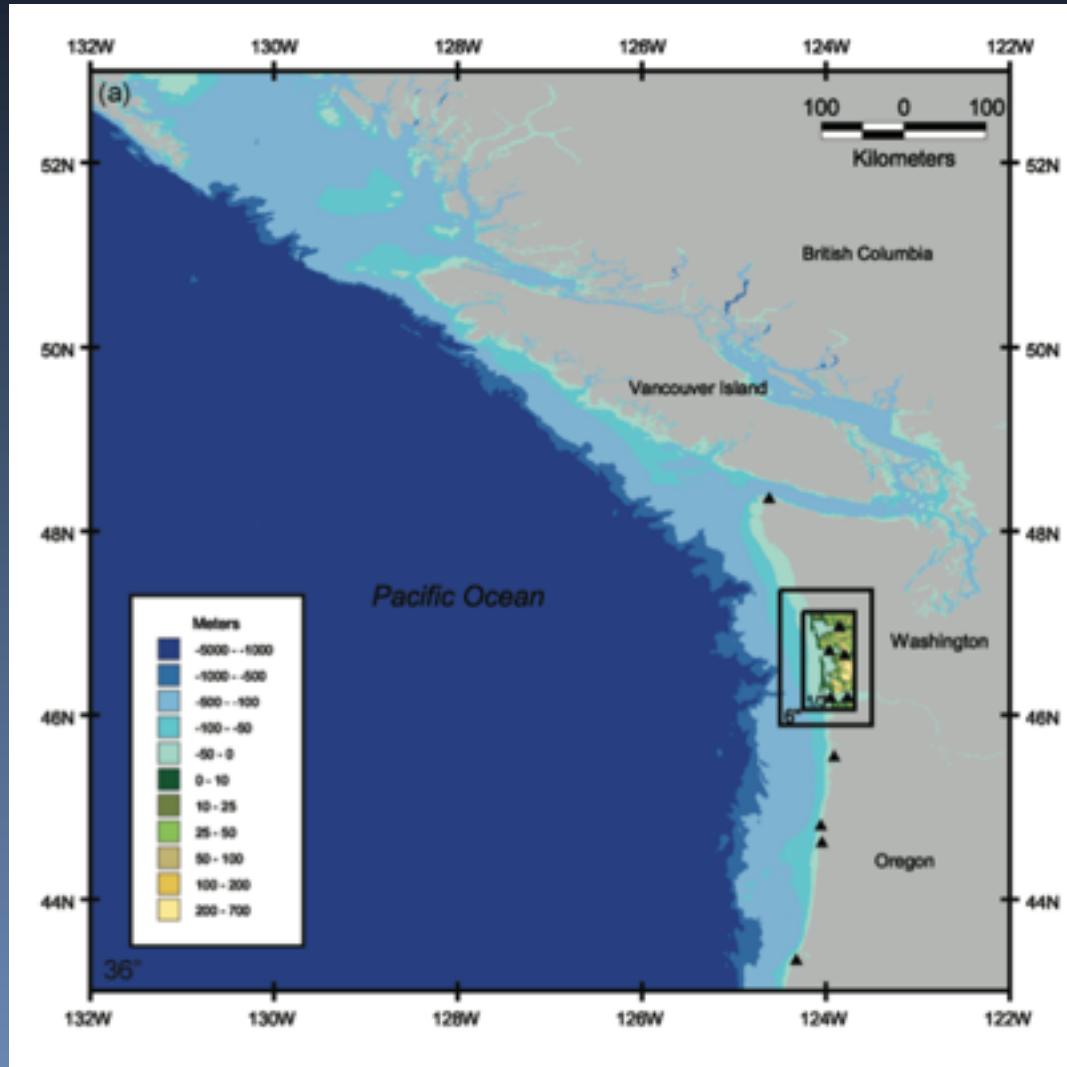


Simulation of the Aonae
inundation

(1993 Okushiri tsunami)

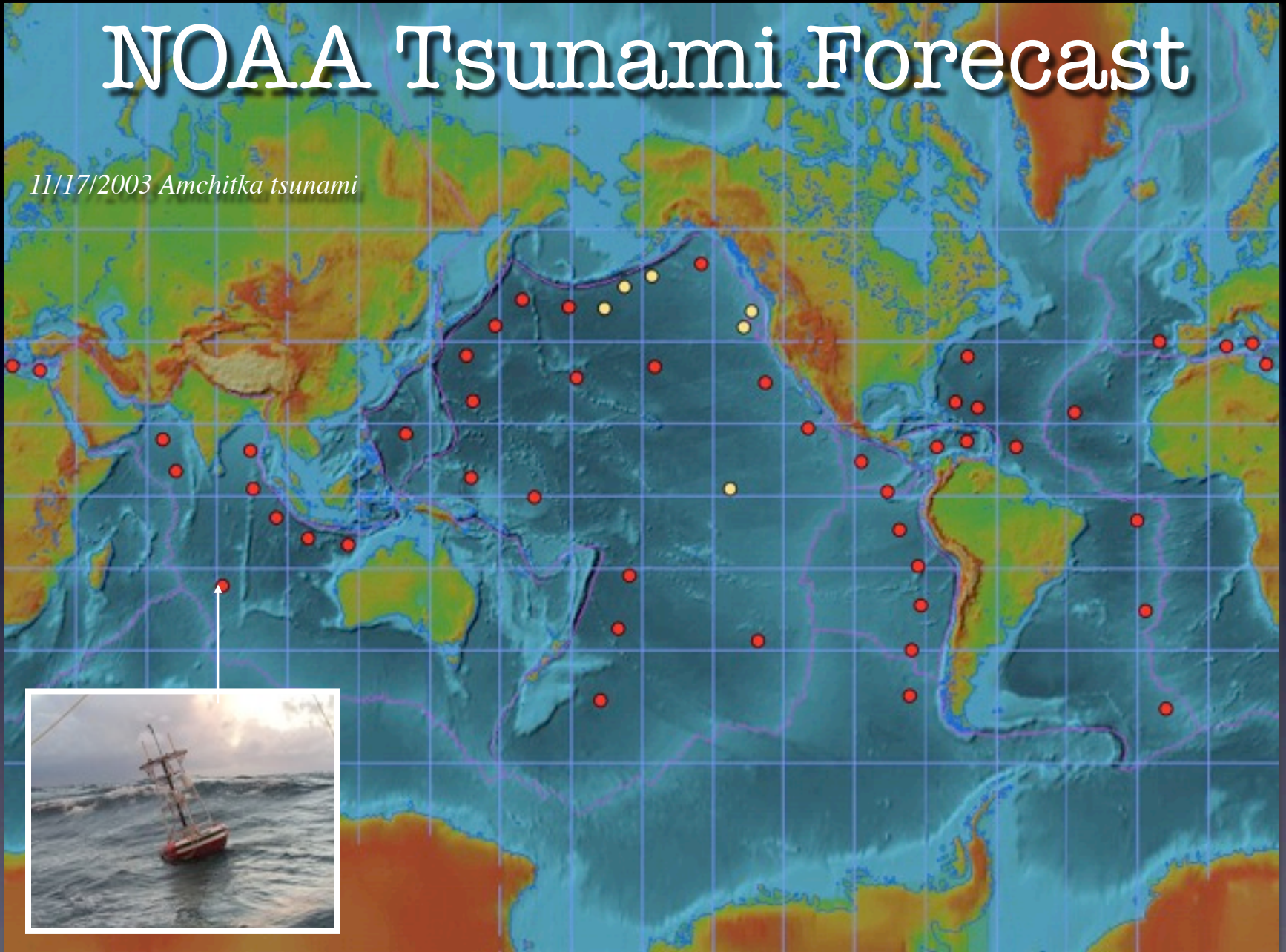


Tsunami Forecast for Ocean Shores, WA



NOAA Tsunami Forecast

11/17/2003 Amchitka tsunami



NOAA Tsunami Forecast

11/17/2003 Amchitka tsunami

$M_w = 7.5$



NOAA Tsunami Forecast

11/17/2003 Amchitka tsunami

$M_w = 7.5$

3cm

-3

3cm

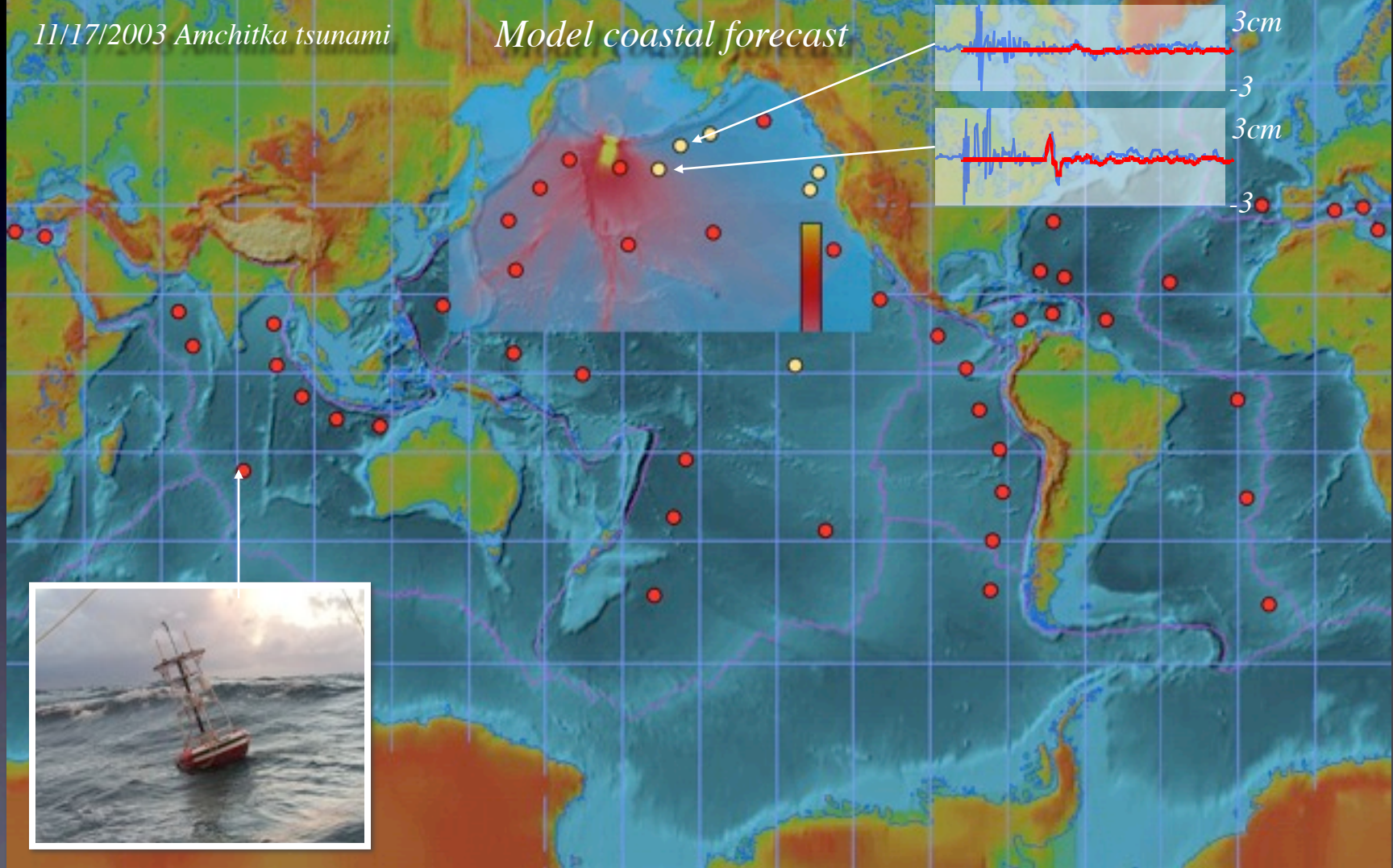
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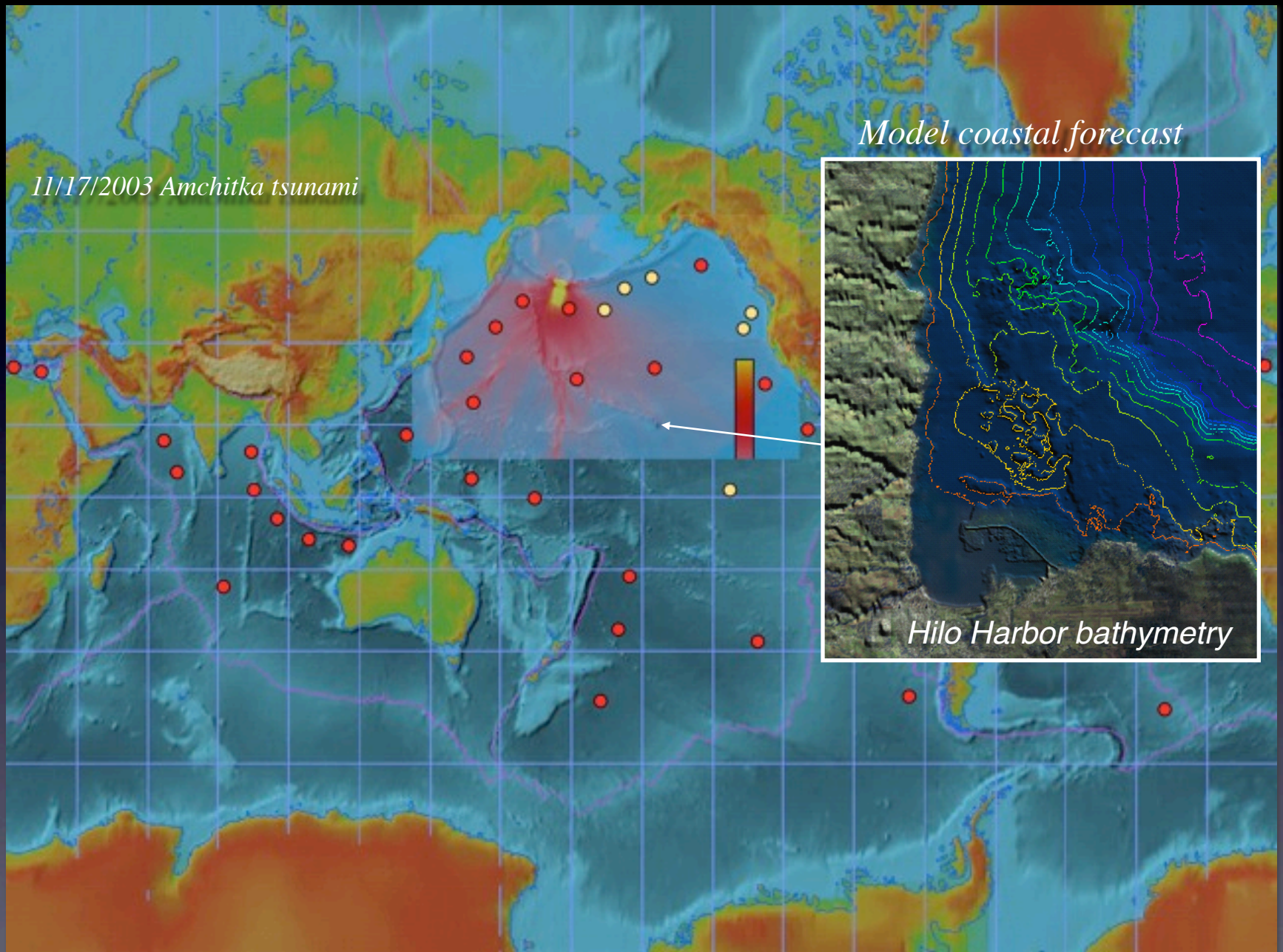


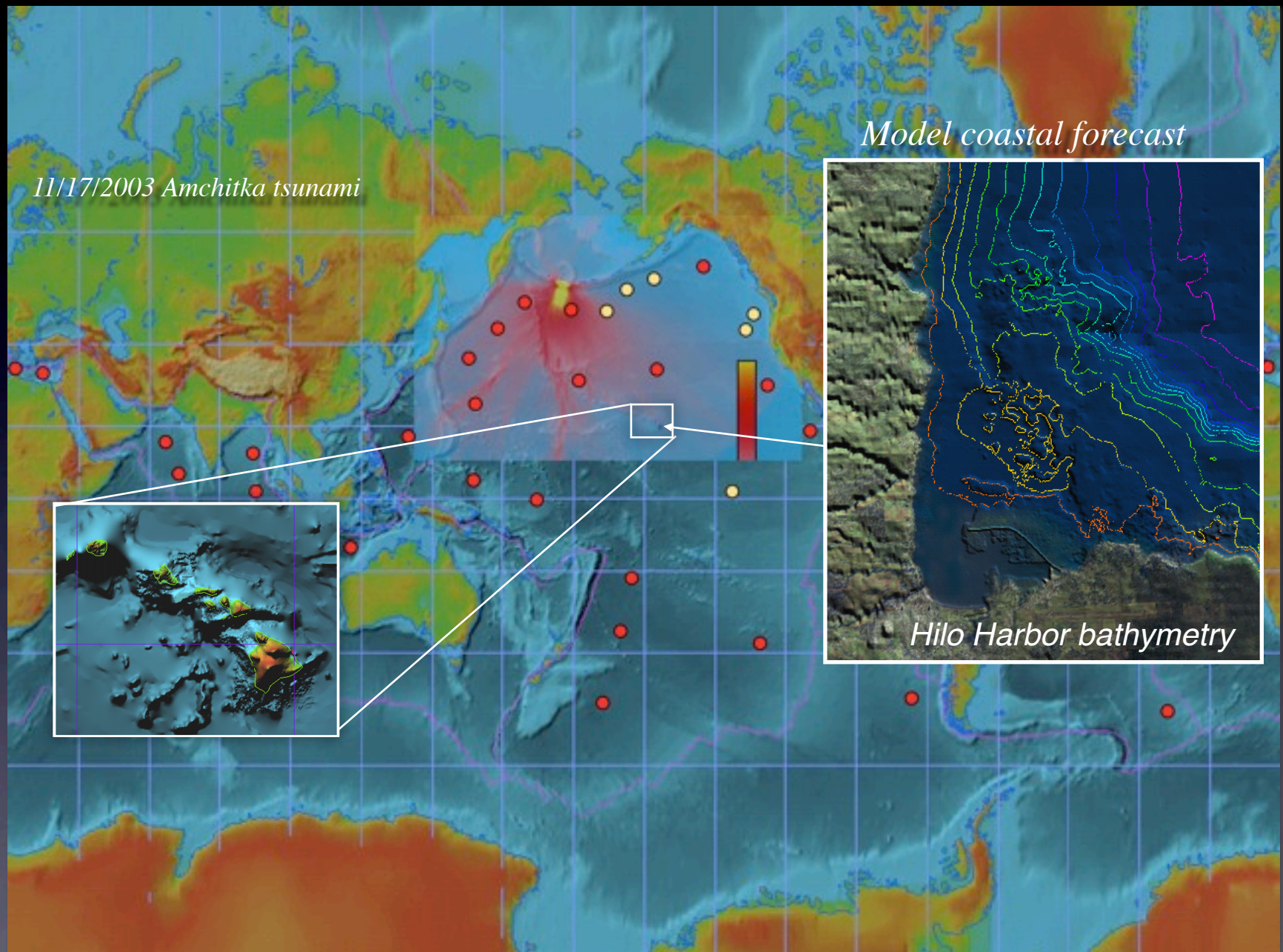
NOAA Tsunami Forecast

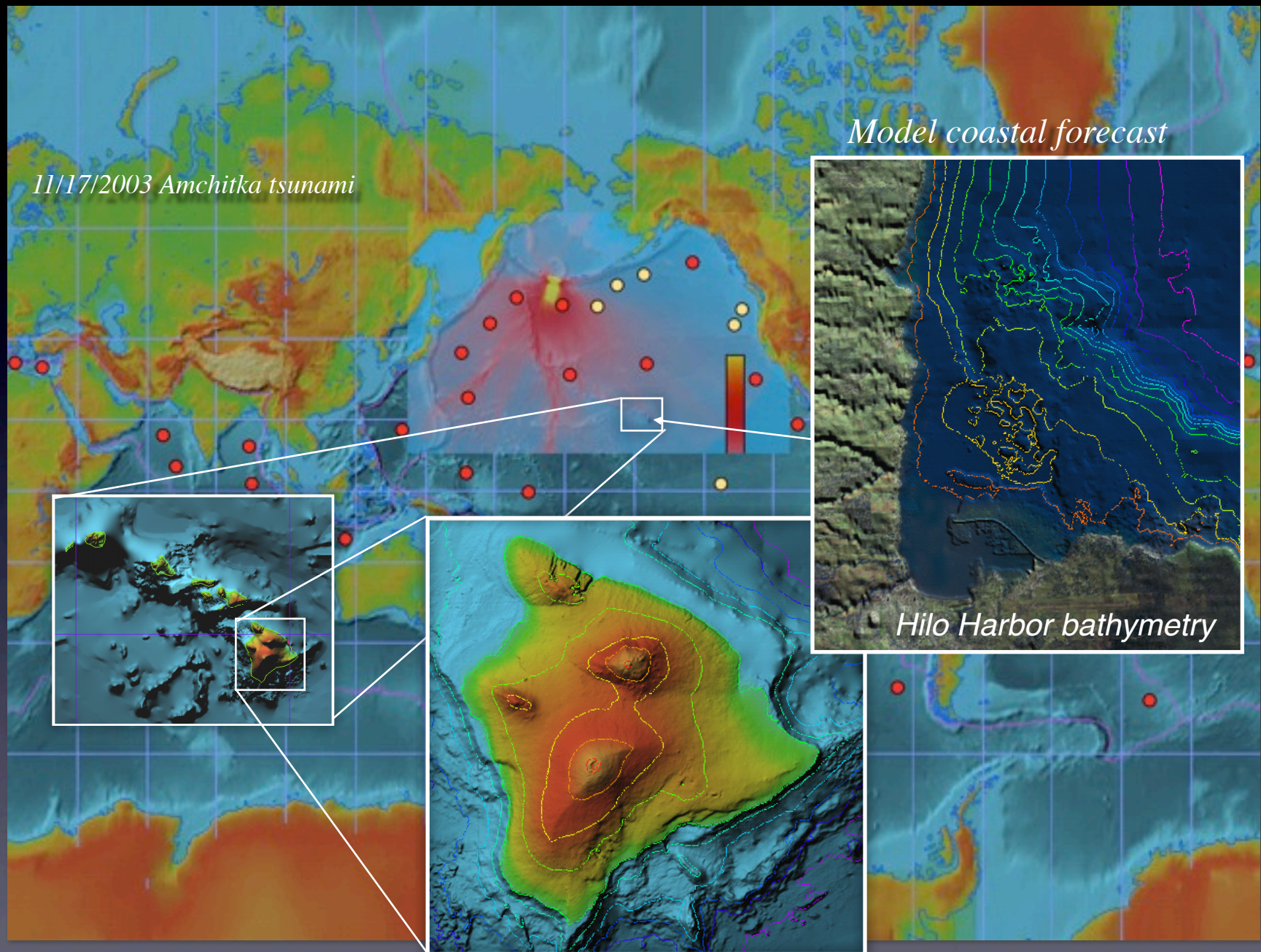
11/17/2003 Amchitka tsunami

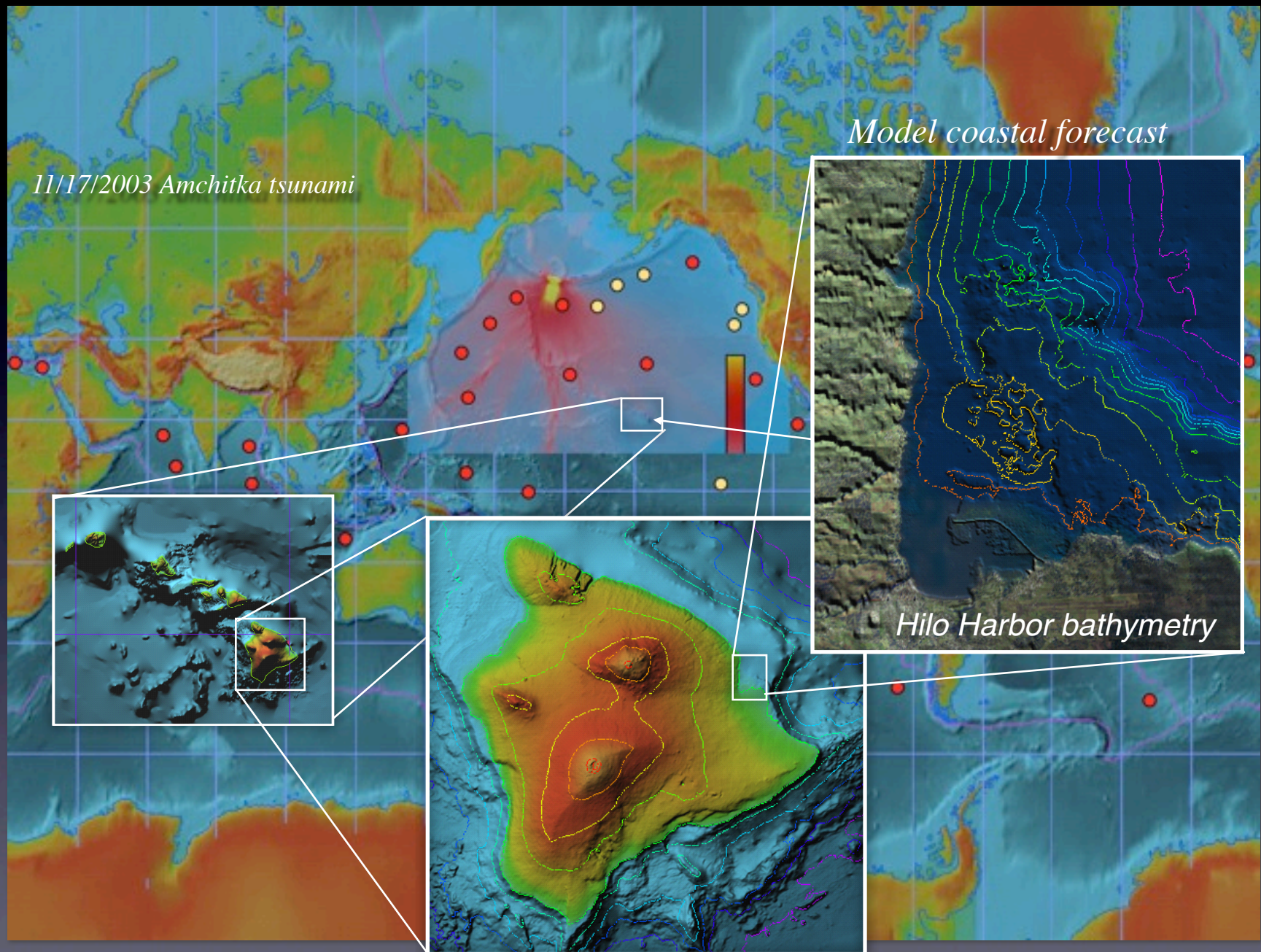
Model coastal forecast

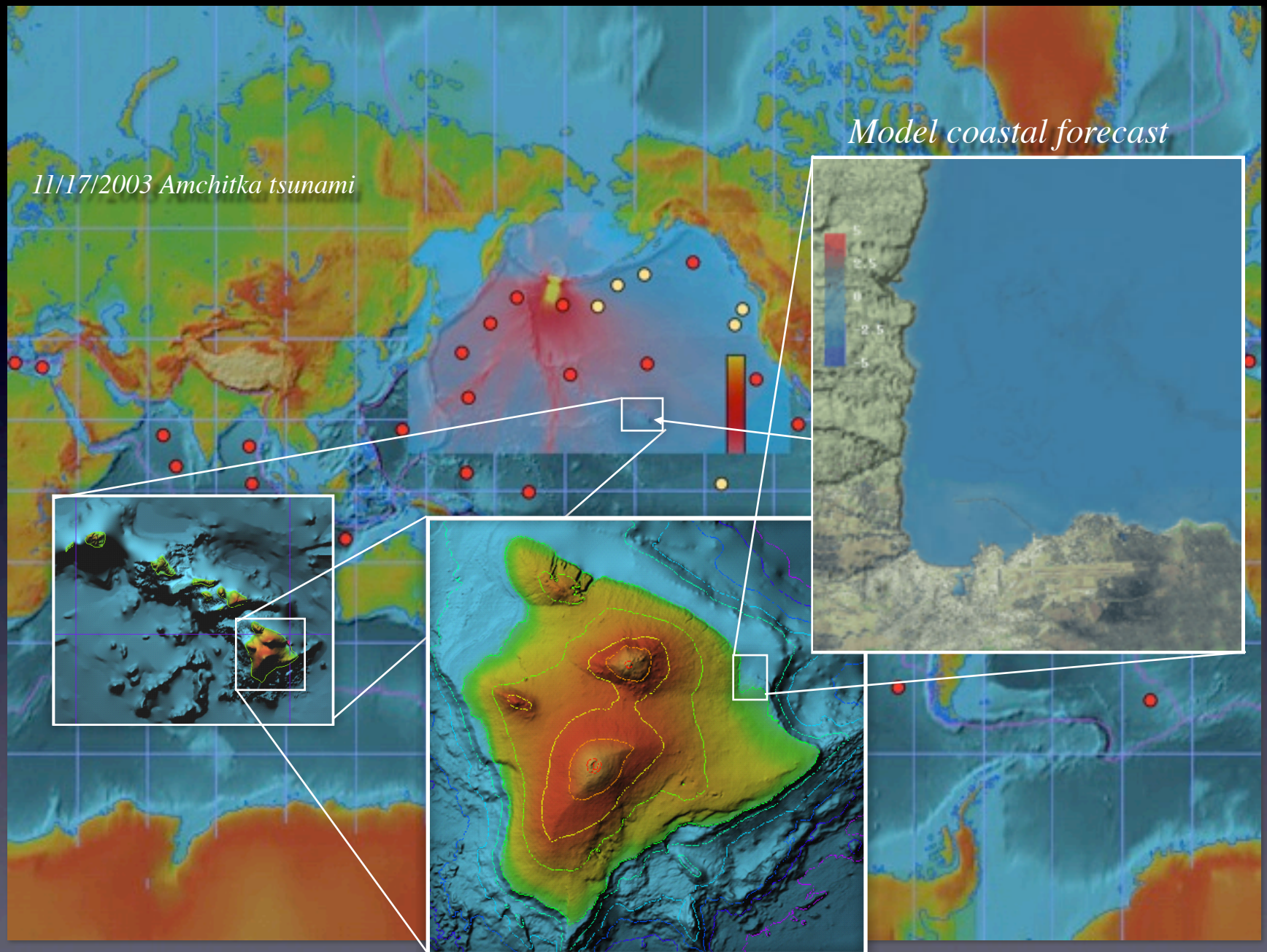


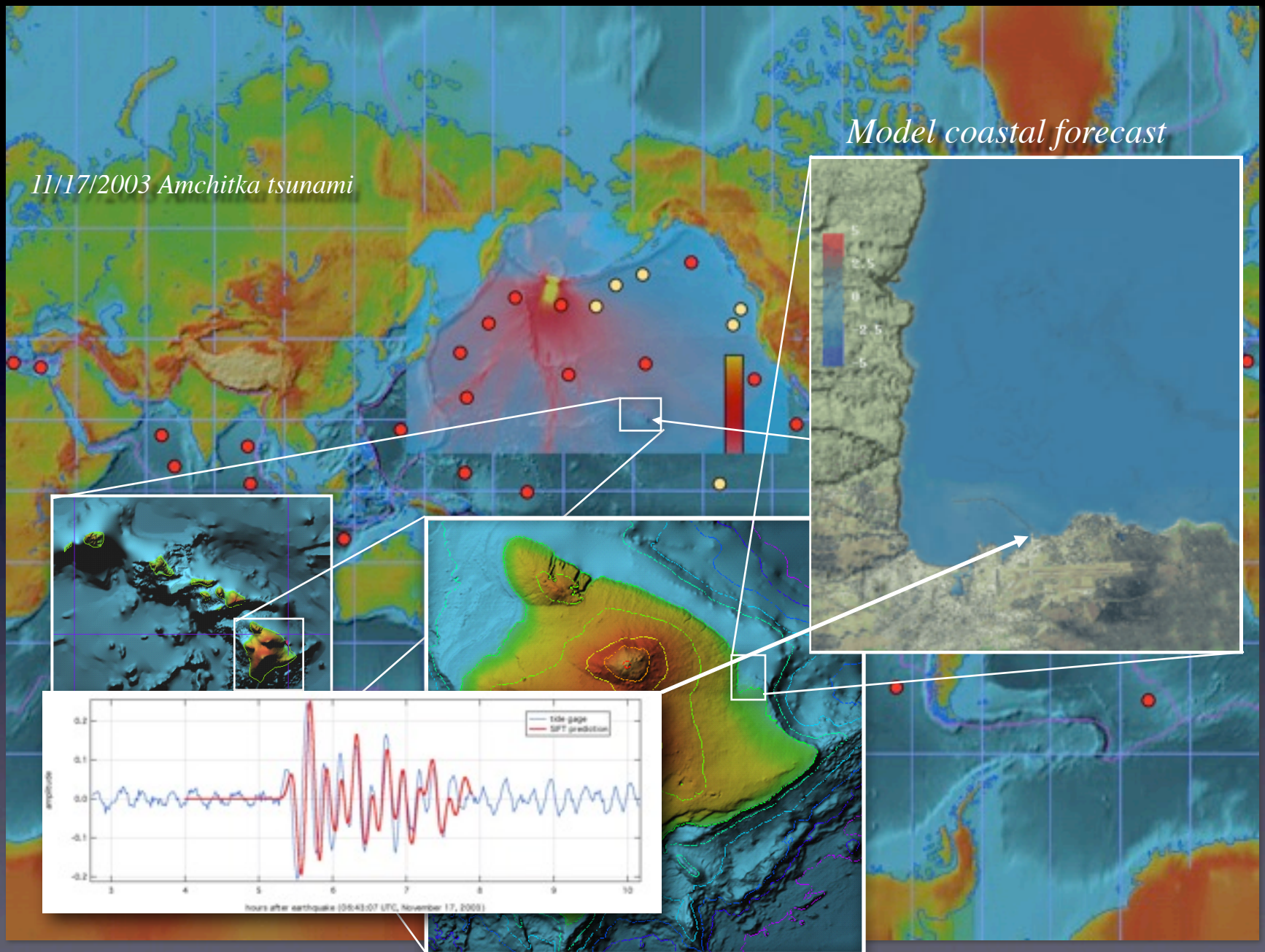




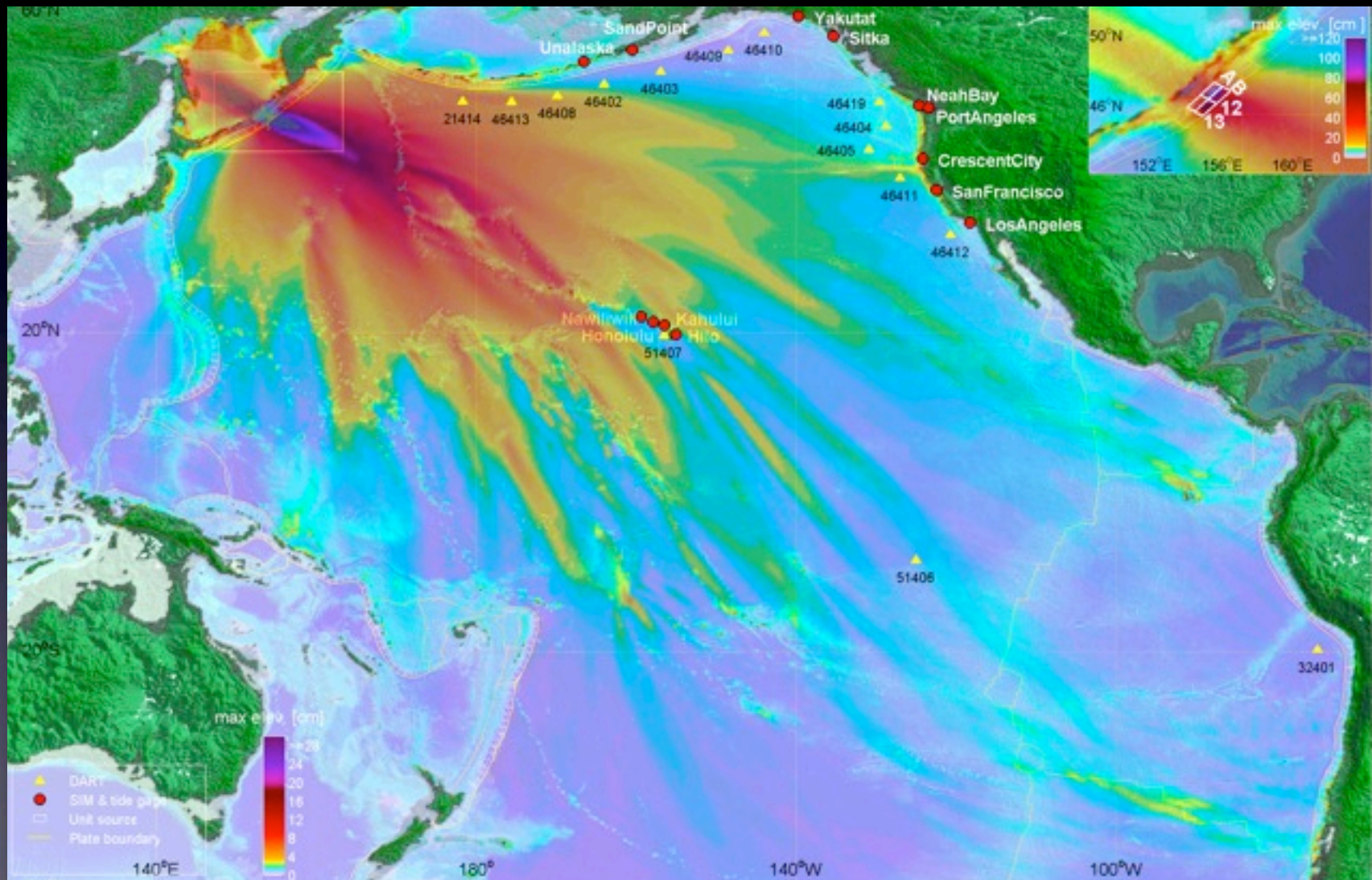




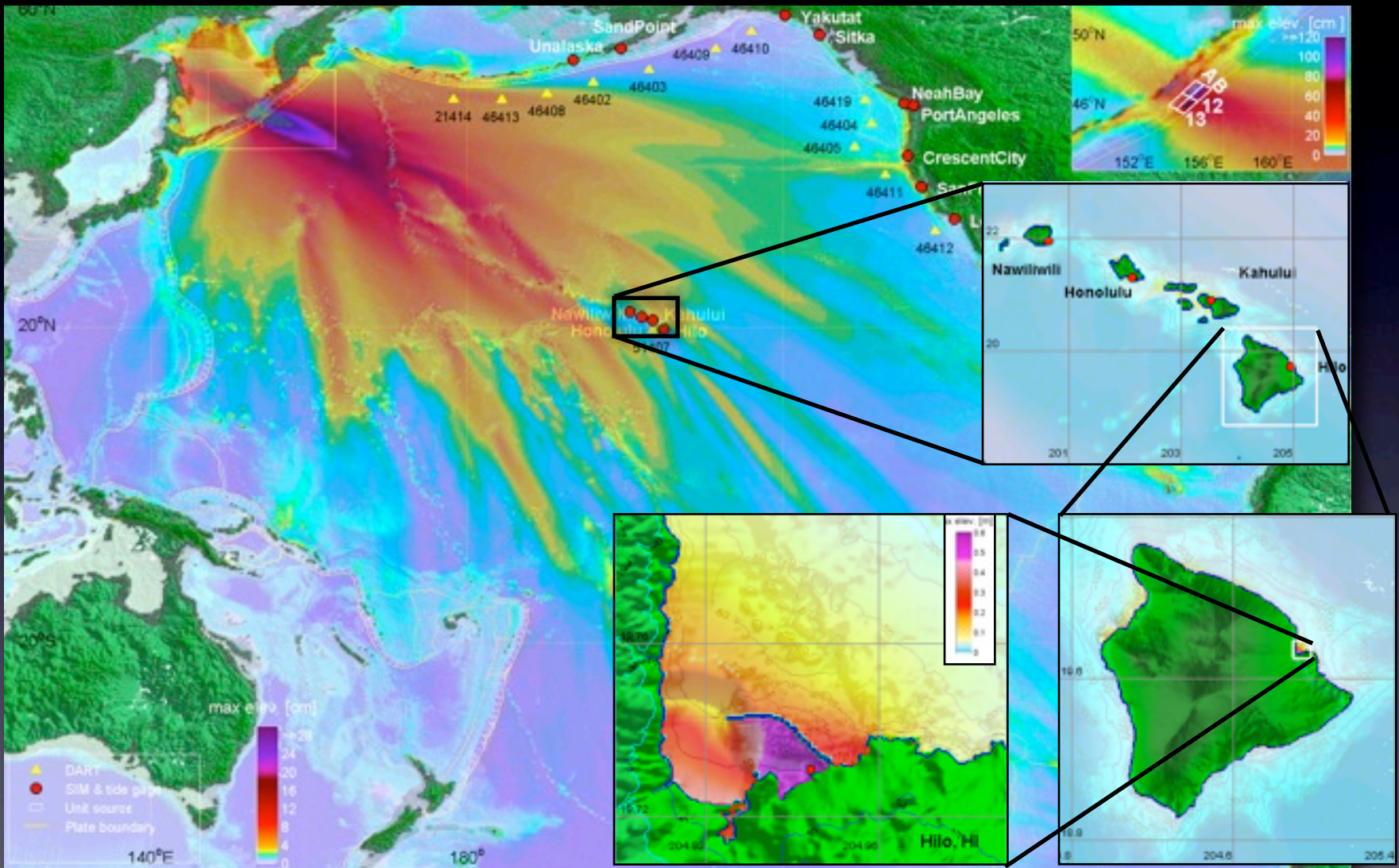




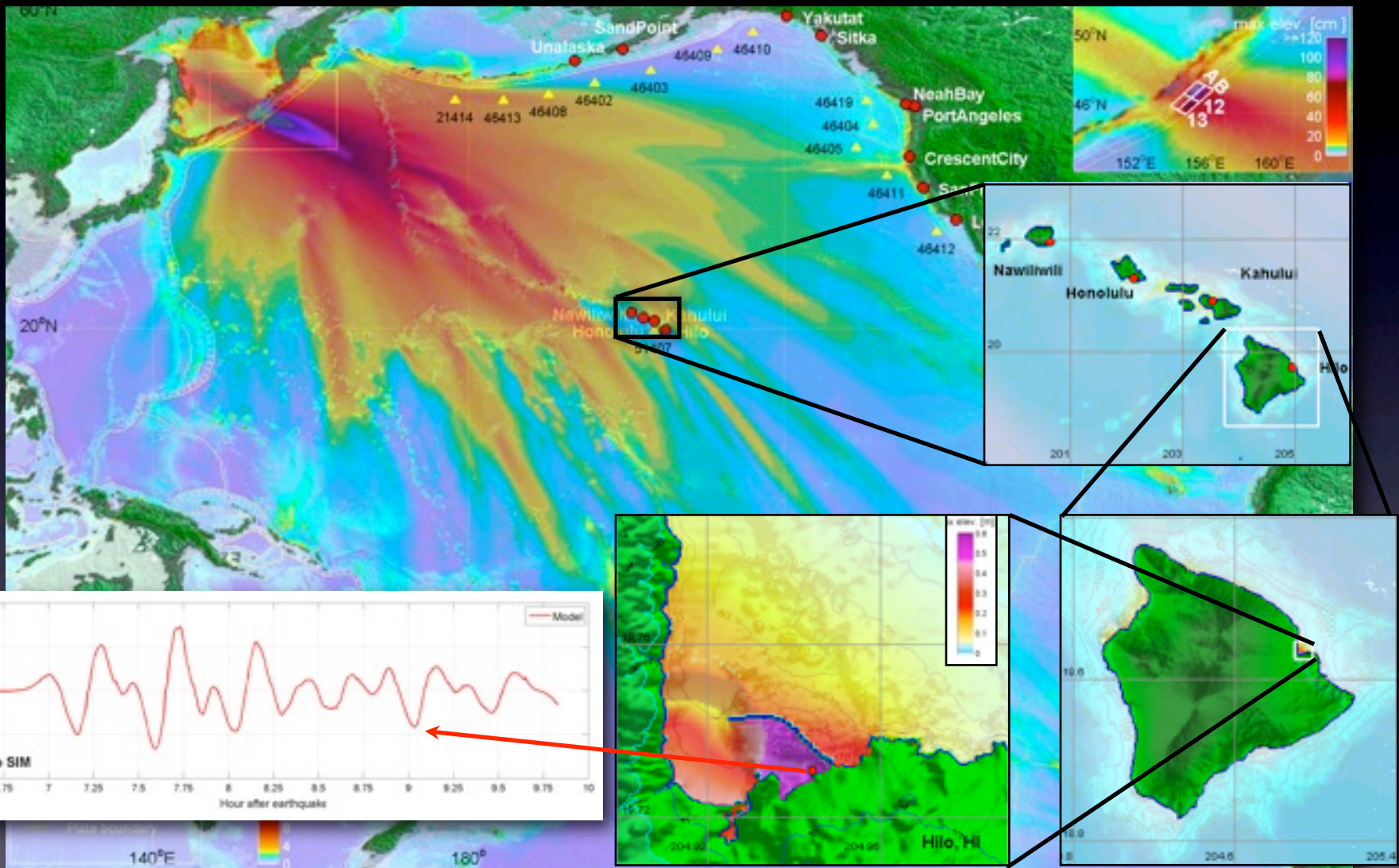
The November 15, 2006 Central Kuril Tsunami



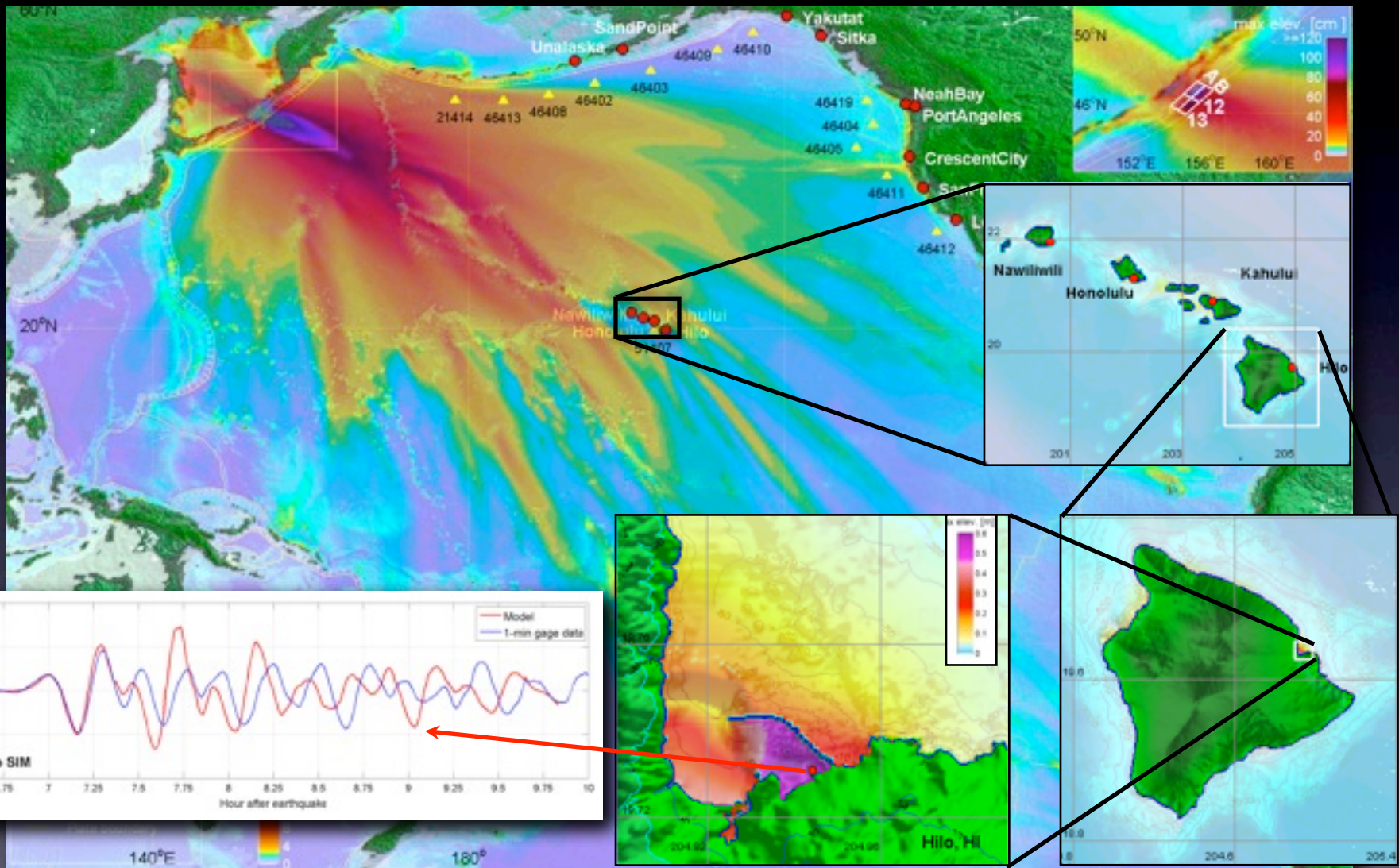
The November 15, 2006 Central Kuril Tsunami



The November 15, 2006 Central Kuril Tsunami

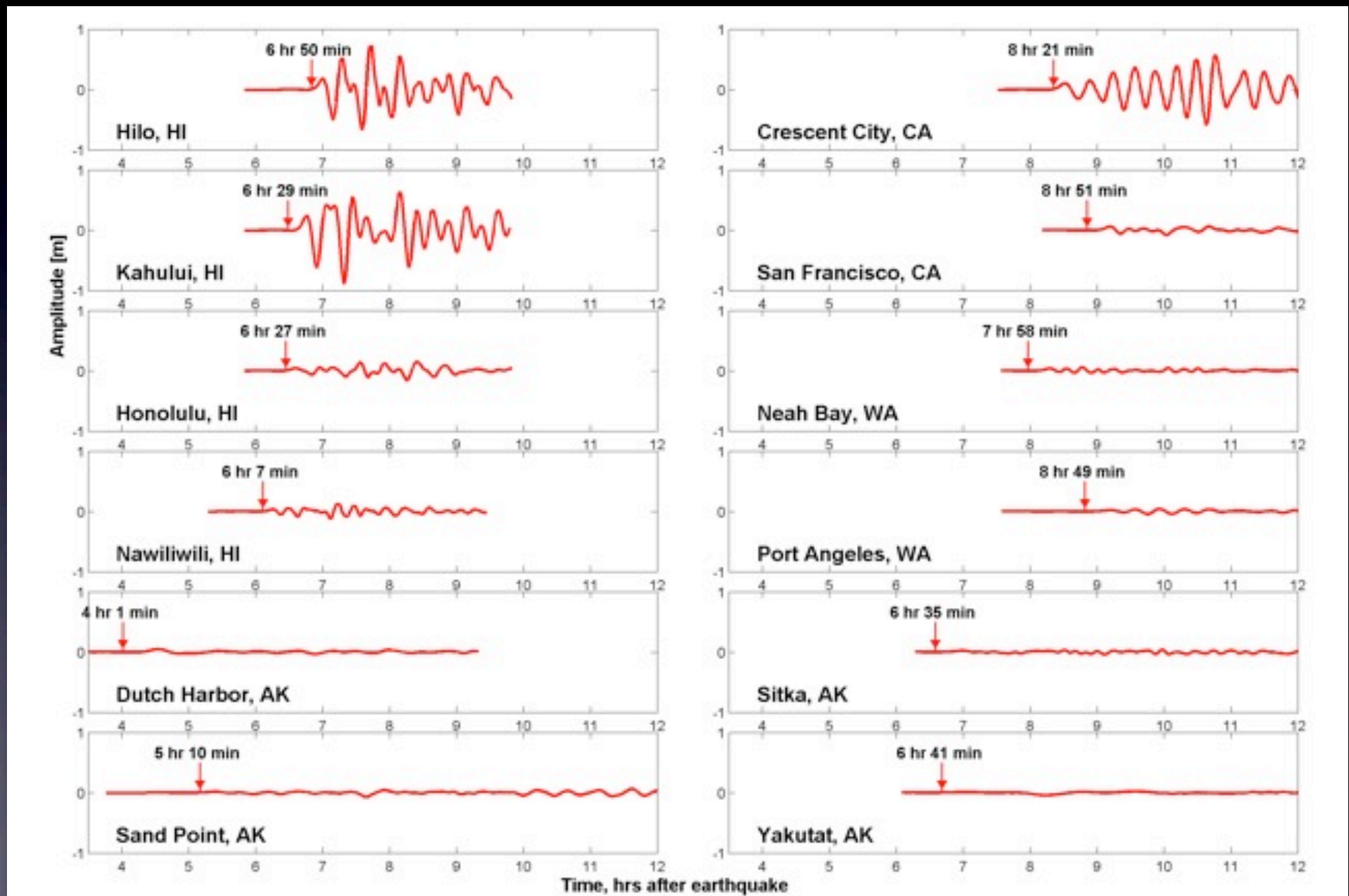


The November 15, 2006 Central Kuril Tsunami



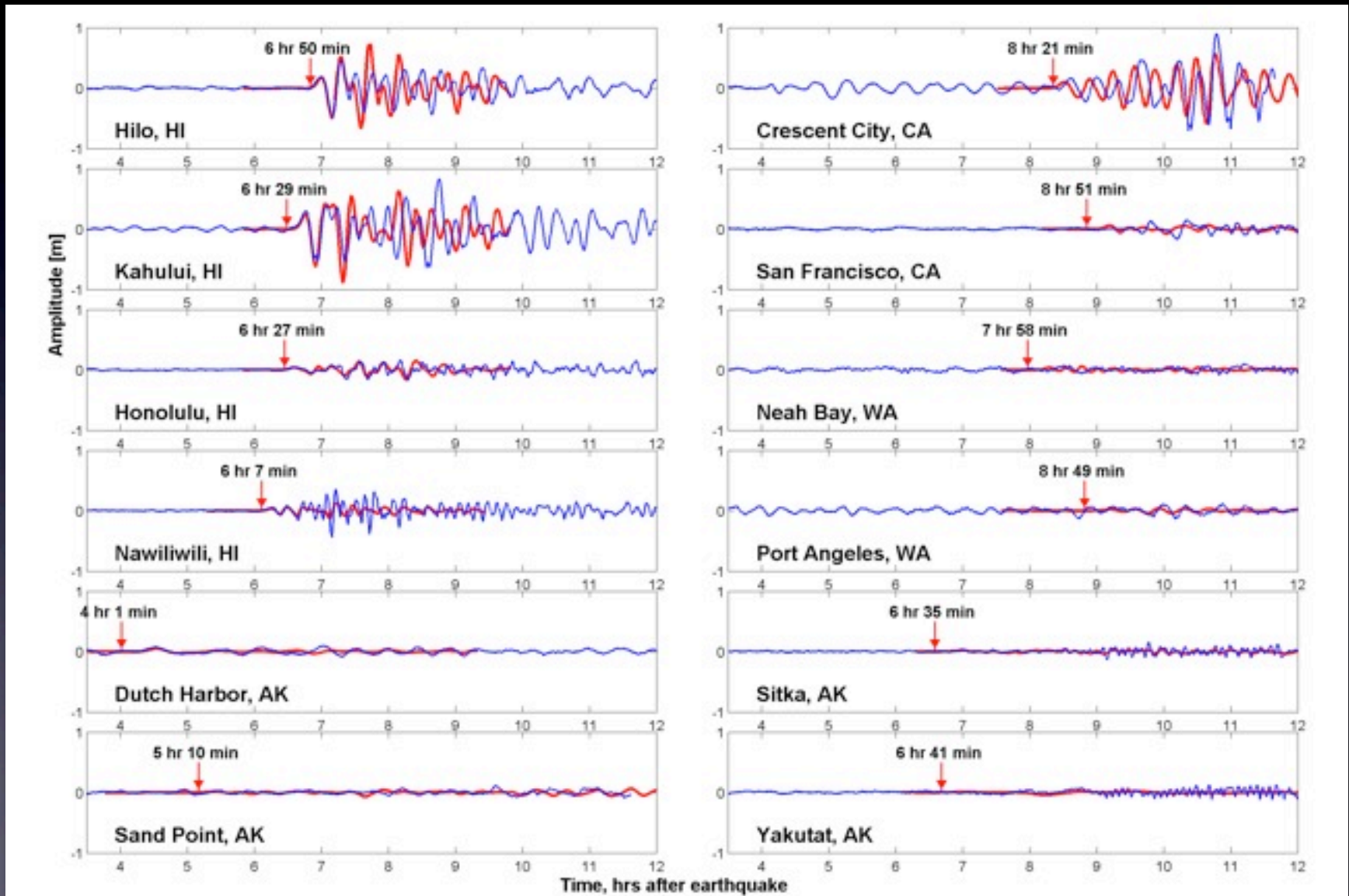
The November 15, 2006 Central Kuril Tsunami

Forecast vs Observation



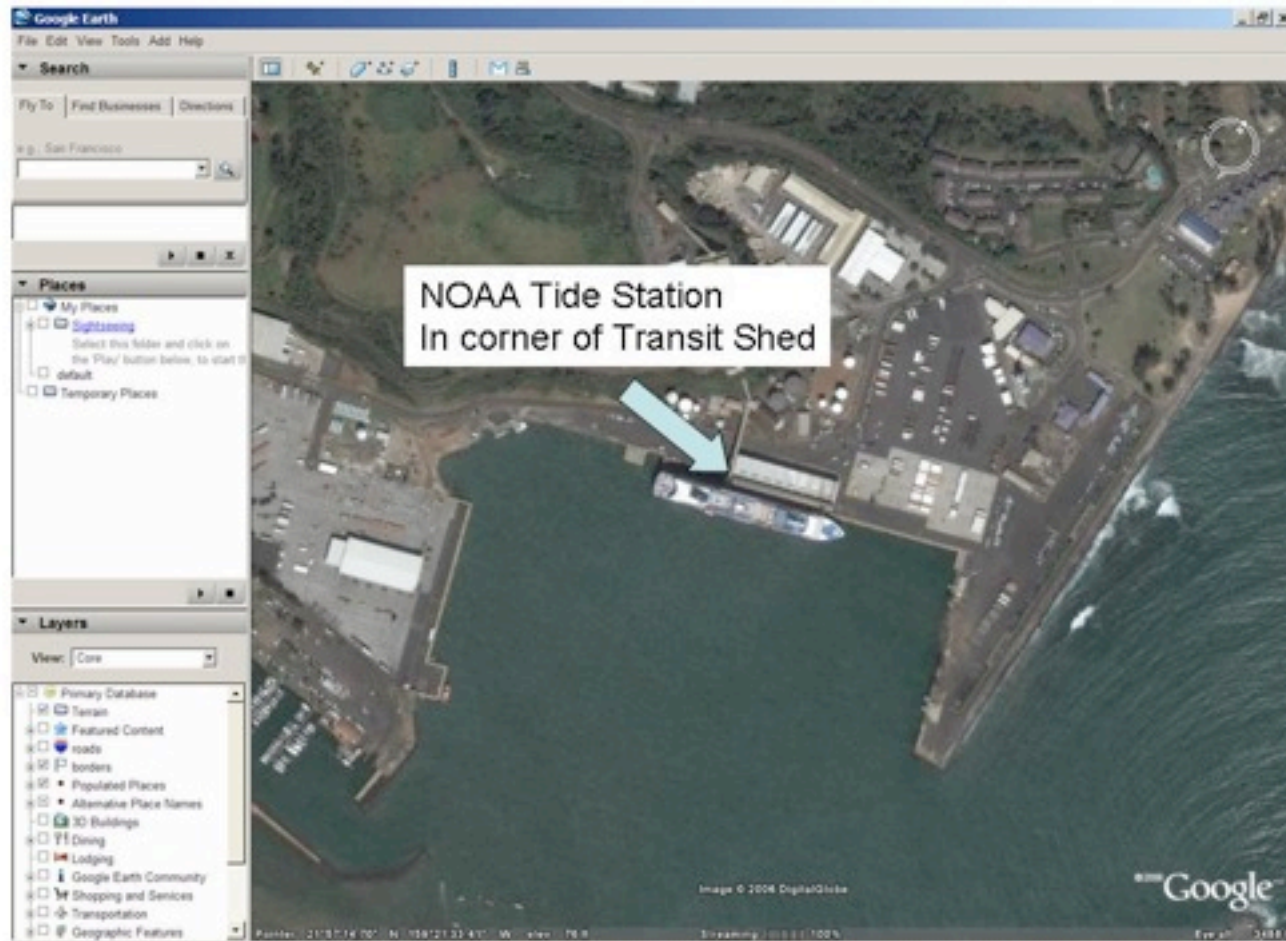
The November 15, 2006 Central Kuril Tsunami

Forecast vs Observation

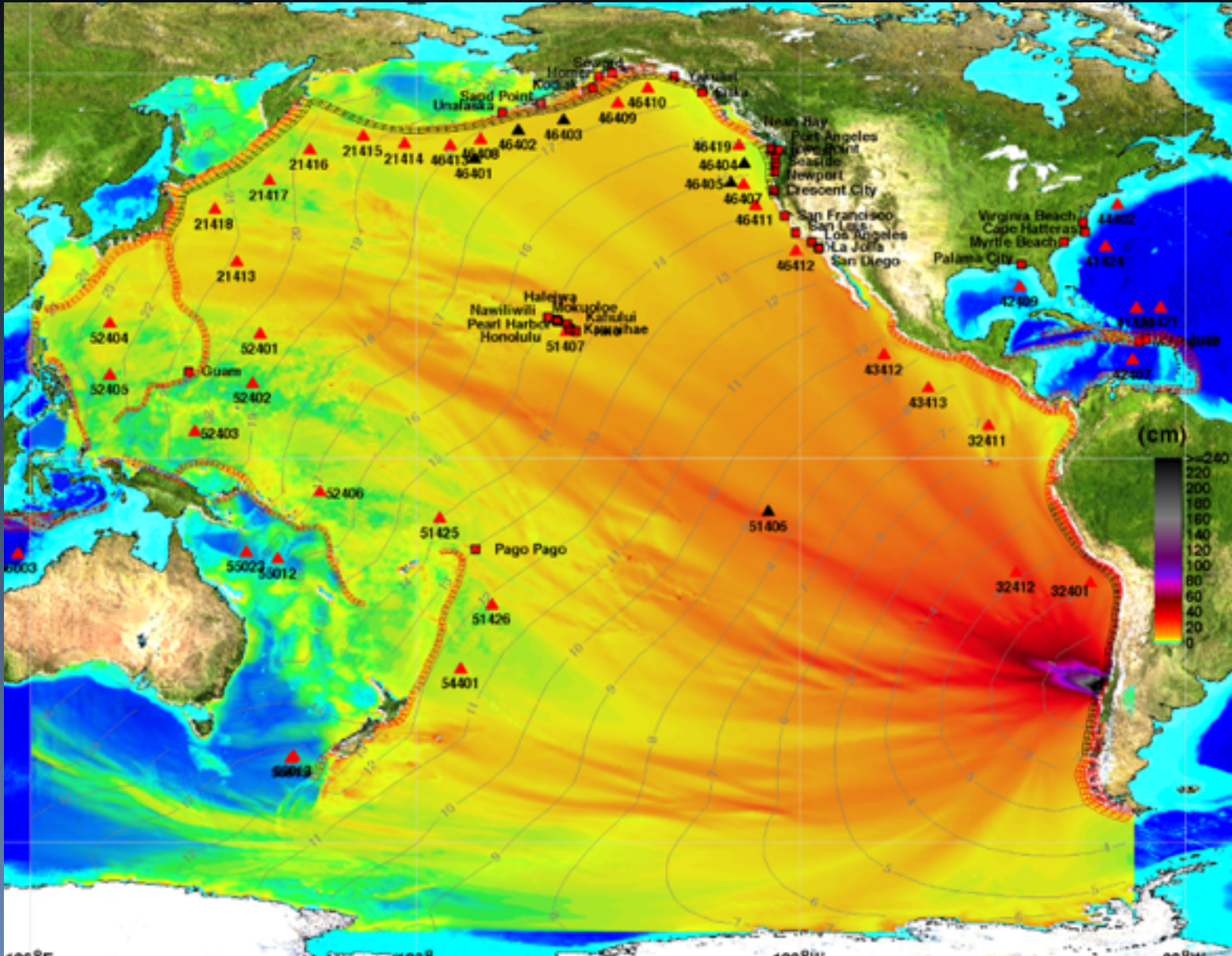


Nawiliwili Comparison

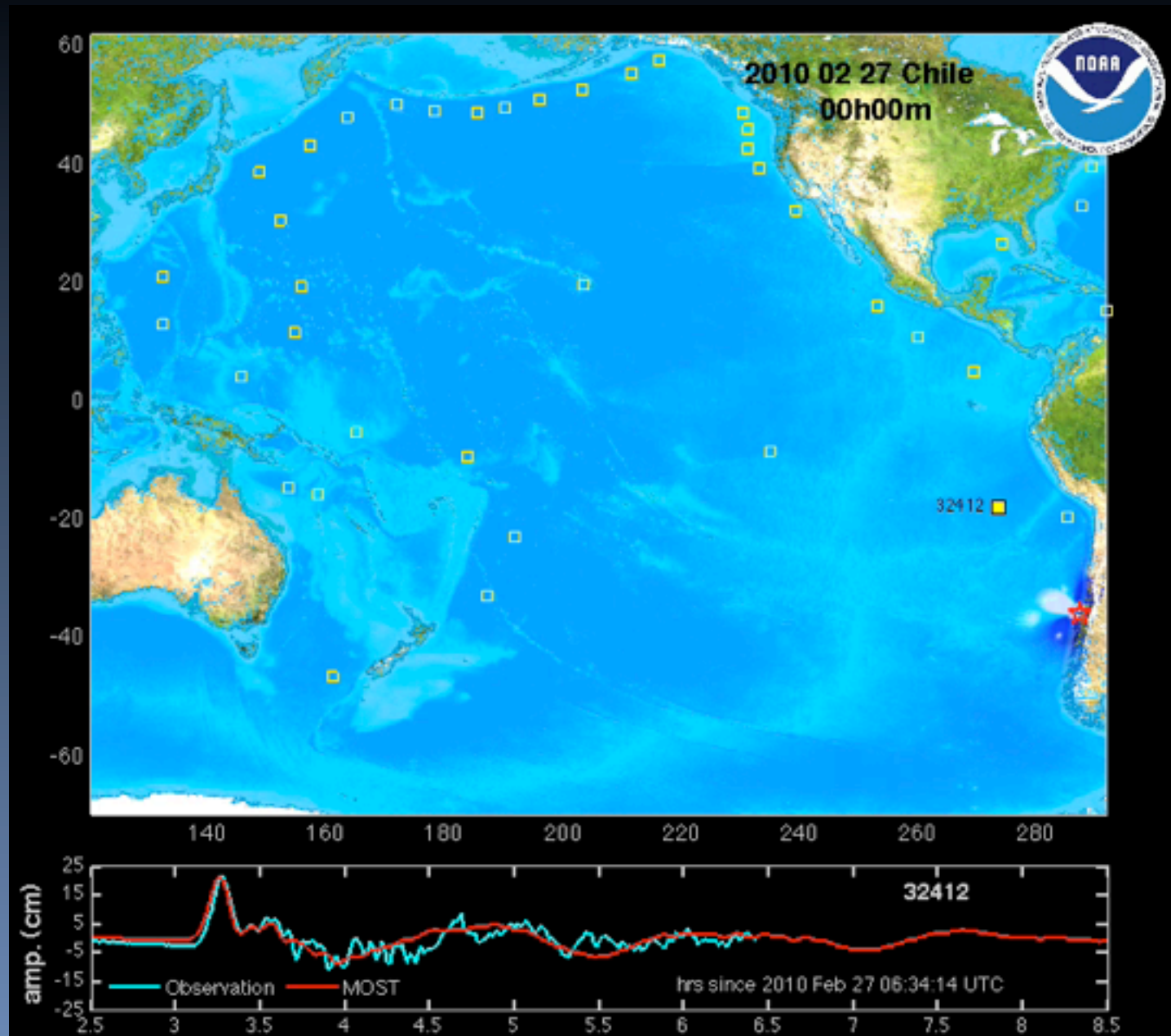
(Impacted by Cruise Ship?)



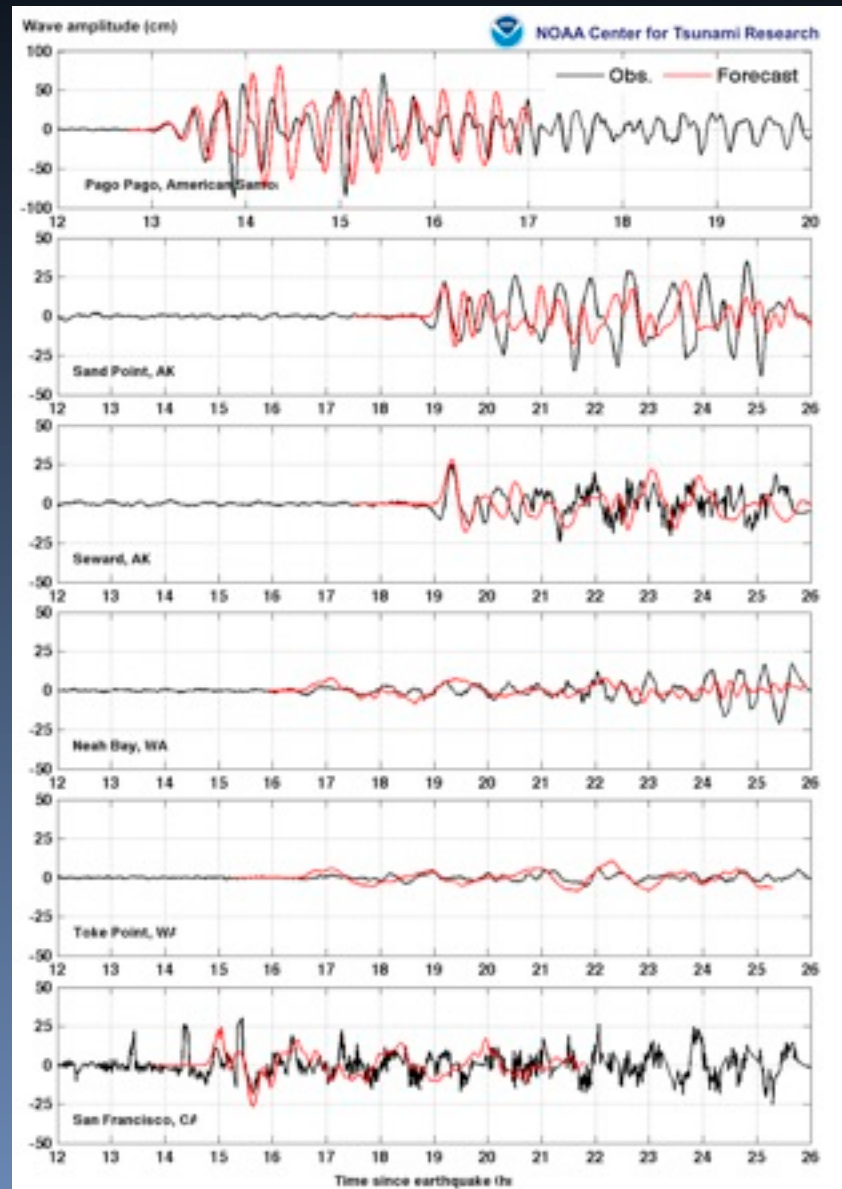
Tsunami Forecast Overview, Chile 2010



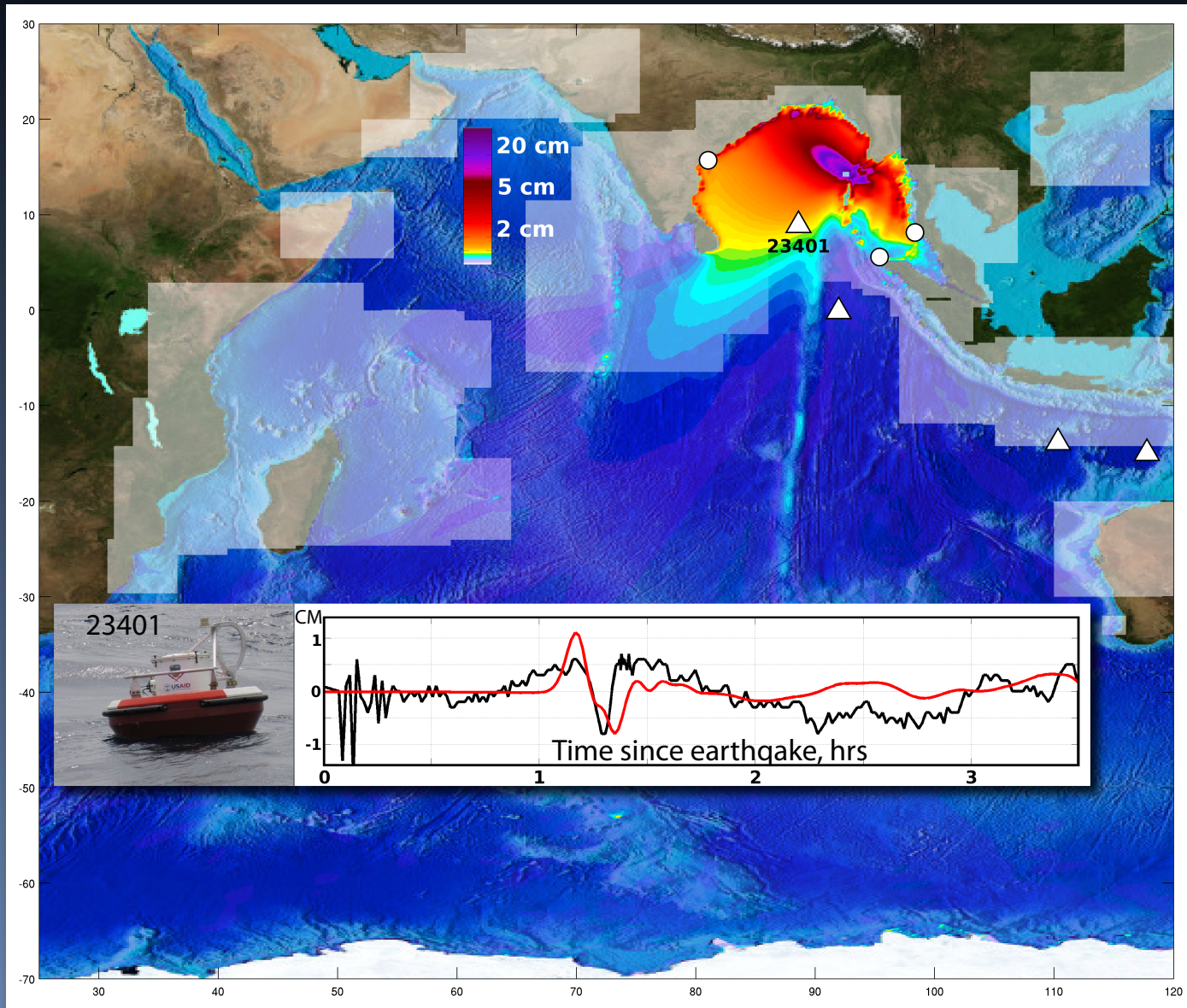
Tsunami Forecast Overview, Chile 2010

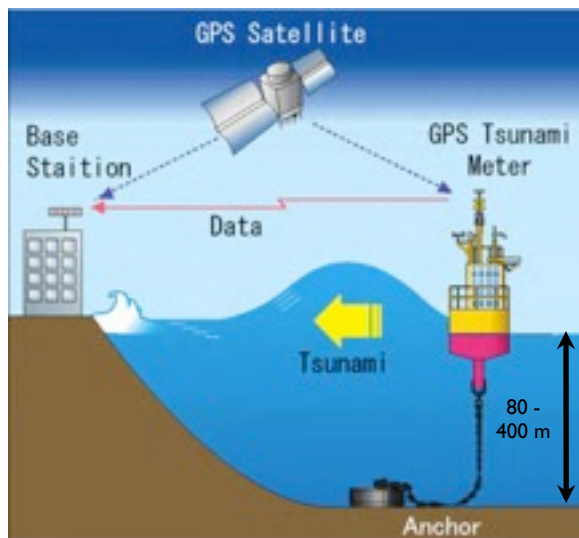
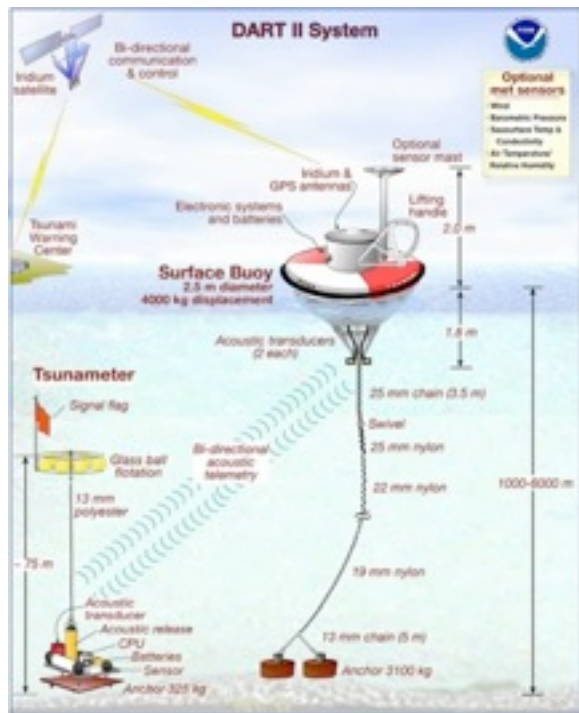


Results: Tide gauge comparisons, Chile 2010

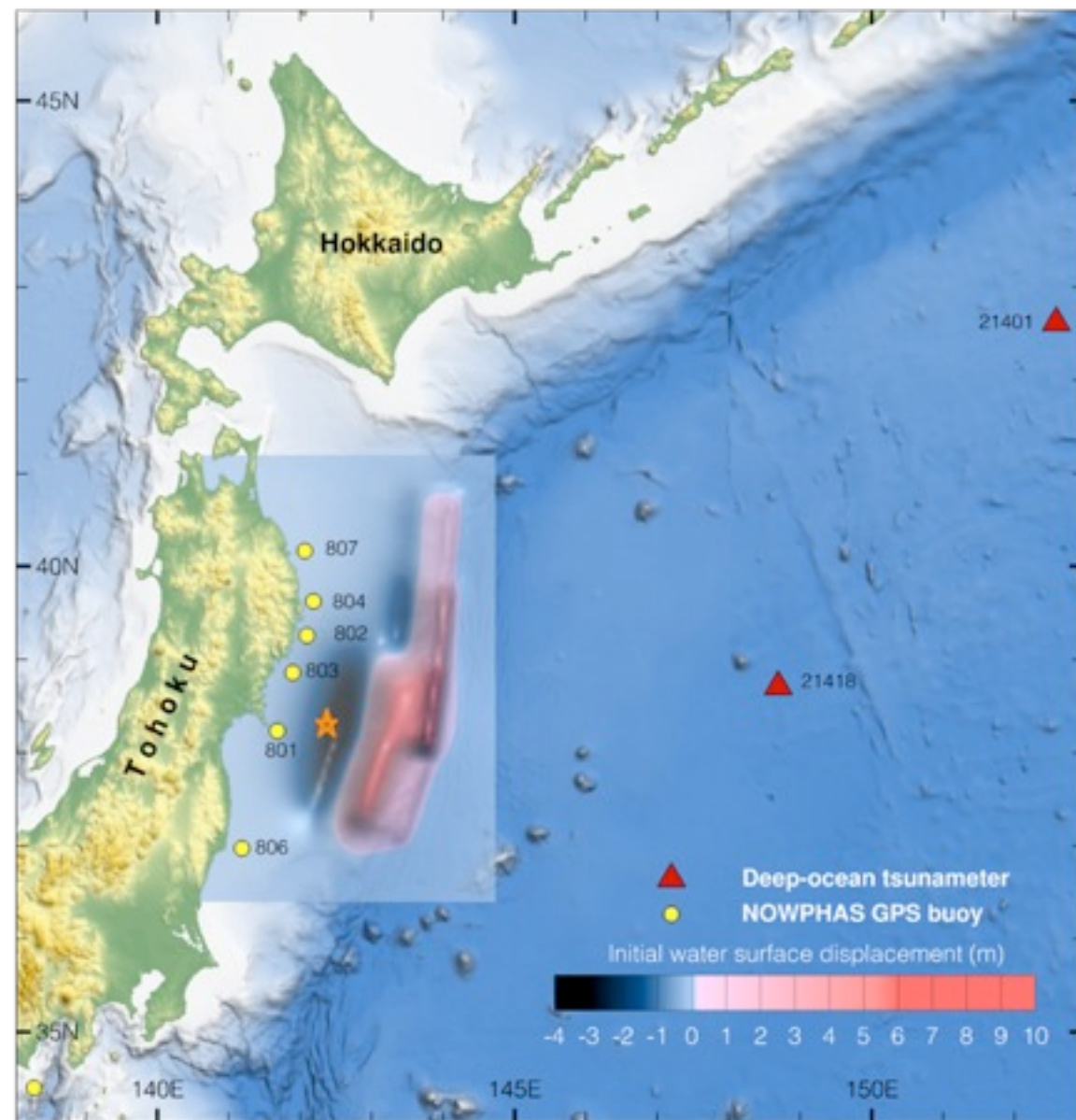


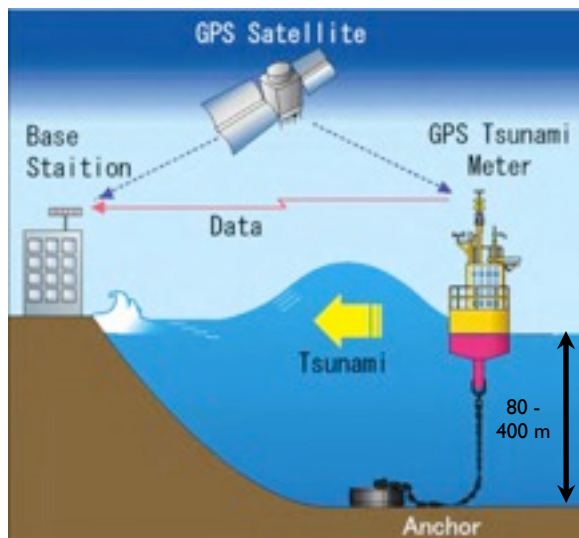
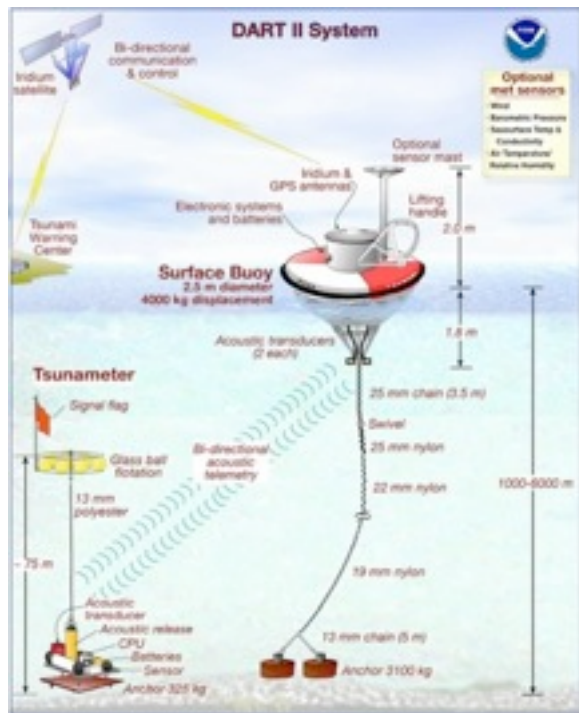
August 10, 2009 Andaman



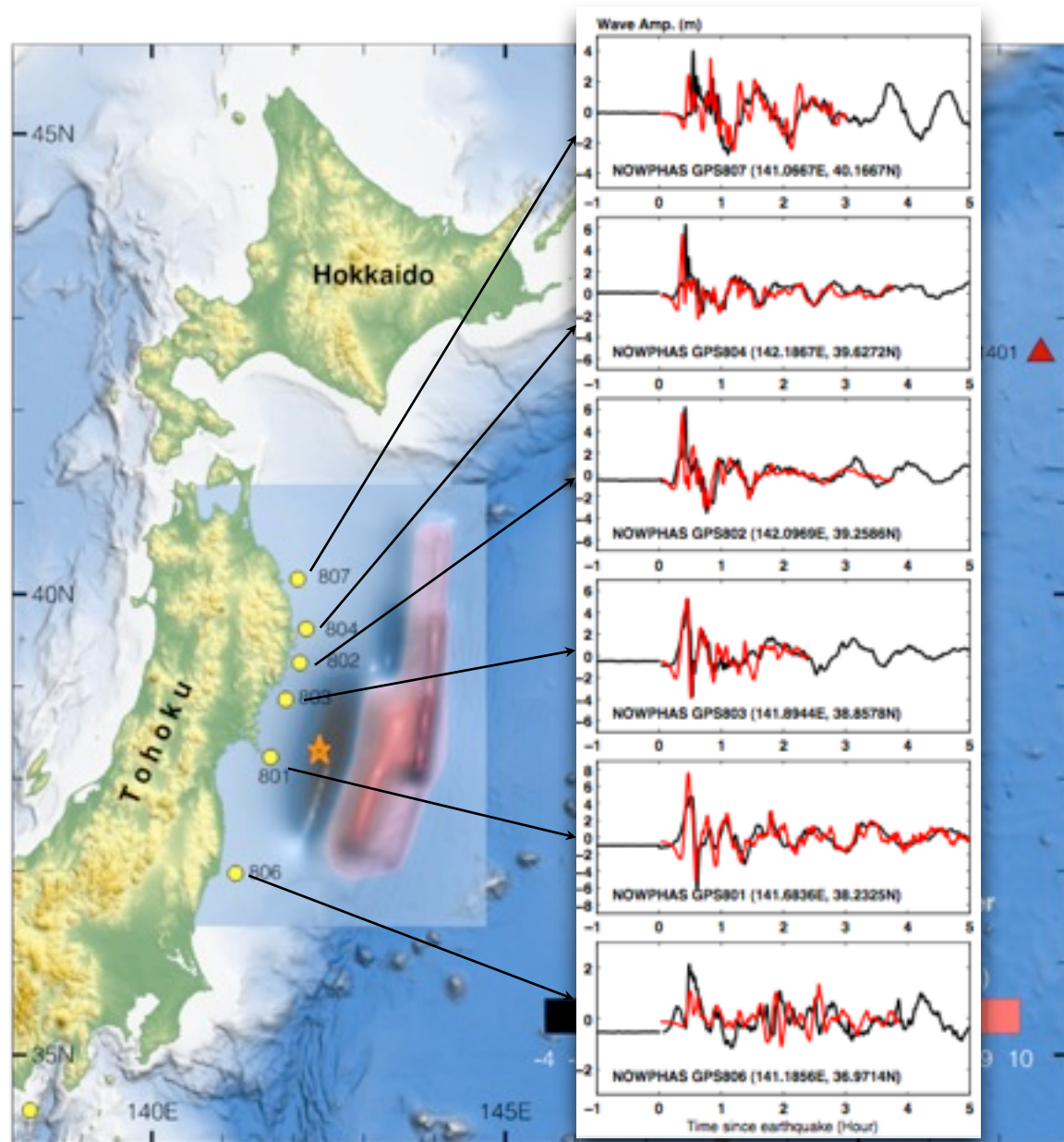


Courtesy of Kato et al.





Courtesy of Kato et al.



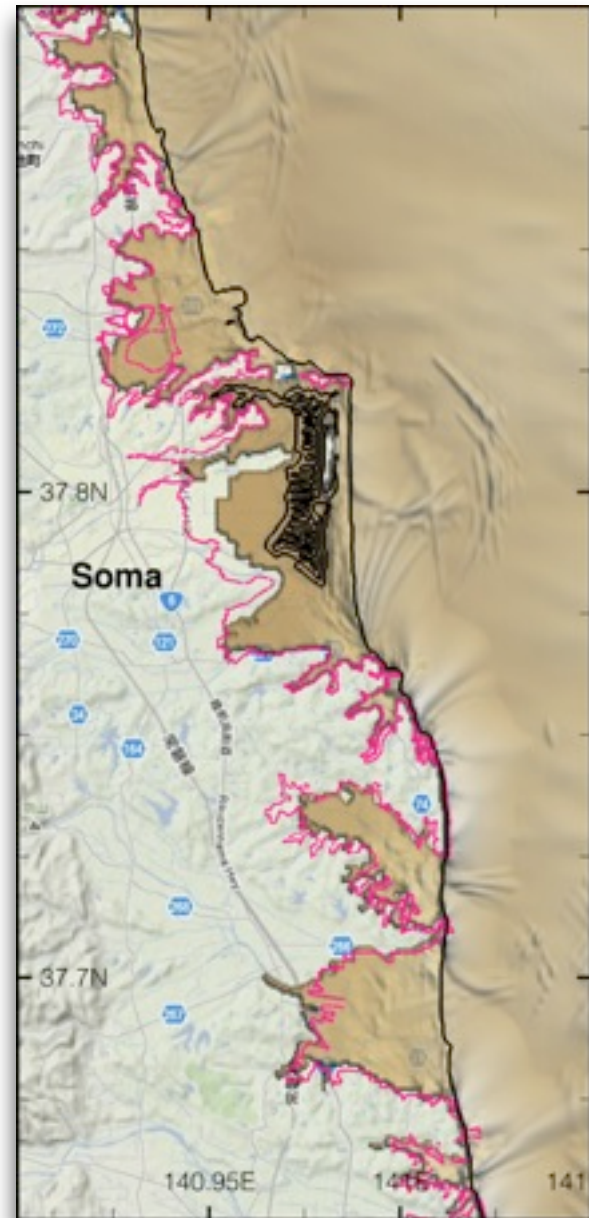
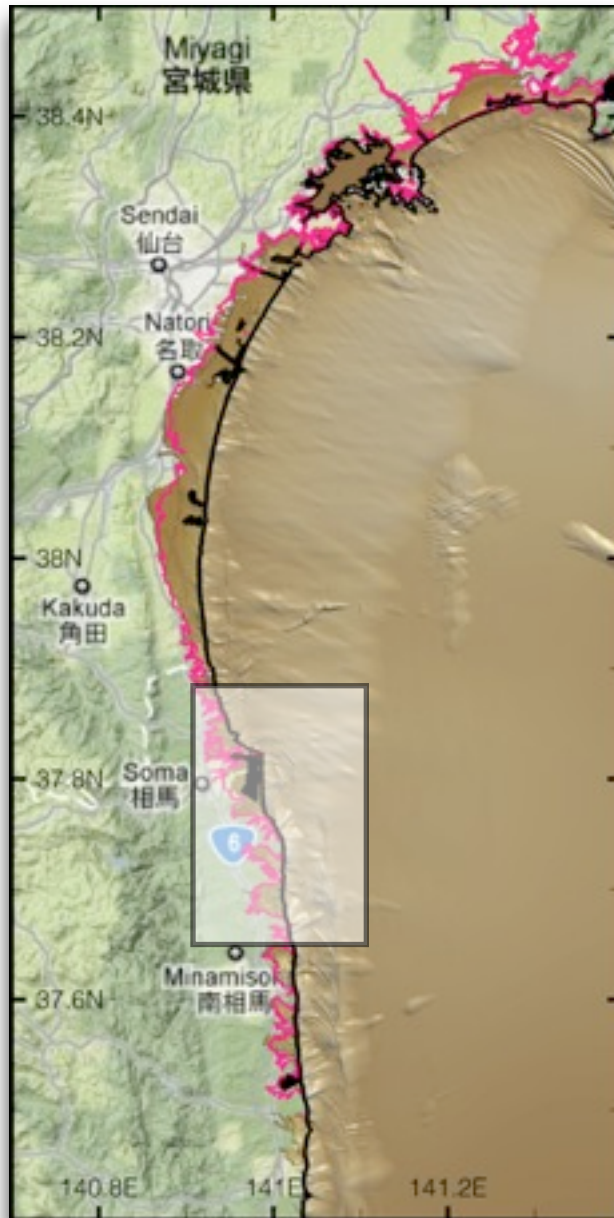
Local Forecast Test



Local Forecast Test

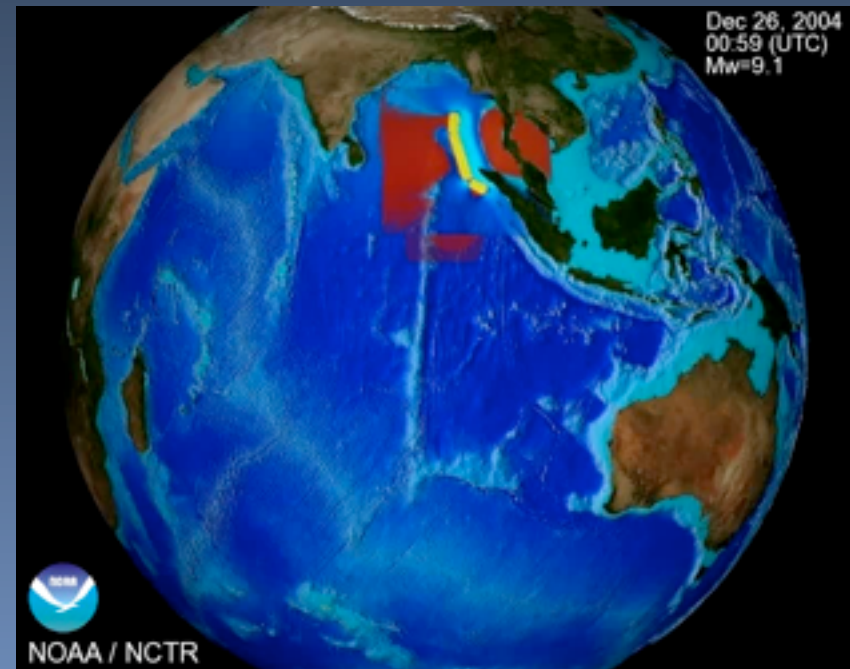


Local Forecast Test



Summary - NOAA's numerical forecasting techniques

- Earthquakes are the major generation mechanism, but tsunamis can have more than one.
- The source is complicated, so we measure the wave directly.
- DART buoy data helps us to constrain the model
- Inverted propagation model is used to force the inundation model.



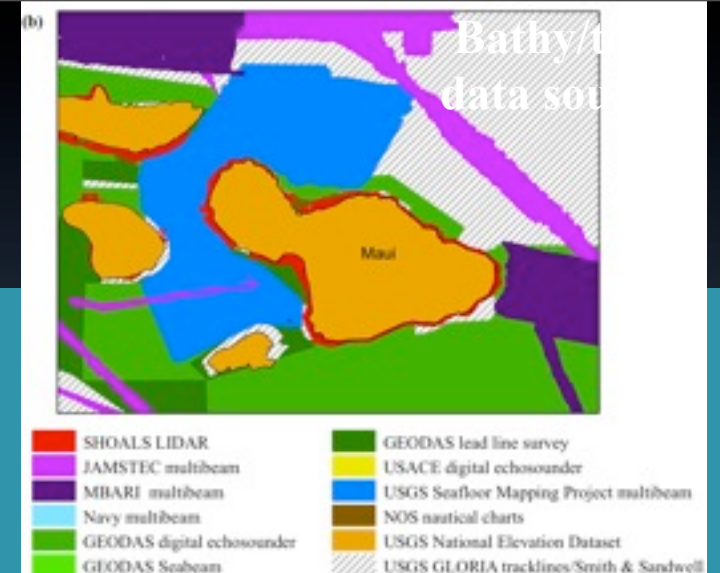
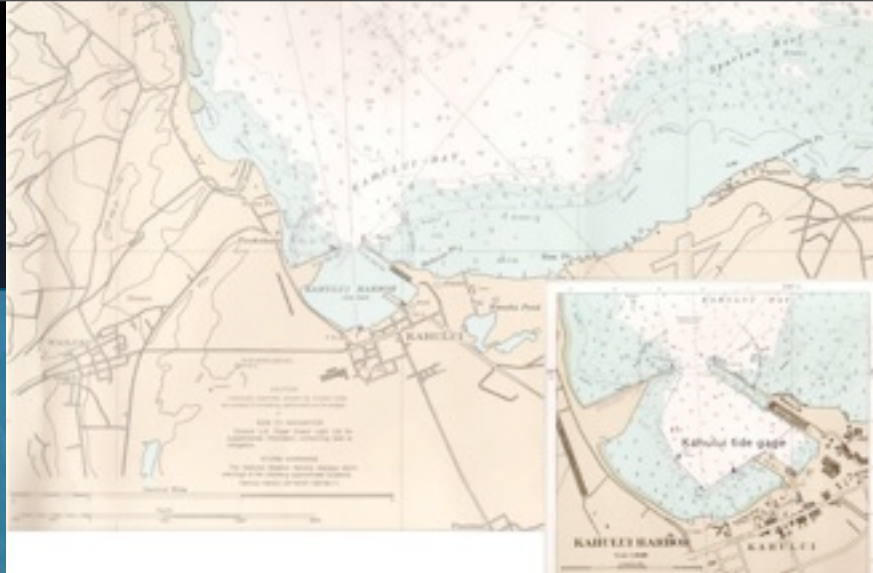
Stop Here

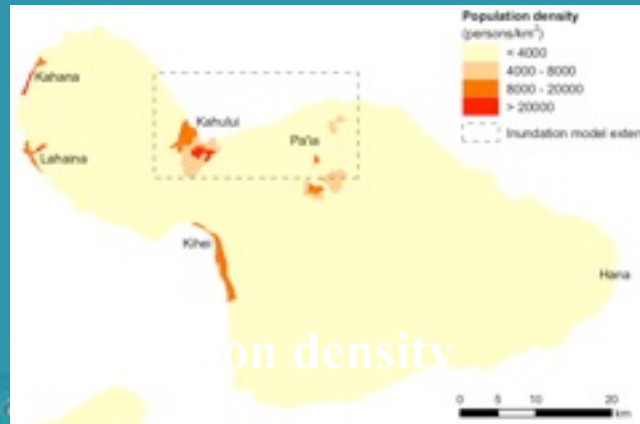
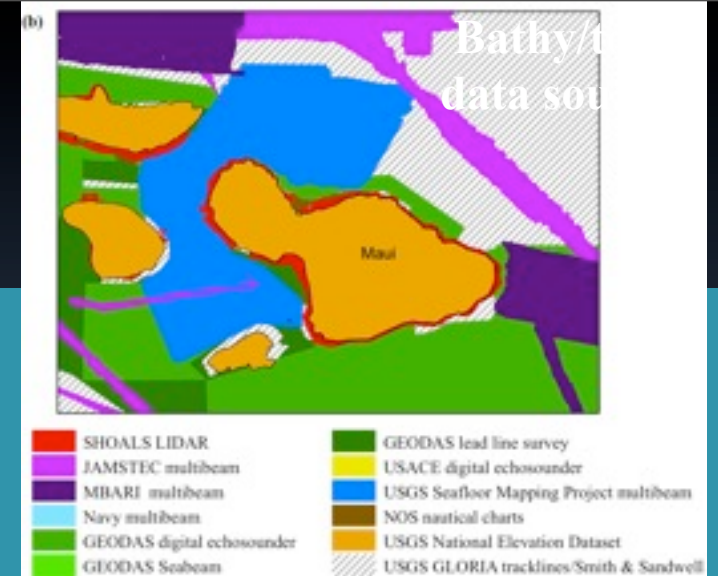
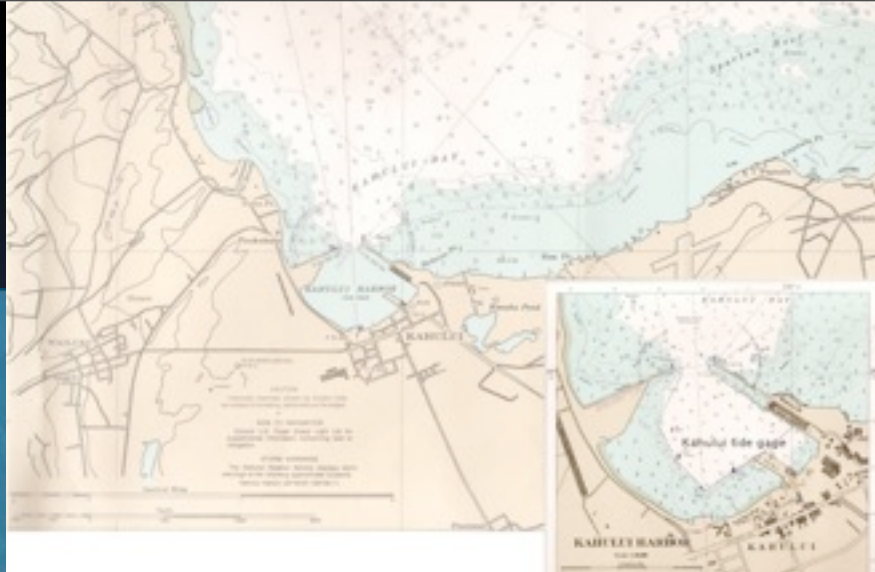
Developing Inundation Grids

- Reference model uses the highest quality and resolution available for a community
- Model from different sources is combined to form 3 nested grids
- Tested against historical data, and for robustness
- Highly optimized grids are derived from the reference grids

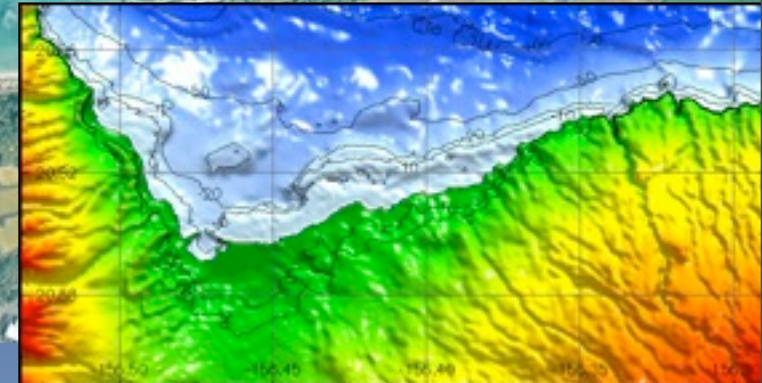
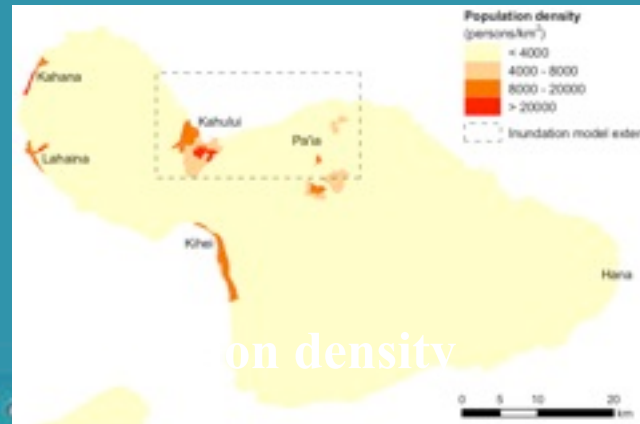
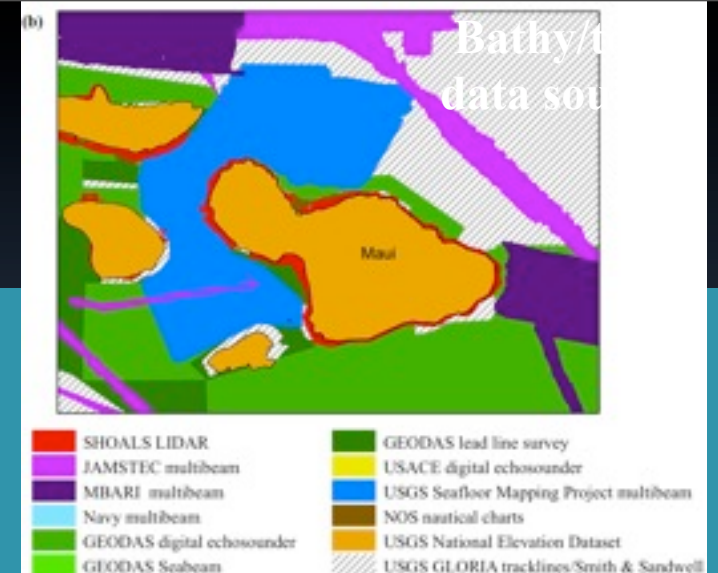
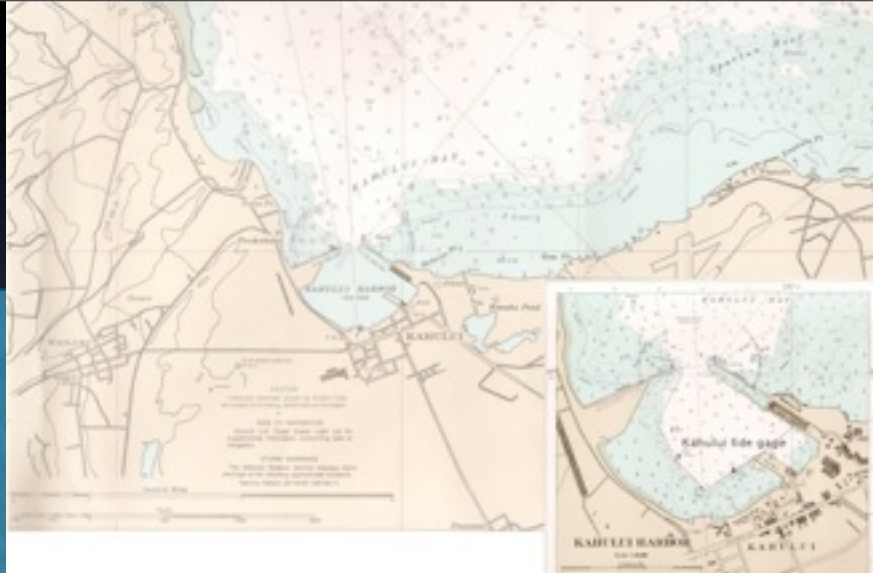


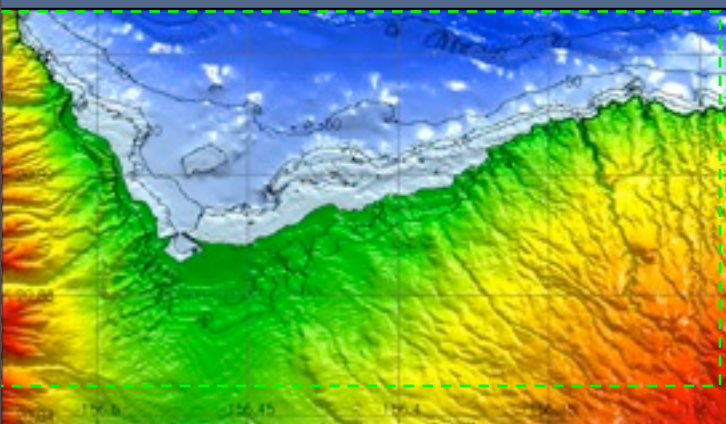
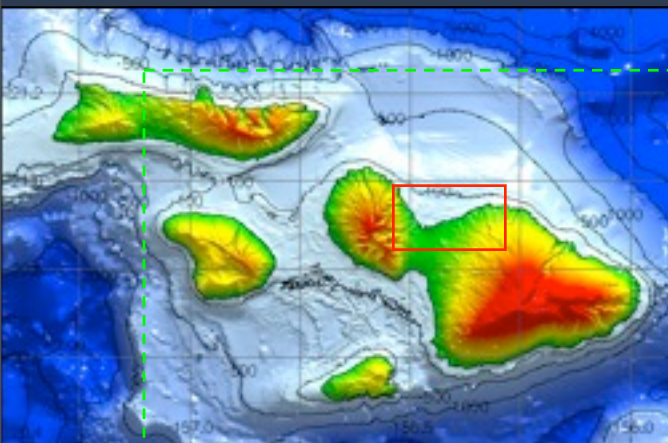
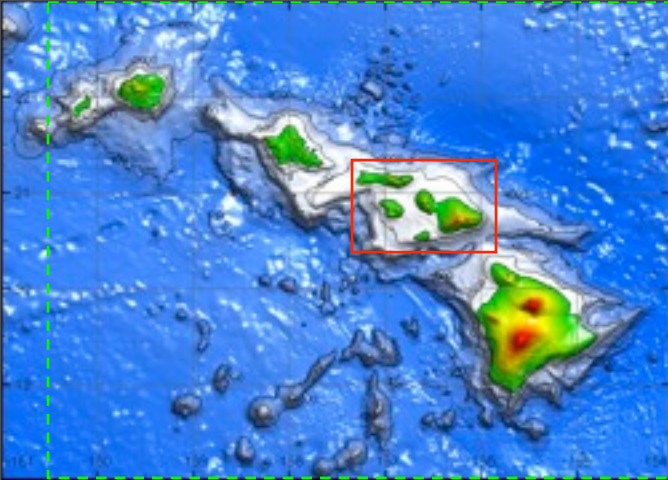


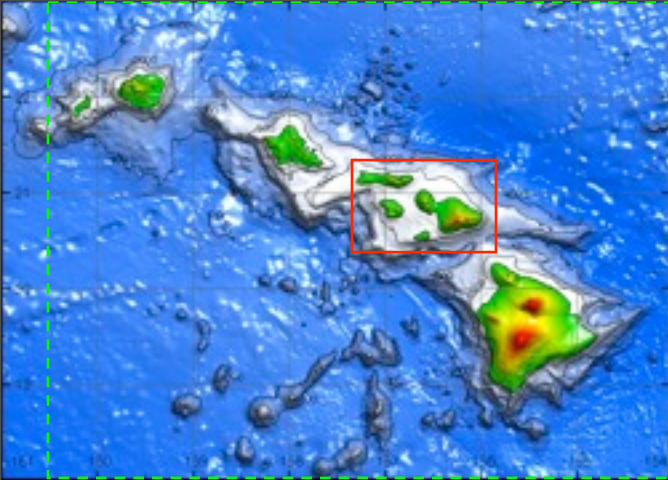




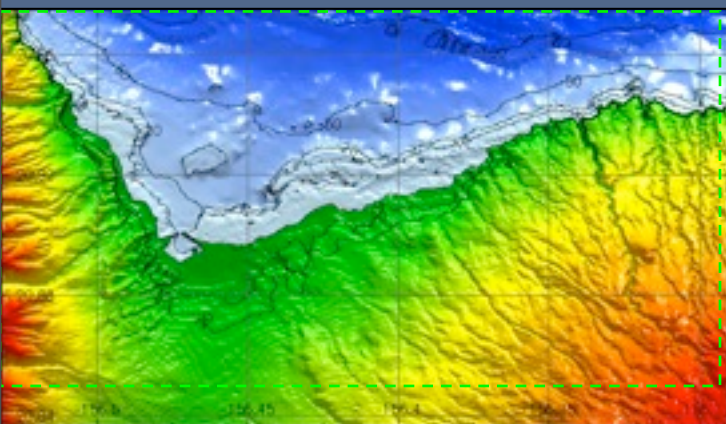
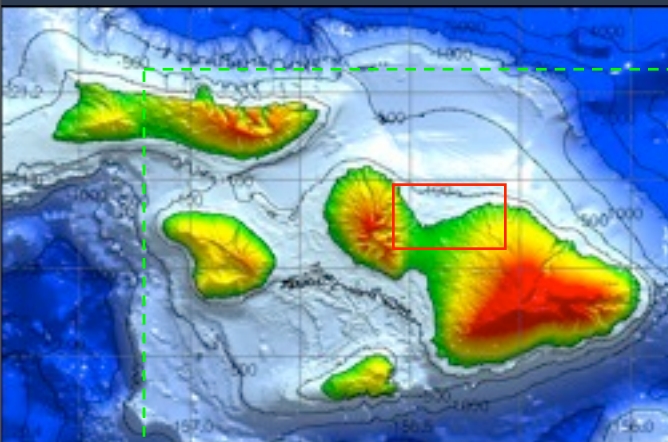
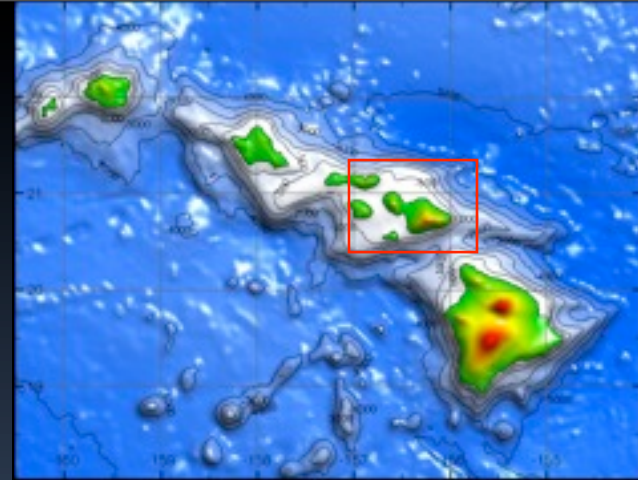
on density

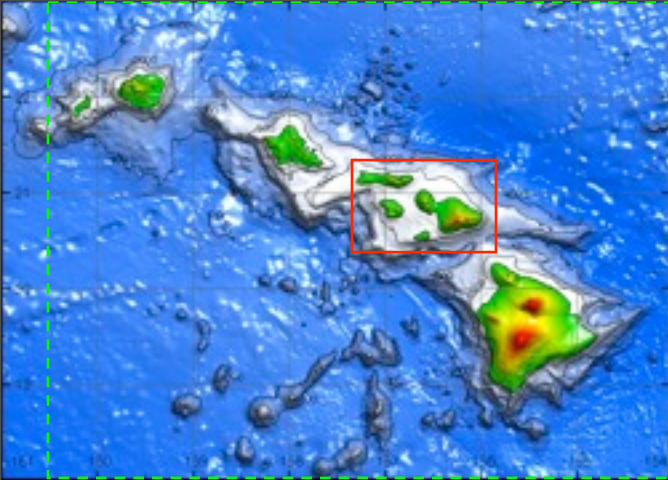




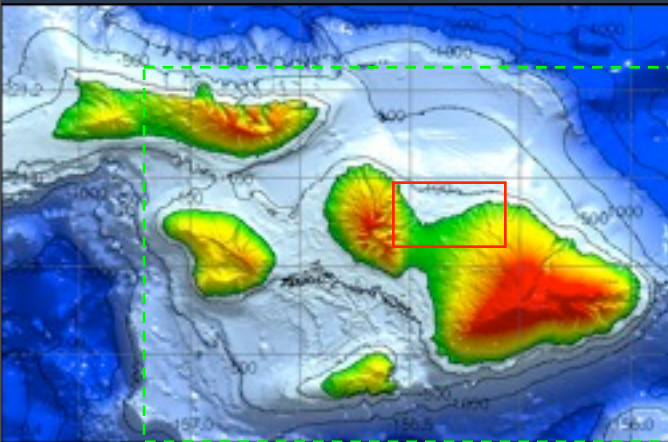
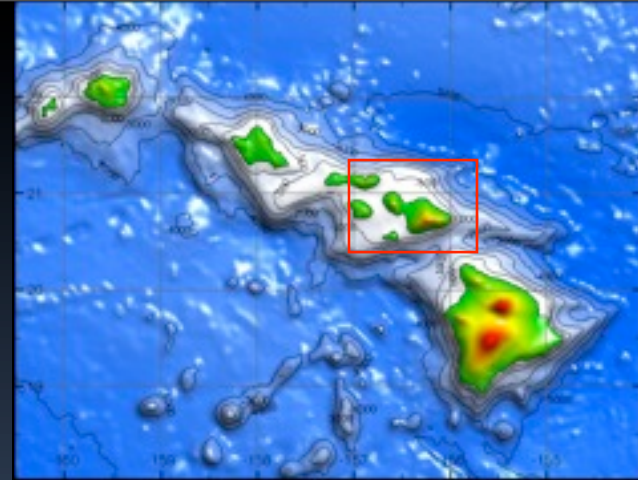


Resolution: 36" to 120"
Grid Size: 700x500 to 196x150
Time Step: 2 to 12 sec

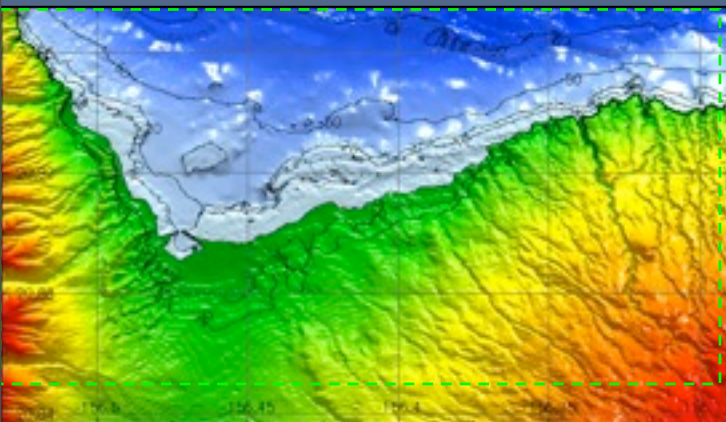
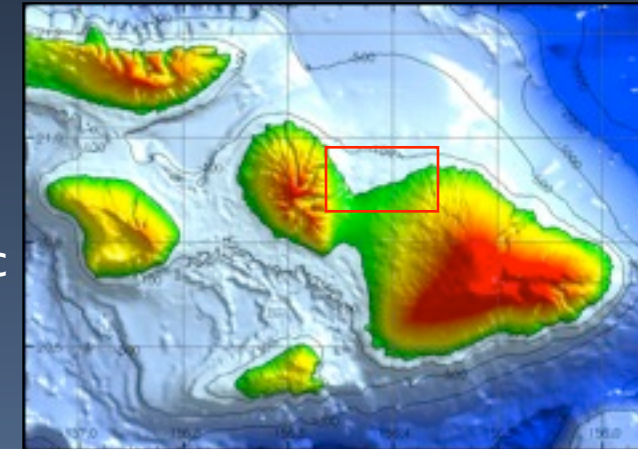


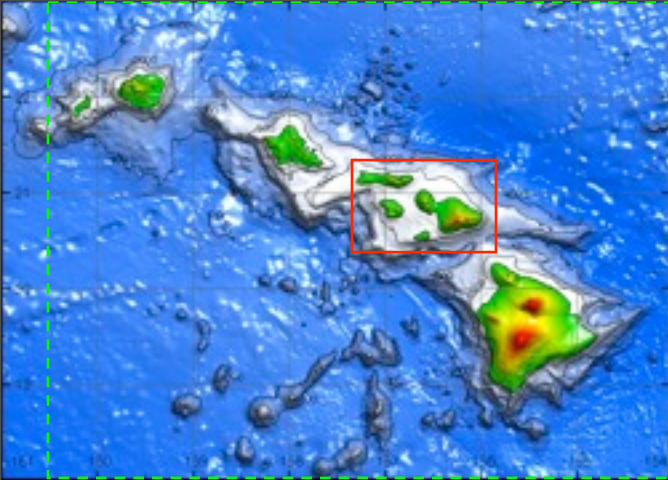


Resolution: 36" to 120"
Grid Size: 700x500 to 196x150
Time Step: 2 to 12 sec

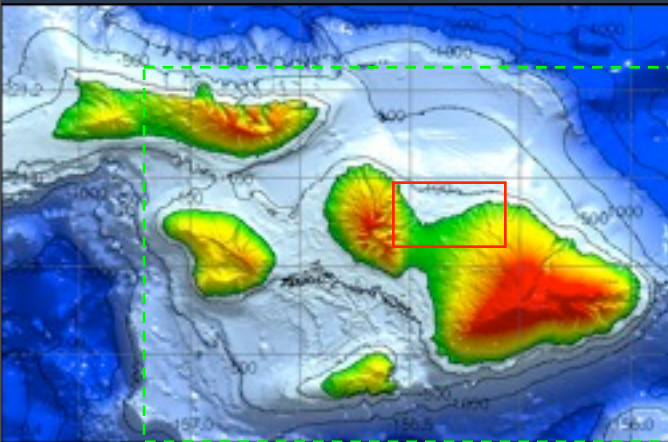
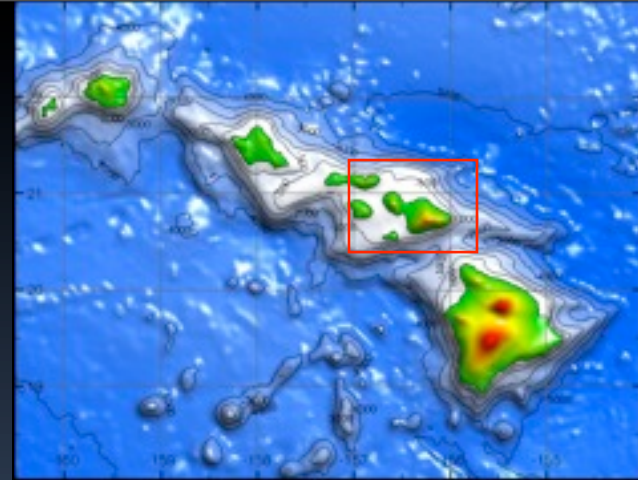


Resolution: 6" to 12"
Grid Size: 917x597 to 361x257
Time Step: 0.4 to 1.5 sec

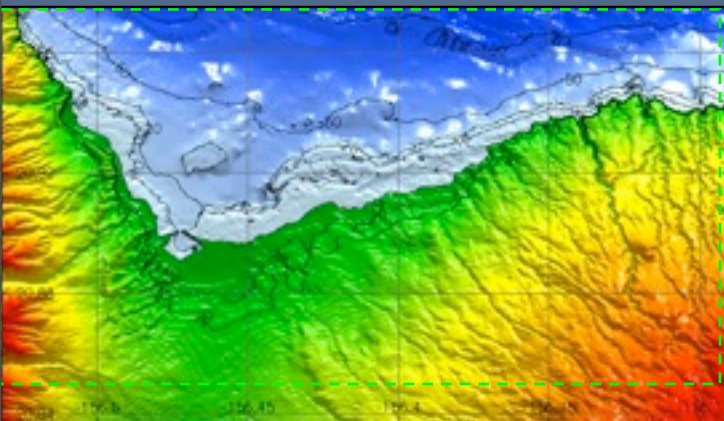
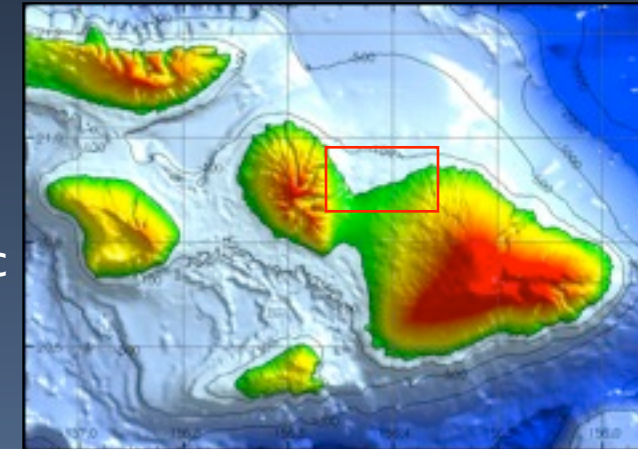




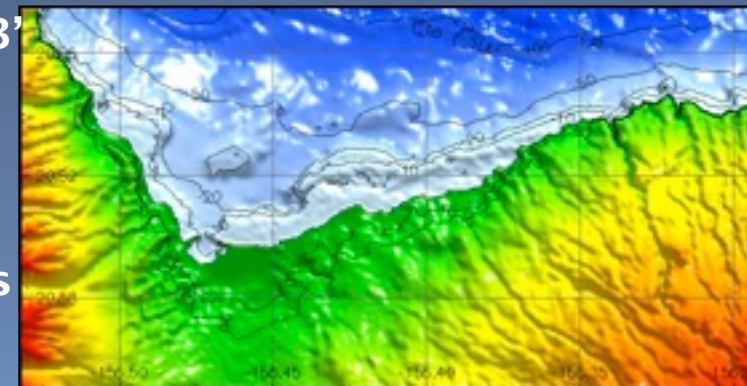
Resolution: 36" to 120"
Grid Size: 700x500 to
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Time Step: 2 to 12 sec



Resolution: 6" to 12"
Grid Size: 917x597 to
361x257
Time Step: 0.4 to 1.5 sec

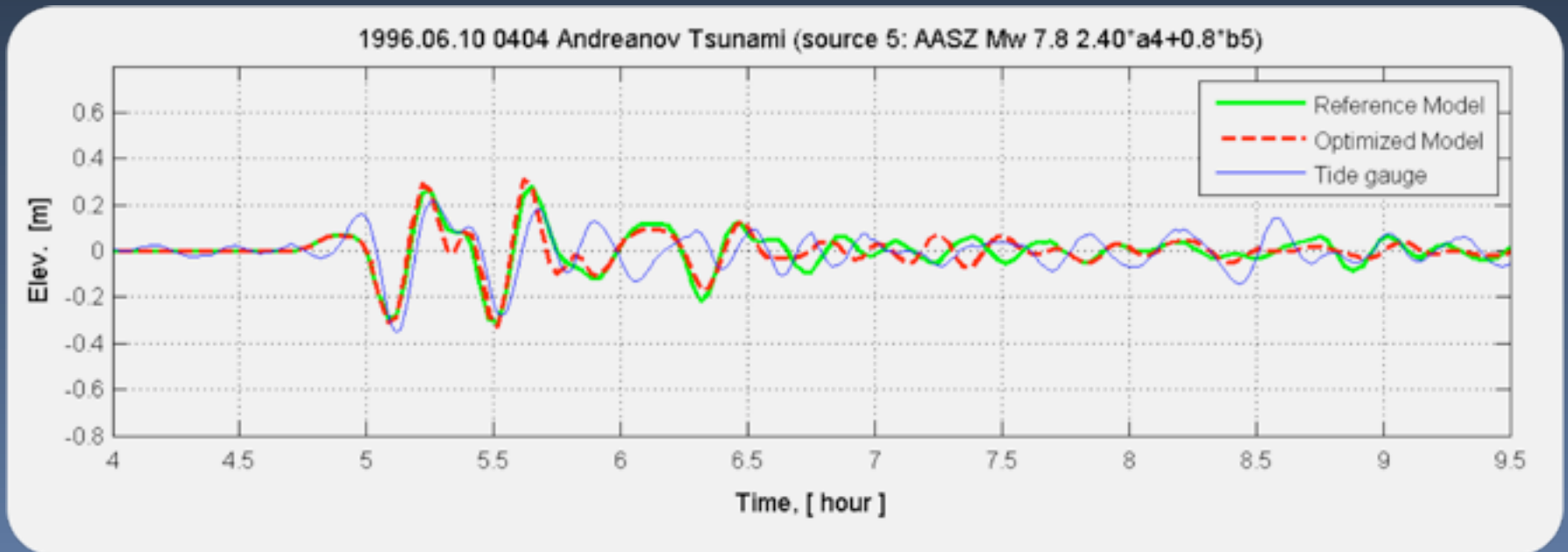


Resolution: 1" to 13"
Grid Size: 872x500
to 291x150
Time Step: 0.2 to
1.5 sec
Run Time: 8+ hours
to 10- min



Creation of the SIM Set of Grids

Monitor time series degradation at Warning Point and/or Tide Gage by comparison with Reference Run. (No tide-gage data available for Seaside)



Graphics by Liujuan Tang UW/JISAO & NOAA/NCTR